

# Optimal NH<sub>3</sub> Storage in SCR Catalysts

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- Progress in advanced combustion technologies has made the exhaust temperature cooler
- Urea-SCR performance during low temperature operating conditions is a concern in meeting future emission legislation
- Maintaining optimum set levels of  $\text{NH}_3$  in the catalyst is critical for higher  $\text{NO}_x$  control performance during low temperatures
- One approach is to design an optimal urea injection control strategy that minimizes  $\text{NO}_x$  and  $\text{NH}_3$  emissions simultaneously.

- Data Driven Control Strategies
- ILC Strategy using Hammerstein-Wiener Models
  - Learning H-W Models
  - Iterative Learning Control Strategy
- Model Free Adaptive Control Strategy
- Simulation Results
- Summary & Future Work

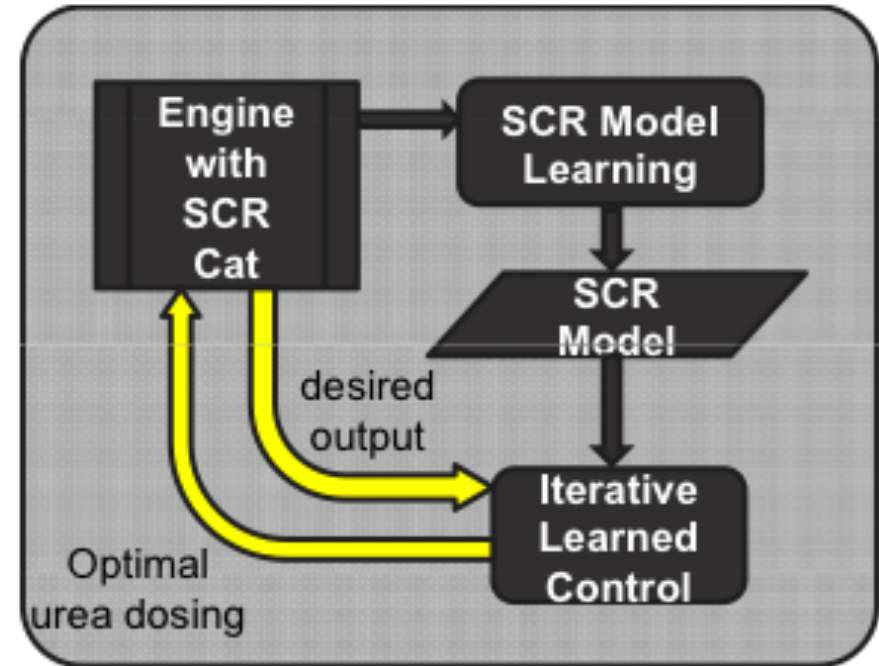
# Why Data Driven Control Strategies?

- Reducing high fidelity models into accurate lower order models is complex and sometimes an impossible task.
- Uncertainty in model parameters (pre-exponentials, activation energies) can be avoided.
- Data driven control strategies can be easily plugged in with the hardware and offer real time optimal solutions.
- Two data driven control strategies are presented
  - Iterative Learned Control (ILC)
  - Model Free Adaptive Control (MFAC)



# Process Flow for ILC Strategy

- Catalyst data measured on the engine is used to train the model.
- Learned model is then integrated with iterative learned control (ILC) strategy, optimal on H-W models, to design an urea injection strategy.



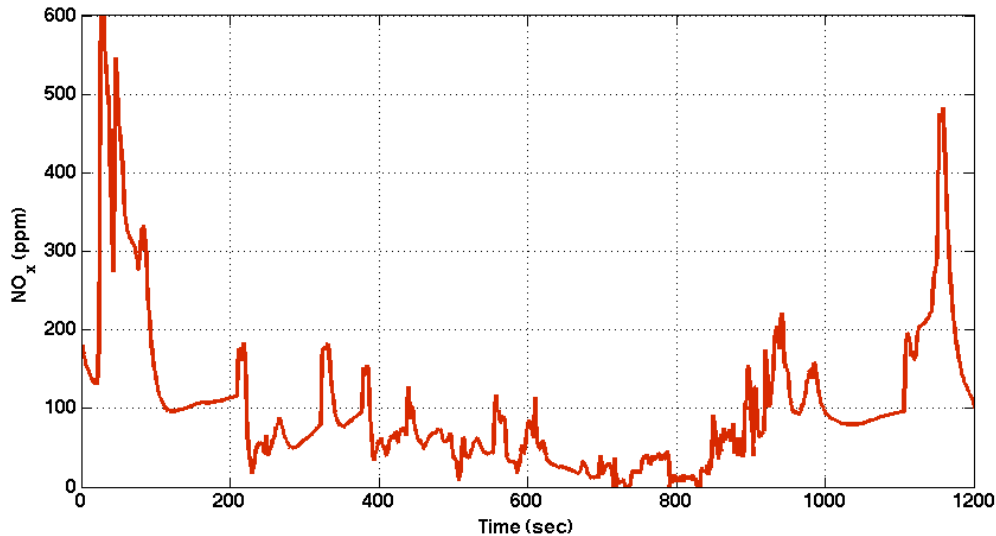
- Multiple input single output (MISO) models are developed for  $\text{NO}_x$  and  $\text{NH}_3$ .
- Both models use the following inputs

$$\begin{aligned}u_1 &= c_{\text{NH}_3, \text{in}} \\u_2 &= c_{\text{NO}_x, \text{in}} \\u_3 &= \dot{m} \\u_4 &= e^{-1e4/T_{\text{in}}}\end{aligned}$$

- Identification uses a recursive prediction error method (RPEM) with a restricted black box parametrization<sup>1</sup>.
- Algorithm identifies the coefficients of a polynomial in states, inputs and derivative of inputs.

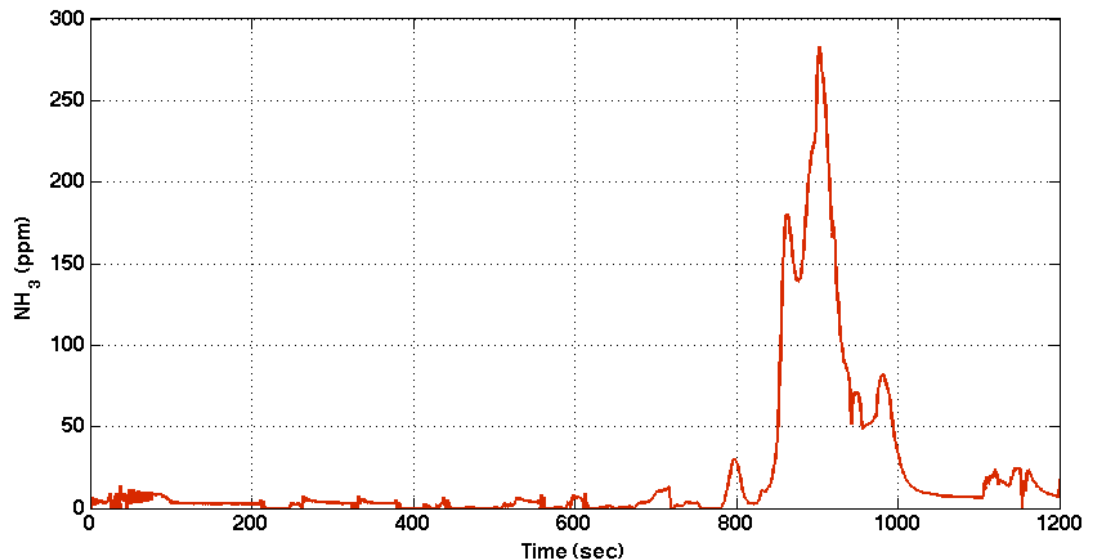
<sup>1</sup> Tayamon, S., and Wigren, T., American Control Conference, 2010

# Learned Models Validation



- Learned model fits the measured FTP data well (not shown here)
- Low root mean square error in NO<sub>x</sub> and NH<sub>3</sub> models

Need to validate on multiple data sets for more confidence in the model.



- ILC guarantees optimality for H-W models.
- Algorithm is simple and well grounded in stochastic control theory

Denote the tracking error by  $e_k(t) = y_d(t) - y_k(t)$ , where  $y_d$  is the desired output and  $y_k$  is the output at the  $k$ -th iteration. For each  $t$ ,  $u_0(t)$  is arbitrarily chosen.

The control signals at odd steps are given by

$$u_{2k+1}(t) = u_{2k}(t) + c_k \Delta_k(t),$$

The control signals at even steps are given recursively by

$$\begin{aligned} \bar{u}_{2(k+1)}(t) &= u_{2k}(t) - \frac{a_k}{c_k \Delta_k(t)} (|e_{2k+1}(t+1)|^2 - |e_{2k}(t+1)|^2), \\ &\quad u_{2(k+1)}(t) \cdot I_{[|\bar{u}_{2(k+1)}| \leq M_{\sigma_k(t)}]}, \\ \sigma_k(t) &= \sum_{l=1}^{k-1} I_{[|\bar{u}_{2(l+1)}| > M_{\sigma_l(t)}]}, \\ \sigma_0(t) &= 0. \end{aligned}$$

# Model Free Adaptive Control (MFAC)

A data driven control strategy that uses dynamic linearization to linearize a nonlinear system

$$y(k+1) = f(Y(k), U(k))$$

as

$$\Delta y(k+1) = \Phi^T(k) \Delta U(k)$$

where  $Y$  and  $U$  are matrices containing signals from time  $k$  to time  $k-L$ ,  $\Phi_{n_u \times L} = [\phi_1 | \phi_2 | \dots | \phi_L]$  is a time-varying pseudo-Jacobi matrix, and  $n_u$  is the number of input signals. Starting with the control law

$$J(u(k)) = \|y^*(k+1) - y(k+1)\|^2 + \lambda \|\Delta U(k)\|^2$$

we derive an update rule for  $u(k)$ ,

$$u(k) = u(k-1) + \frac{\phi_1(k)}{\lambda + \|\phi_1(k)\|^2} \left[ \rho_1 (y^*(k+1) - y(k)) - \sum_{i=2}^L \rho_i \phi_i \Delta u(k-i+1) \right],$$

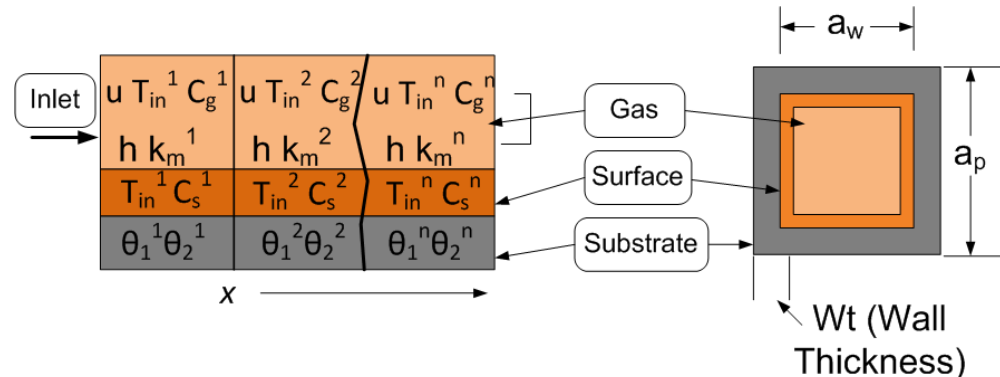
Energy criterion is used to find the update rule for  $\Phi$

$$J(\Phi(k)) = \|\Delta y(k) - \Phi^T(k) \Delta U(k-1)\|^2 + \mu \|\Delta \Phi(k)\|^2$$

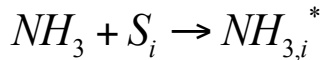
# Overview of MTU's SCR Model

MTU's SCR model was run using the MFAC strategy and the results are compared.

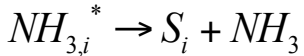
- 1D single channel model with gas and surface phase
- 2 NH<sub>3</sub> storage sites
- All reactions take place on the surface of the catalyst



## Chemical Reactions in the Model

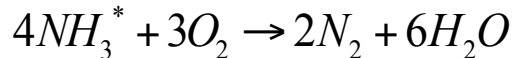


NH<sub>3</sub> Adsorption

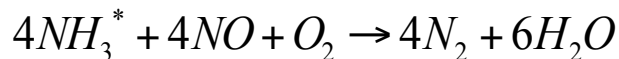


NH<sub>3</sub> Desorption

$i = Site1, Site2$



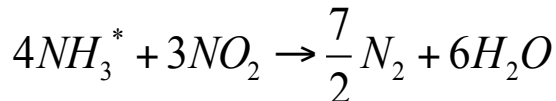
NH<sub>3</sub> oxidation



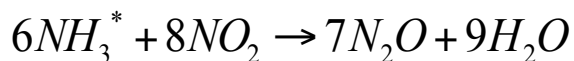
Standard SCR



Fast SCR



Slow SCR



N<sub>2</sub>O Formation

## Gas and Surface Phase Species Balance

$$\varepsilon \frac{\partial C_{g,i}}{\partial t} = -u \frac{\partial C_{g,i}}{\partial x} - \beta_i A_g (C_{g,i} - C_{s,i})$$

$$(1 - \varepsilon) \frac{\partial C_{s,i}}{\partial t} = \beta_i A_g (C_{g,i} - C_{s,i}) - \sum_j n_{i,j} R_j$$

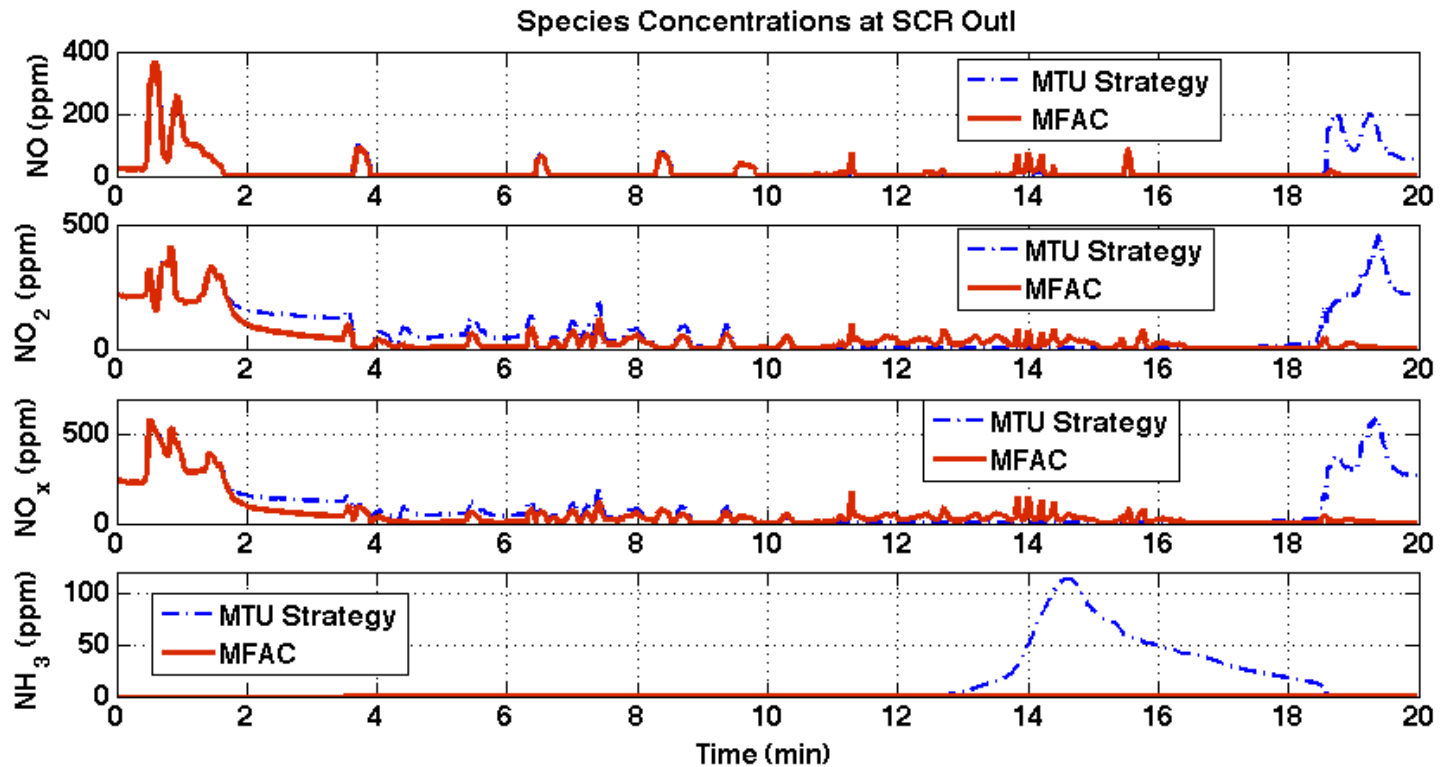
$i = NH_3, NO, NO_2, N_2O$  &  
 $j = Ads, Des, std, Fst, slo, oxi$

## NH<sub>3</sub> Storage Equations For Site 1 and 2

$$\Omega_1 \frac{d\theta_1}{dt} = R_{Ads,1} - R_{Des,1} - 4R_{Oxi} - 4R_{std} - 4R_{Fst} - 4R_{slo}$$

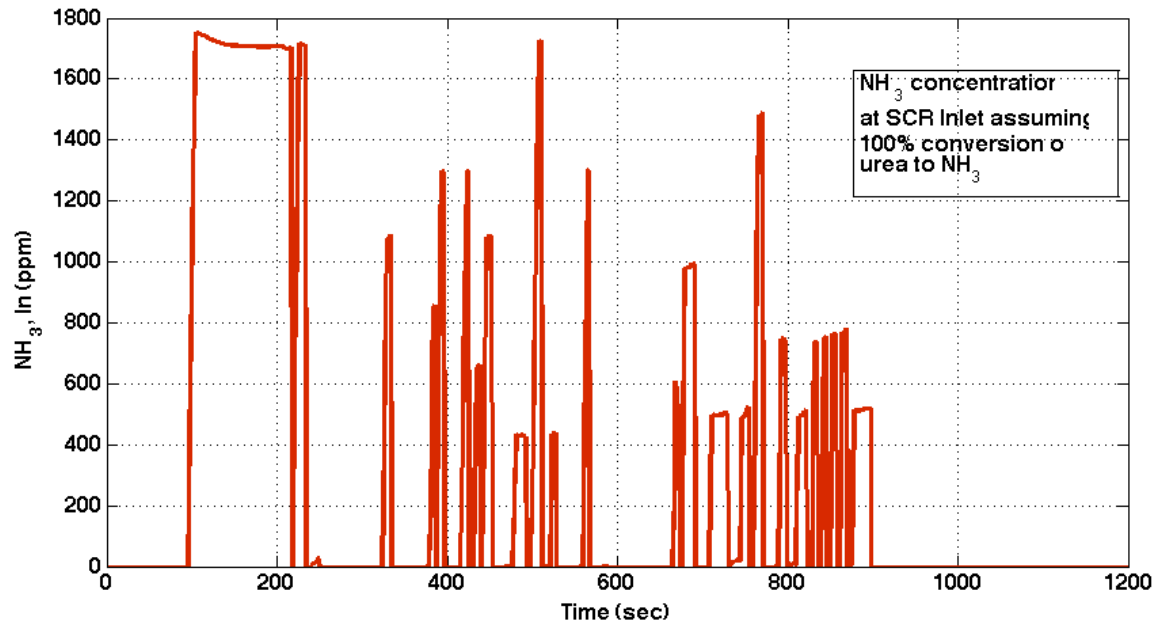
$$\Omega_2 \frac{d\theta_2}{dt} = R_{Ads,2} - R_{Des,2}$$

# MFAC strategy results in greater $\text{NO}_x$ reduction while eliminating $\text{NH}_3$ slip



- Benefits in overall  $\text{NO}_x$  reduction and  $\text{NH}_3$  slip (completely eliminated in the catalyst)

# MFAC strategy also results in lesser cumulative urea usage



- Cumulative urea injection is 4% lesser than the existing strategy
- Cumulative SCR out  $\text{NO}_x$  is reduced by 30% using this strategy.
- Further efforts to improve the control performance (urea injection rate) are underway.



# Summary and Future Work

- Optimal controls literature was reviewed and data driven control strategies were chosen for optimal NH<sub>3</sub> storage task
- ILC Strategy
  - H-W models for NO<sub>x</sub> and NH<sub>3</sub> emissions were validated using FTP data
- MFAC Strategy
  - Benefits in overall NO<sub>x</sub> control and urea consumption
  - NH<sub>3</sub> slip was completely eliminated

## Future Work

- Further validation of H-W models and integrating with ILC strategy
- Comparison of ILC and MFAC strategies in NO<sub>x</sub> and NH<sub>3</sub> control and urea usage.

# Acknowledgements

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- ▶ John Johnson, Jeff Naber (Michigan Tech University)



# Modeling Aging Effects on Reaction Pathways in Cu-CHA Urea SCR Catalysts

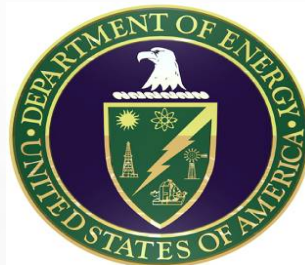
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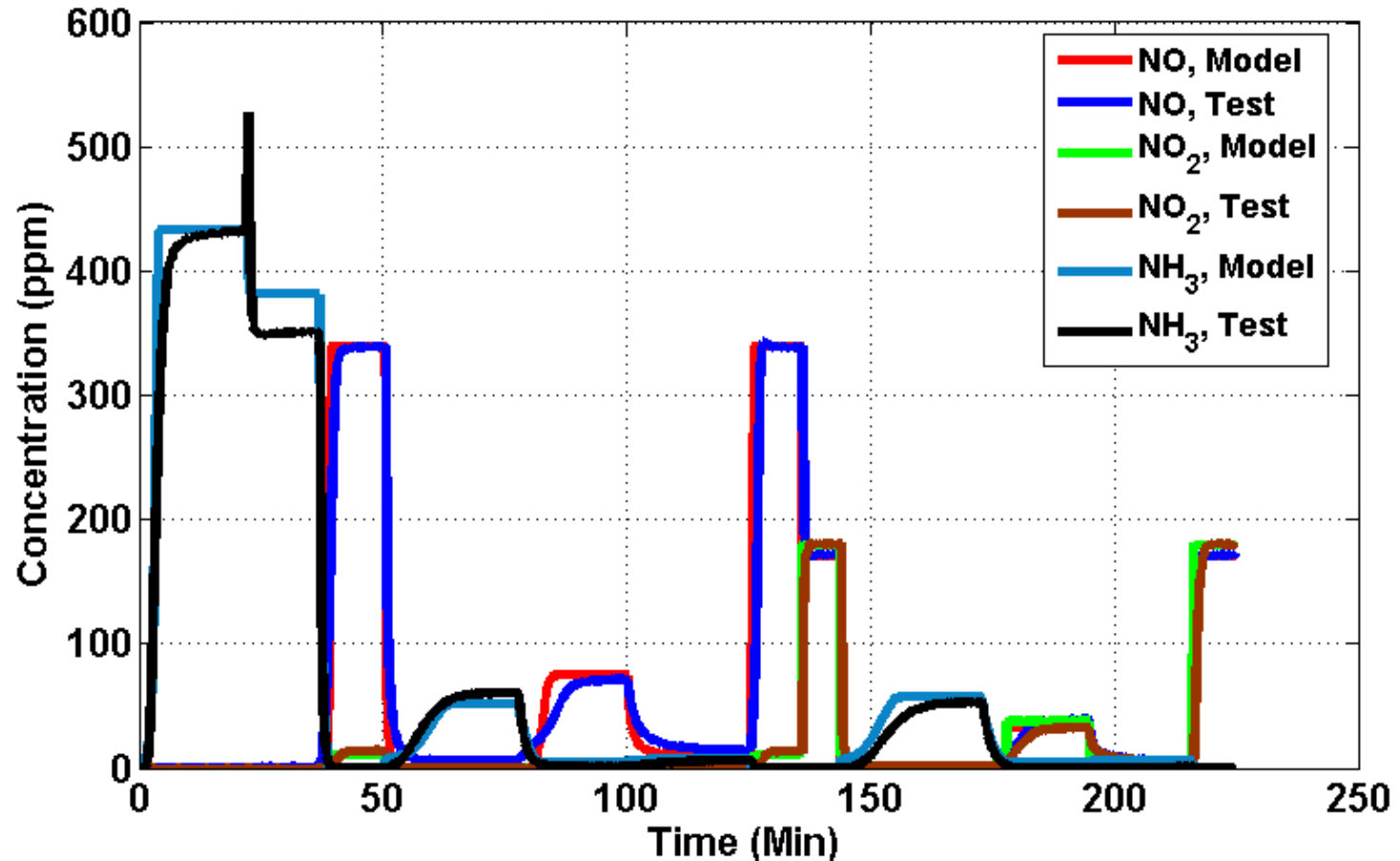
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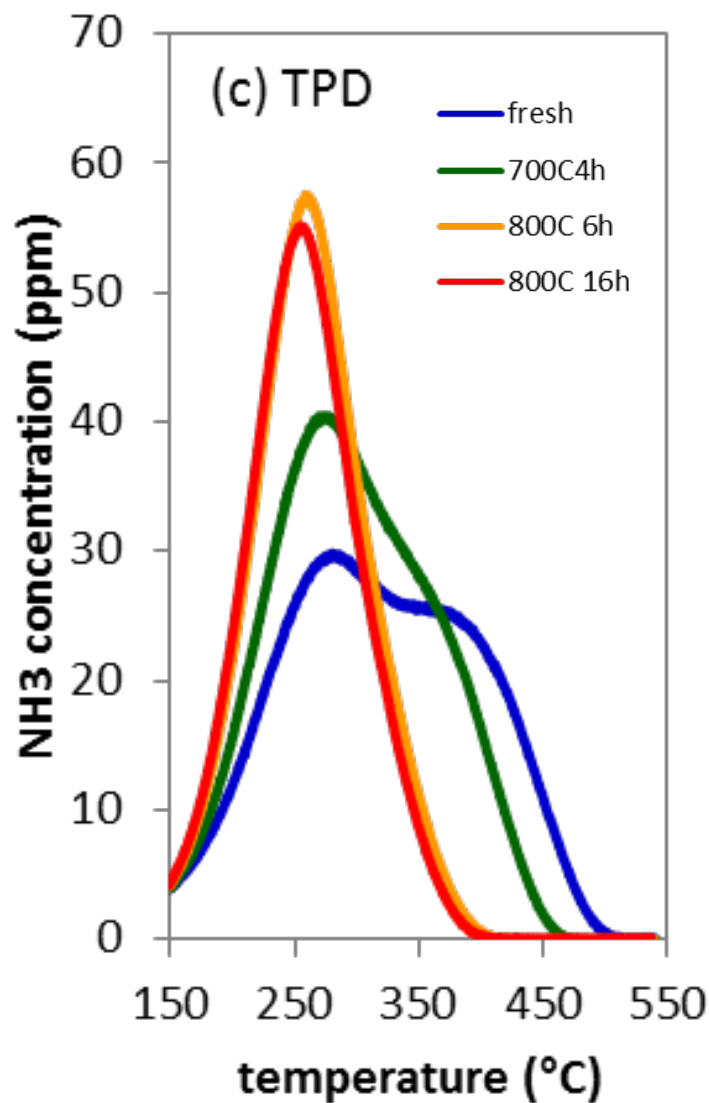
- Overall goal is to develop catalyst aging factors, essential for model based control adaptation, using 1D SCR models.
- Transient protocol and TPD data collected on Cu-CHA samples at ORNL were used to develop the SCR model.

# SCR model considering a single $\text{NH}_3$ storage site was developed and validated



- SCR Model validation shown at 90k SV at  $T = 300^{\circ}\text{C}$
- Model was successfully validated for various cases:  $0.8 \leq \text{NH}_3/\text{NO}_x \leq 1.2$  and  $30\text{k} \leq \text{SV} \leq 90\text{k}$

# Recent TPD data on a fresh Cu-CHA sample showed more than one storage site



- Recent data on a fresh catalyst sample ( $\text{NH}_3$  desorption vs temperature during TPD shown on the left) shows two peaks indicating the possibility of more than one active site with different stabilities in the catalyst.
- The two peaks convolute into one as the sample is degreened and aged as shown in the figure.
- This has motivated us to develop a model with two  $\text{NH}_3$  storage sites so that the aging effect on  $\text{NH}_3$  storage and other reaction pathways can be accurately predicted.

## Site 1 (Weakly Adsorbed)

$$r_{ads,s1} = A_{ads,s1} c_{g,NH_3} (1 - \theta_{NH_3,s1})$$
$$r_{des,s1} = A_{des,s1} e^{\frac{-E_{des,s1}(1-\gamma\theta_{NH_3,s1})}{RT}} \theta_{NH_3,s1}$$

## Site 2 (Strongly Adsorbed)

$$r_{ads,s2} = A_{ads,s2} c_{g,NH_3} (1 - \theta_{NH_3,s2})$$
$$r_{des,s2} = A_{des,s2} e^{\frac{-E_{des,s2}}{RT}} \theta_{NH_3,s2}$$

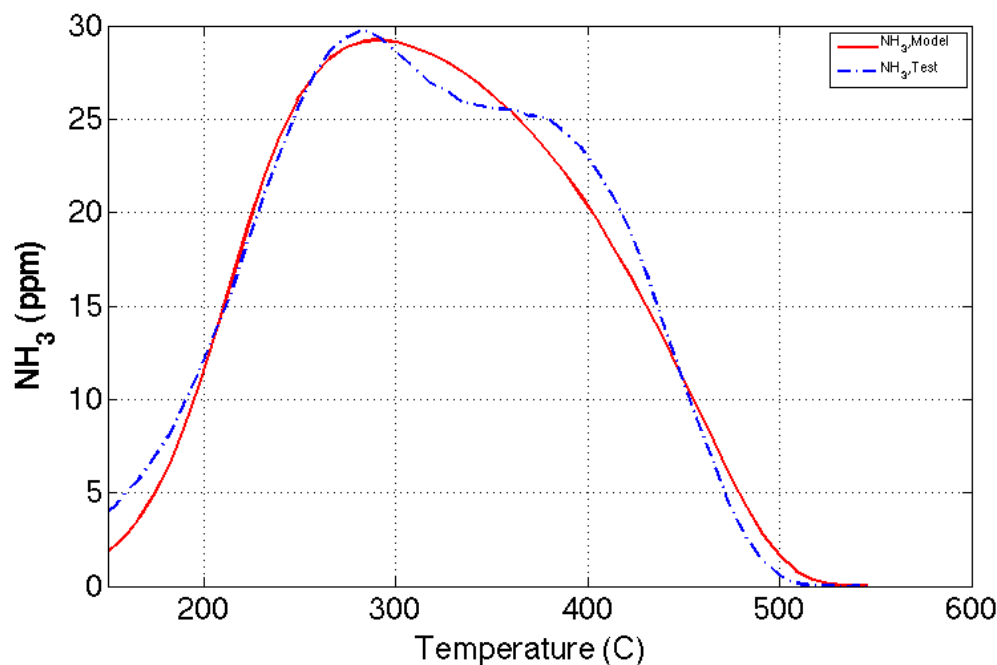
$$\frac{\partial c_{g,NH_3}}{\partial t} = -\frac{u}{\varepsilon} \frac{\partial c_{g,NH_3}}{\partial x} + \frac{\Omega_1}{\varepsilon} (r_{des,s1} - r_{ads,s1}) + \frac{\Omega_2}{\varepsilon} (r_{des,s2} - r_{ads,s2})$$

$$\frac{d\theta_{NH_3,s1}}{dt} = r_{ads,s1} - r_{des,s1}$$

$$\frac{d\theta_{NH_3,s2}}{dt} = r_{ads,s2} - r_{des,s2}$$

Rate equations are taken from  
Colombo et al.'s recent  
modeling work on Fe-Z catalyst

# Current dual site $\text{NH}_3$ storage model does not match the desorption peaks



- Number of storage sites is critical to predict aging effect on each of the reaction pathways in the SCR catalyst and to identify if 'a' site participates.
- Should more  $\text{NH}_3$  storage sites be considered to predict this effect, as reported by Skarlis et al. (Journal of Physical Chemistry C, 2012)?
- How to estimate the activation energies of each of the sites?
- Will the multi-site model be suitable for controls adaptation during aging?