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# Numerical tools and methodologies for generating and refining kinetic models of lean $\text{NO}_x$ traps

**Anthony McDaniel**  
**Combustion Research Facility**  
**Sandia National Laboratories, Livermore, CA**



# Topics for discussion

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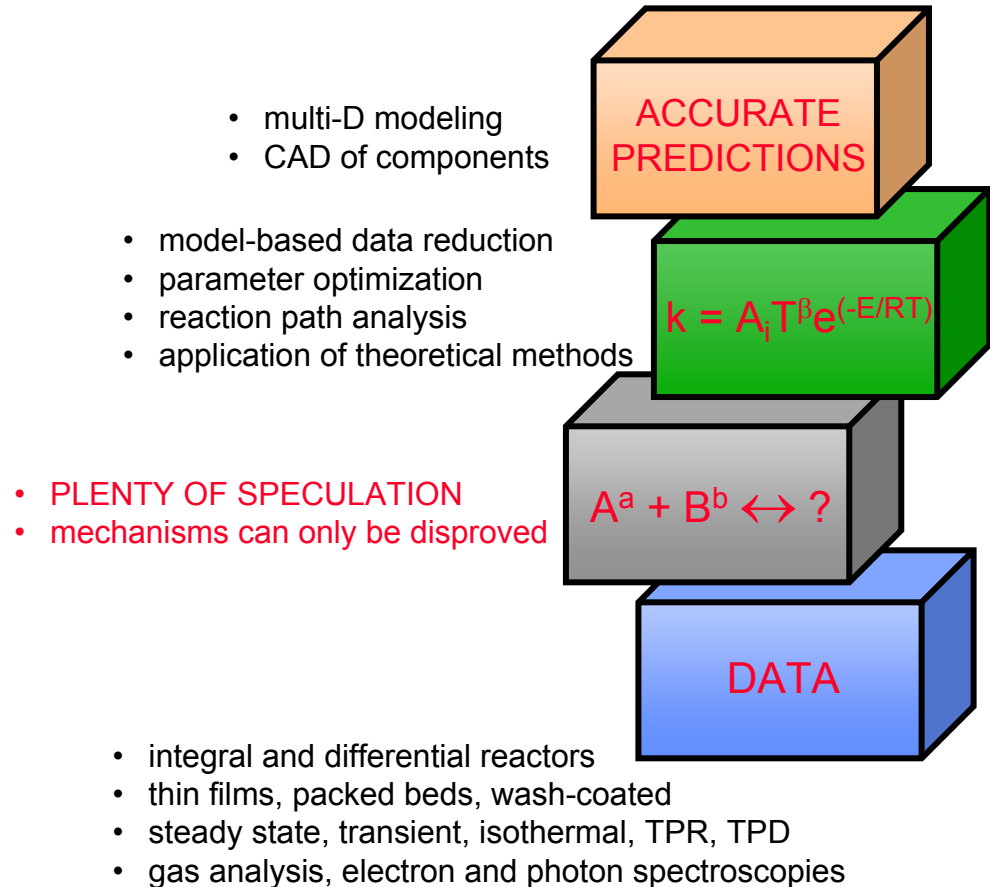
- **General framework for building and testing kinetic models**
  - Data sets, theory, and numerical tools
- **Application of transient perfectly stirred reactor code (PSR)**
  - Chemkin tool
  - Published mechanisms
  - Pt/Al<sub>2</sub>O<sub>3</sub>, BaO/Al<sub>2</sub>O<sub>3</sub>, Pt/BaO/Al<sub>2</sub>O<sub>3</sub> literature results
  - CLEERS SCONO<sub>x</sub> material
- **DAKOTA**
  - Design optimization, parameter estimation, uncertainty quantification, and sensitivity analysis
- **Commercial versus open source (GNU)**
  - Chemkin
  - Cantera
- **Path forward**



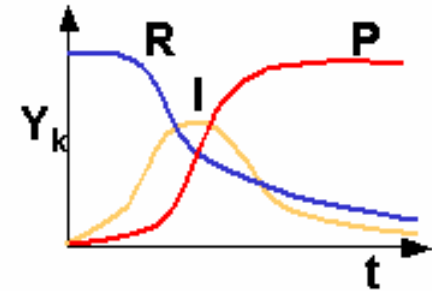
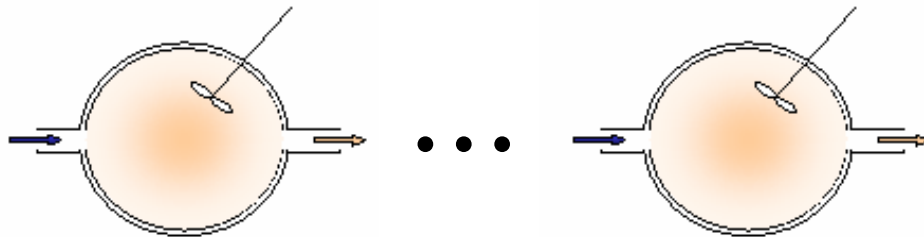
# Building kinetic models



- **Validate, refine and apply kinetic model**
- **Resolve model parameters**
  - Theory
  - Numerical tools
- **Formulate mechanistic detail**
  - Rate laws
- **Experiments**
  - Identify major players
    - product species
    - adsorbates
  - **Capture critical P, T, C dependencies**



# Lean NOx traps as perfectly stirred reactors



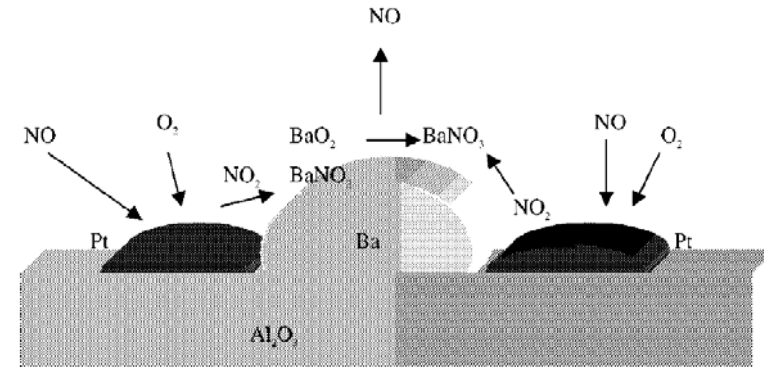
- **RD Chemkin**
  - Collection of problem-independent algorithms to manage computation and provide information
    - species, reactions, thermodynamic and transport properties
  - Suite of 0-, 1-, and 2-D reacting flow simulators
- **Have a transient PSR model**
  - Linked in series
  - User defined
    - T, [C] profiles, active area fraction
  - Equations integrated over  $V_R$  as opposed to  $M_{cat}$
- **Need a transient plug flow model**
  - Pore diffusion, surface transport



# Evaluation of published mechanisms



- **Mechanisms are scarce and often not transferable**
  - Tuned to a particular data set
  - **Pt/Al<sub>2</sub>O<sub>3</sub>** most abundant
    - TWC, catalytic combustion, POX
    - NO reduction still debatable
  - **BaO/Al<sub>2</sub>O<sub>3</sub> + Pt/BaO/Al<sub>2</sub>O<sub>3</sub>**
    - high degree of speculation
    - only 1 published as of 2003
- **Conversion to Chemkin formulation not trivial**
  - **Pseudo-first order TOF space to mass action kinetics**
  - **Transport of NO<sub>2</sub>(s) between Pt(s) and BaONO<sub>3</sub>(s) not available in PSR model**



## Olsson et al. (storage)

- adsorption/desorption of O<sub>2</sub>, NO, NO<sub>2</sub>
- surface reactions O(s), NO(s), NO<sub>2</sub>(s)
- **transport of NO<sub>2</sub>(s) from Pt(s) to BaONO<sub>3</sub>(s)**

## Deutschmann et al. (reduction)

- adsorption/desorption of H<sub>2</sub>, CO, H<sub>2</sub>O, CO<sub>2</sub>
- surface reactions  
H(s), OH(s), O(s), C(s), CO(s), CO<sub>2</sub>(s)

## Hoebink et al. (NO reduction)

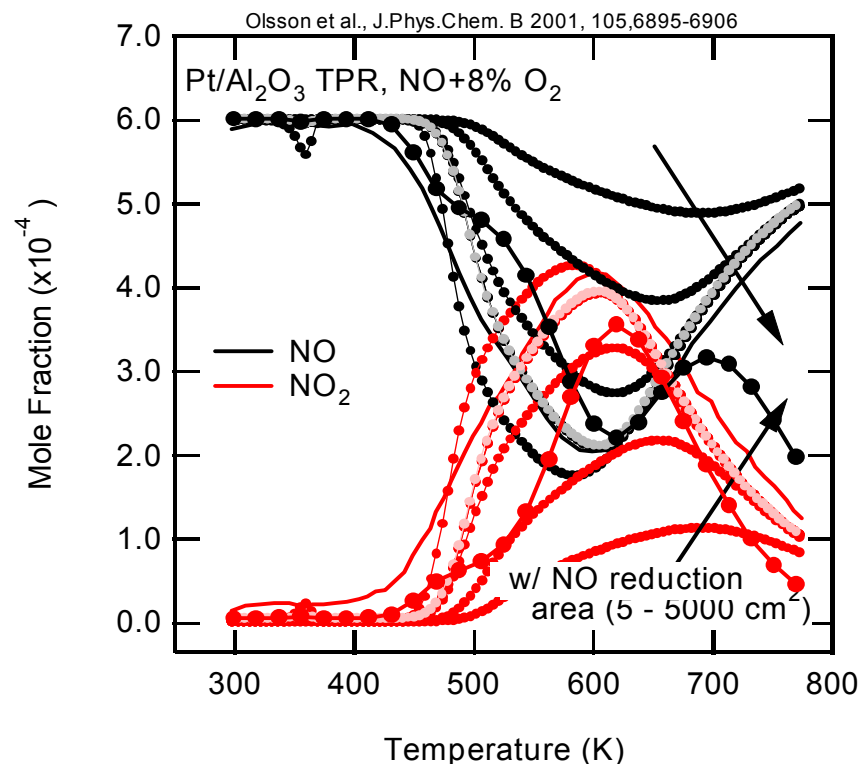
- desorption of N<sub>2</sub>
- surface reactions NO(s), N(s), O(s)



# TPR of NO + O<sub>2</sub> over Pt/Al<sub>2</sub>O<sub>3</sub>



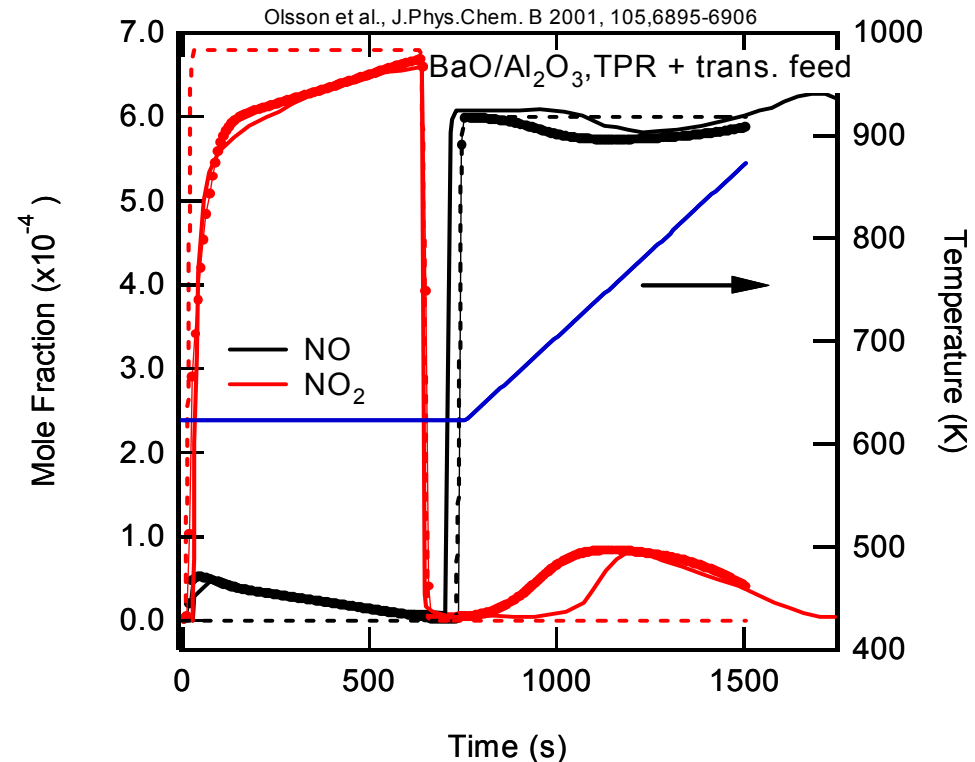
- **Chemkin prediction**
  - **Good agreement obtained by** adjusting active area  
number of PSRs in series
- **Investigate the importance of NO reduction**
  - **Poor agreement**  
creates shoulder region at low T  
NO conversion too extreme at high T
- **WHY?**
  - **NO submodel not transferable?**
  - **Better agreement by retuning the modified mechanism?**
  - **NO reduction not important?**



# TPR (+ transient feed) of NO and NO<sub>2</sub> over BaO/Al<sub>2</sub>O<sub>3</sub>



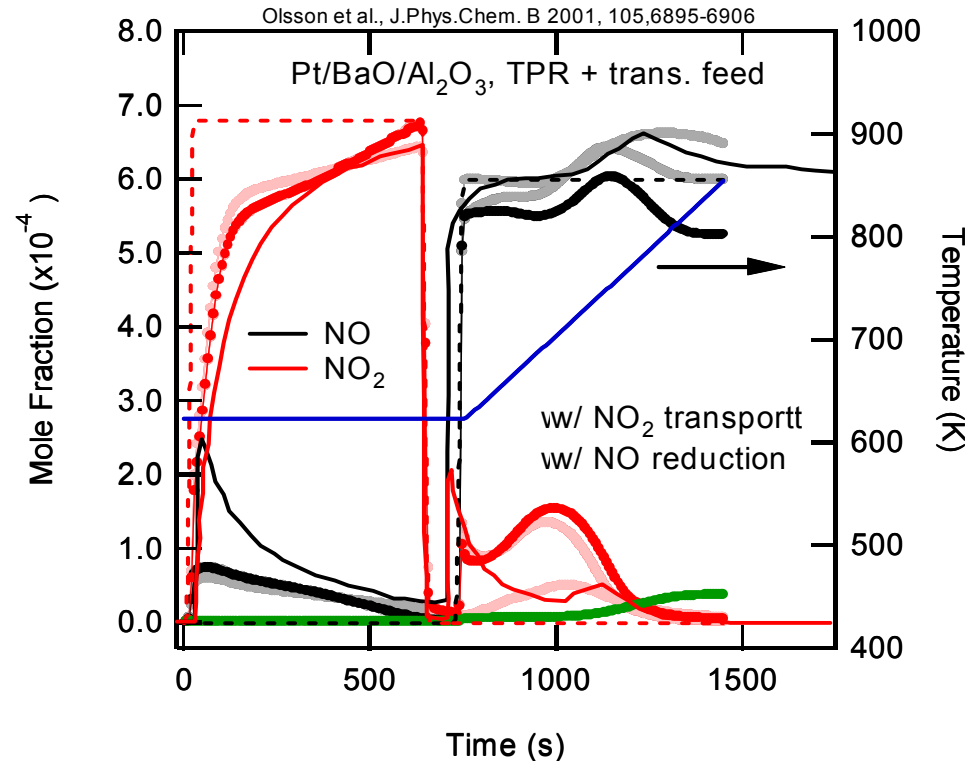
- **Experimental condition**
  - NO<sub>2</sub> exposure followed by NO
  - Linear temperature ramp
- **Observation**
  - NO formed during initial storage period
    - postulate surface oxidation
  - Broad NO<sub>2</sub> desorption peak
    - postulate coverage dependence
- **Chemkin prediction**
  - Good agreement with trends
  - Marginal agreement with peak shapes and positions



# TPR (+ transient feed) of NO and NO<sub>2</sub> over Pt/BaO/Al<sub>2</sub>O<sub>3</sub>

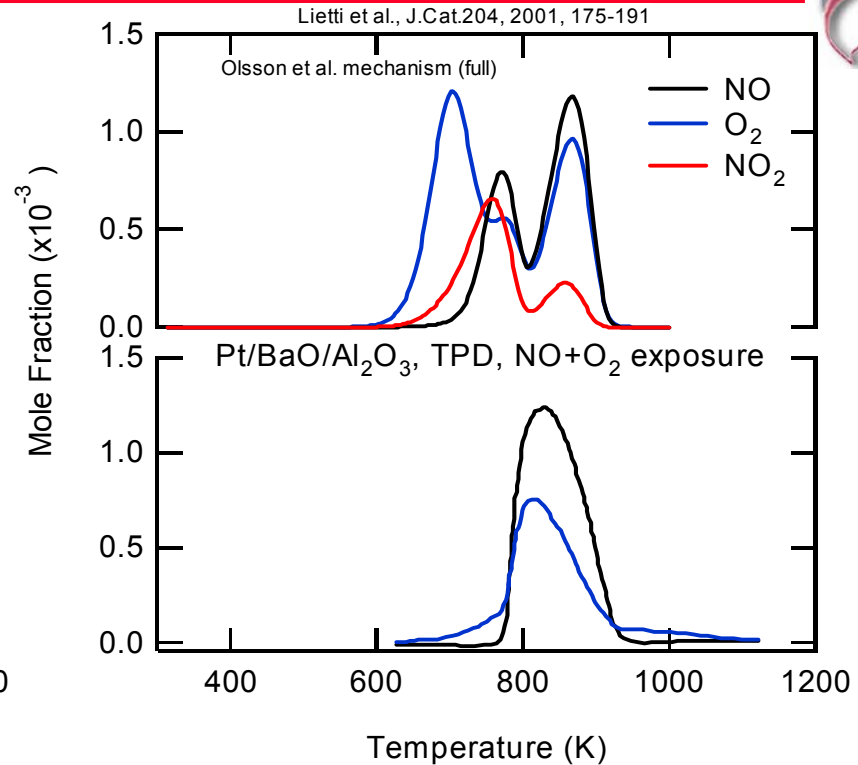
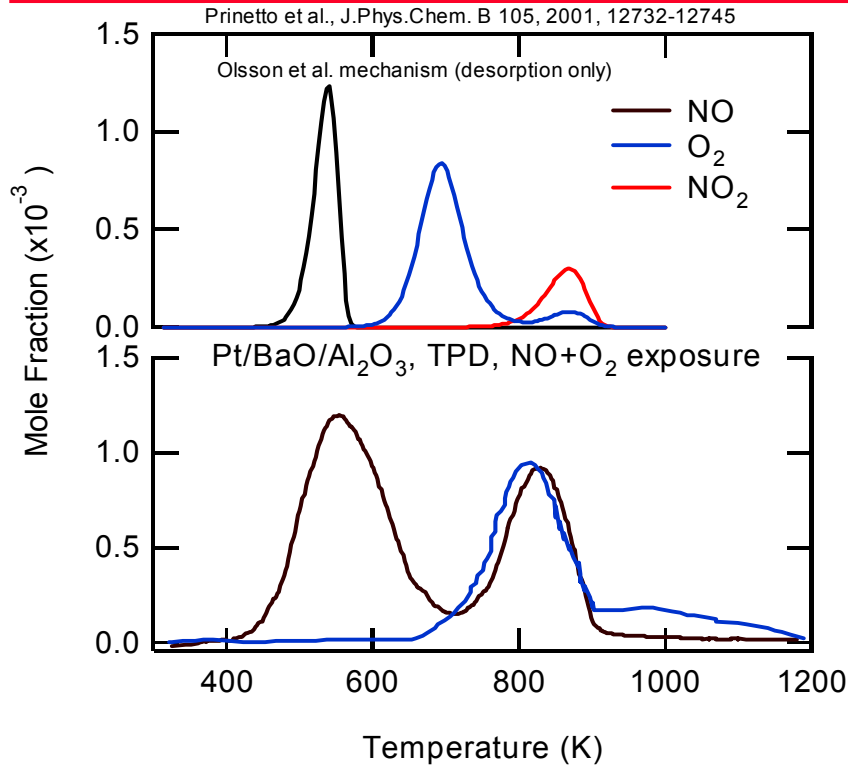


- **Experimental condition**
  - NO<sub>2</sub> exposure followed by NO
  - Linear temperature ramp
- **Observation**
  - NO<sub>2</sub> desorption at low T postulate spillover effect
- **Chemkin prediction**
  - Behaves like BaO material without spillover
  - Predict low T NO<sub>2</sub> desorption with spillover
  - NO reduction does not enhance prediction
  - Marginal agreement with peak shapes and positions





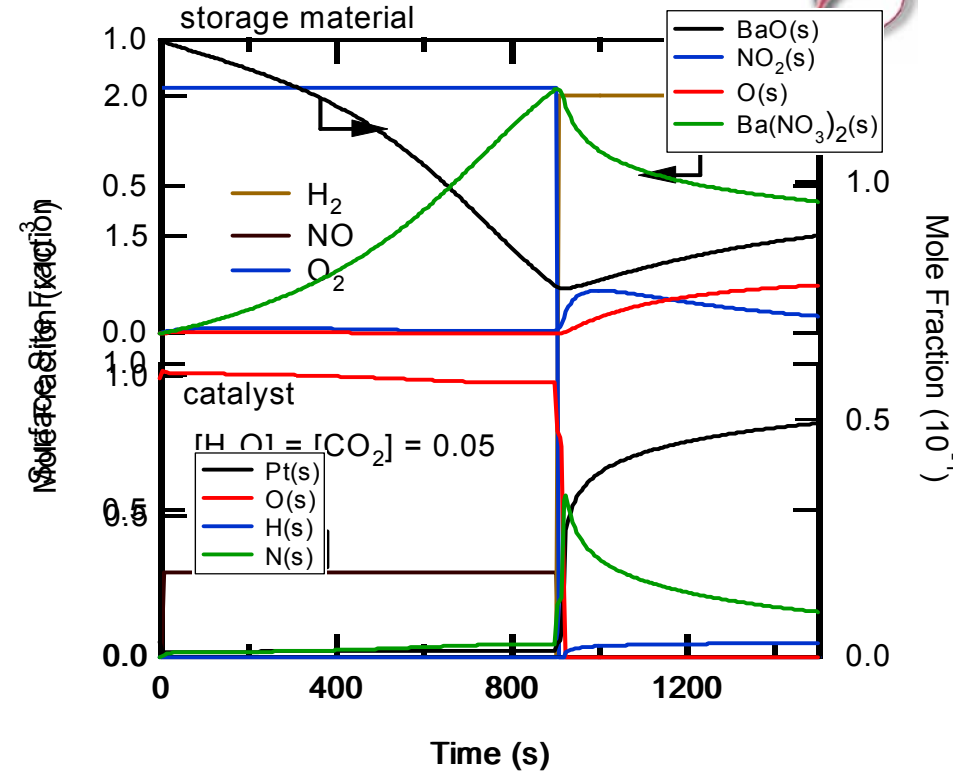
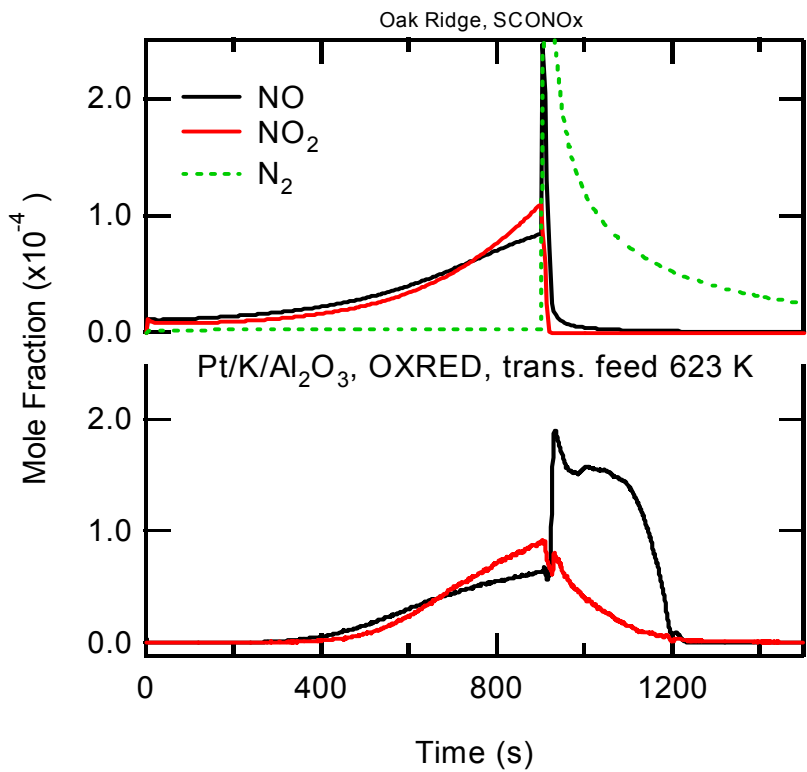
# Simulating TPD experiments



- **Key technique for extracting adsorbate energetics from data**
  - True TDP experiment samples irreversible desorption and surface reaction
- **Predicted behavior strongly dependent on initial state of surface**
  - Site fractions of adsorbates must be known or resolved recursively
- **Cannot reconcile U. di Torino data with Olsson mechanism**



# Oxidation-reduction cycle of SCONOx catalyst at 627 K



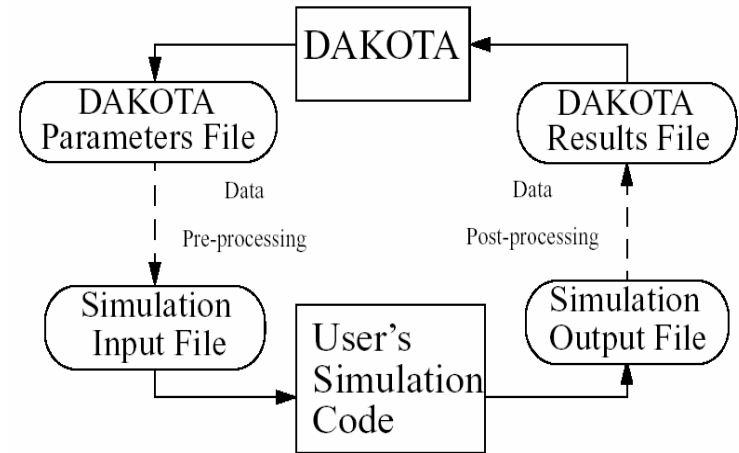
- **Combined Olsson+Deutschmann+Hoebink mechanism**
  - Missing H<sub>2</sub>O and CO<sub>2</sub> reactions with BaO (BaCO<sub>3</sub>, Ba(OH)<sub>2</sub>, etc...)
- **Capture significant trends in data**
  - NO / NO<sub>2</sub> cross over in oxidation cycle + large reductant-induced NO spike



# Extracting model parameters and more...



- **Model-based data reduction**
  - Simulation code
- **DAKOTA**
  - Numerous methods and strategies
  - Parameter study and optimization
    - gradient and non-gradient based
    - local and global search routines
    - sophisticated bounds control
  - Uncertainty quantification
    - effects of error propagation
    - define regions of validity for model
  - Sensitivity analysis
- **Flexible code interface**
  - Script driven or compiled



- Rely on data, theory, and thermodynamics to provide appropriate constraints for search algorithms
- Non-negative  $E_a$
- Thermodynamically consistent
- Appropriate bounds on  $A_i$



# Alternatives to commercial codes

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- **DAKOTA**
  - Available for download from SNL website
  - C++ open source (GNU)
- **Cantera**
  - Chemkin and Surface Chemkin analog
  - Link to download @ Prof. David Goodwin website (Cal. Tech.)
  - C++ open source (GNU), also runs under Python engine
  - Reaction path analysis tools
    - key to mechanism reduction and generating artificial kinetic maps
  - Simulation tools beginning to emerge
- **Others?**
  - Warnatz group, Germany



# Path forward

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- **Continue to search and catalog open literature for relevant information**
  - Modelable data sets
  - Theoretical results (first principles calculations)
- **Take Chemkin applications coupled to DAKOTA as far as possible**
  - Transient PSR models
  - Equilibrium calculations (phase diagram)  
BaCO<sub>3</sub>, Ba(OH)<sub>x</sub>, etc ...
- **Create a transient plug flow model**
  - Pore diffusion / reaction and surface transport models
- **Develop and refine detailed kinetic models for lean NO<sub>x</sub> traps**
  - Standardize and benchmark both kinetic mechanisms and models

