

# Development of Cu SCR Model using CLEERS Transient SCR Reactor Protocol

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# Motivation

- NH<sub>3</sub>/Urea Selective Catalytic Reduction (SCR) proven effective over wide range of conditions, but improvement necessary for:
  - increasingly stringent emission standards
  - higher engine-out NO<sub>x</sub> under high efficiency operating points
    - driven by fuel economy regulations
  - cooler exhaust temperatures from advanced combustion regimes
  - hotter exhaust temperatures from lean gasoline engines
- Model-based SCR system controls not sufficiently developed for adapting to catalyst aging/de-activation
  - better understanding of catalyst aging required

# Objectives

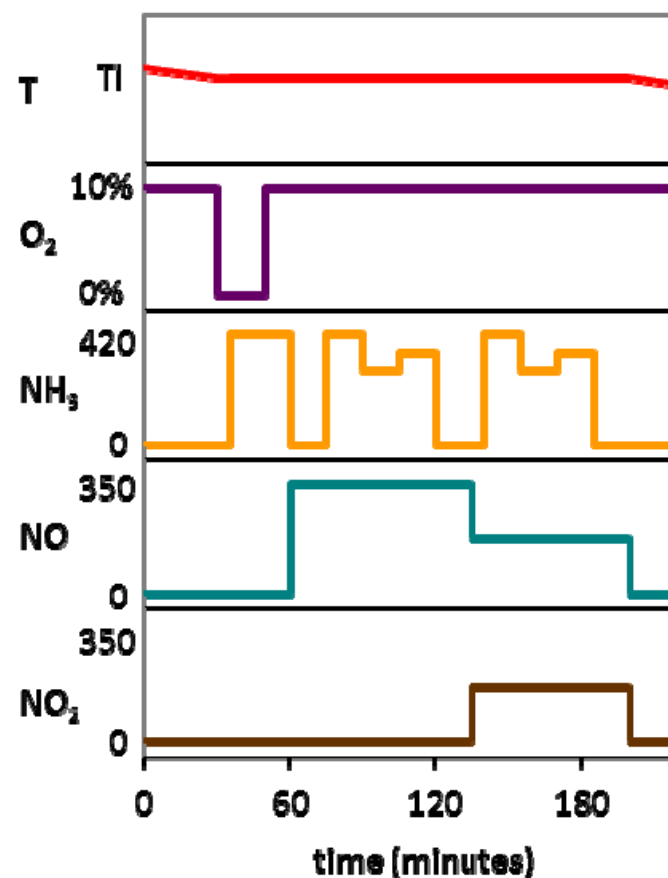
- Characterize a commercially available 2010 Cu zeolite SCR catalyst through CLEERS transient reactor protocol.
- Develop a baseline SCR model and validate it against the transient reactor data for future catalyst aging studies.

# Outline

- CLEERS Transient Reactor Protocol
- Data Analysis
- Cu-SCR Model
- Model Validation
- Conclusions & Future Work

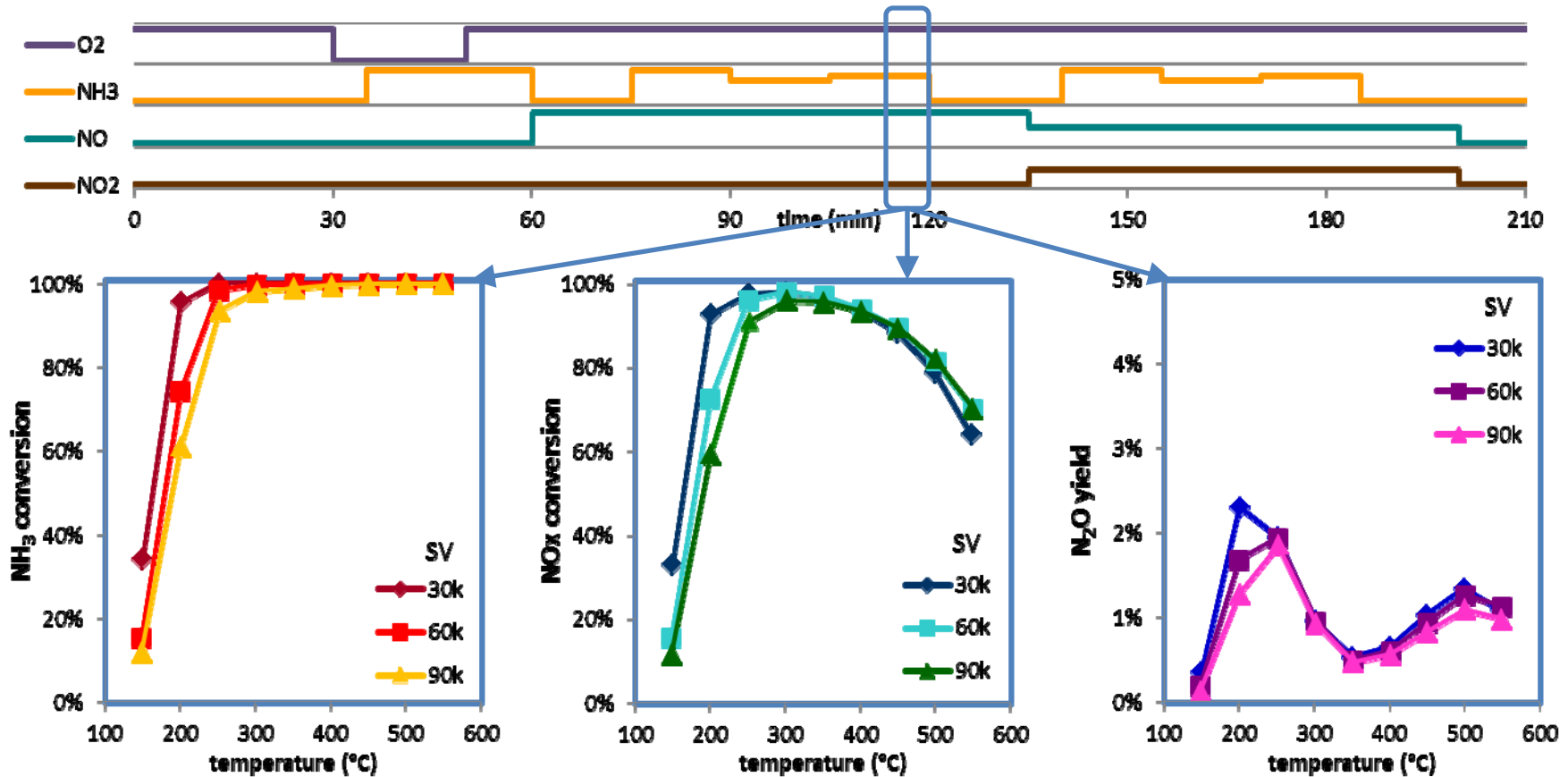
# Revised transient CLEERS SCR protocol; assessed with commercial Cu zeolite

- Protocol designed to generate data needed for model calibration and performance evaluation
  - steady state points
    - SCR conditions:
      - $\text{NH}_3/\text{NO}_x = 0.8, 1.0, 1.2$
      - $\text{NO}_2/\text{NO}_x = 0.0, 0.5$
    - $\text{O}_2$  oxidation of  $\text{NH}_3$  &  $\text{NO}$
  - arranged to measure  $\text{NH}_3$  storage capacities between points
  - goal: minimal operating time and expense
- Experiments conducted on Cu zeolite core sample cut from Ford F-series super duty SCR monolith
  - 150-550°C @ 50°C
  - 30k, 60k, 90k  $\text{hr}^{-1}$  (60k shown if not indicated)
  - 350 ppm  $\text{NO}_x$
- Data will serve as baseline for investigations of hydrothermal aging and HC fouling



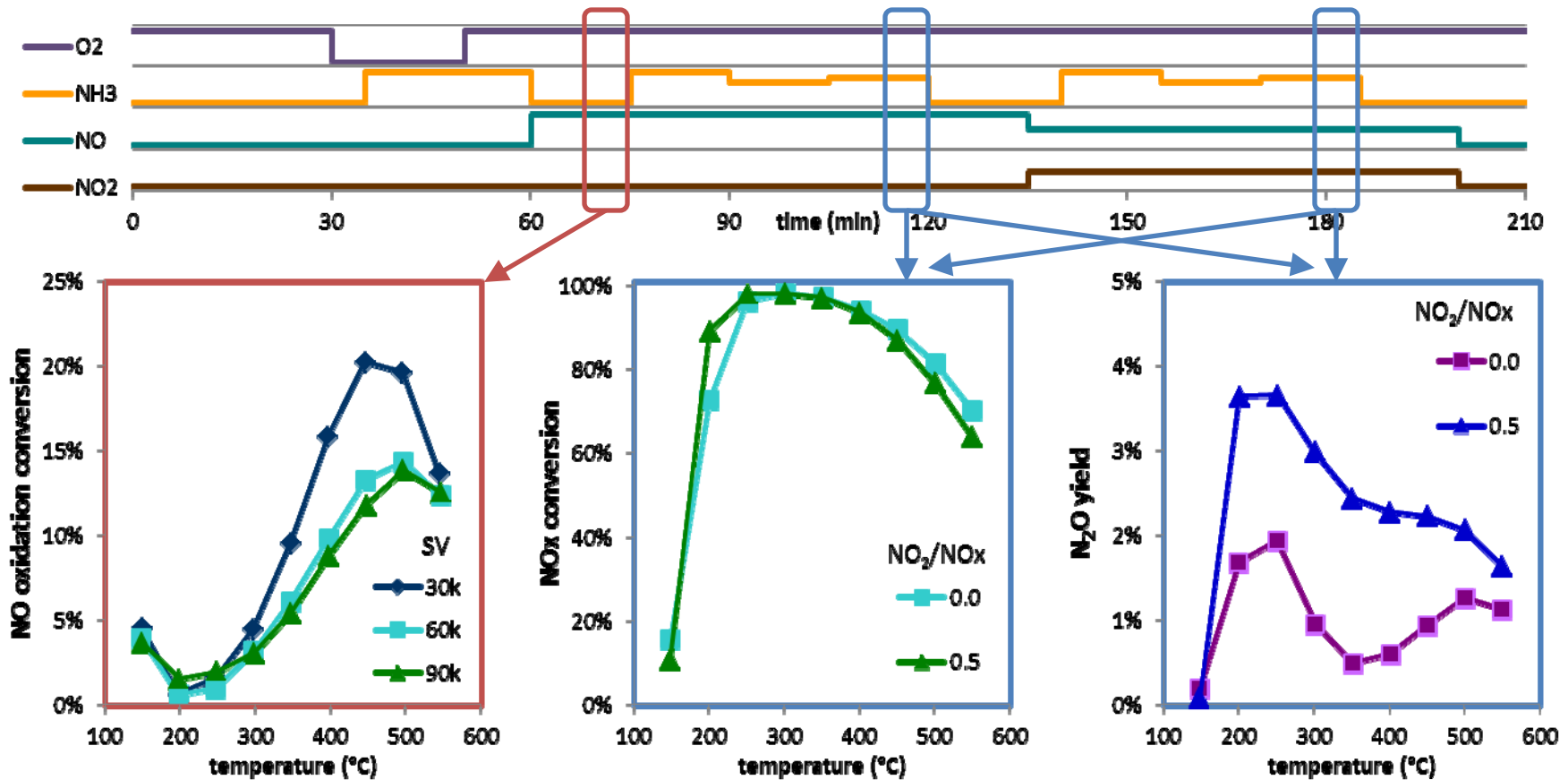
note: 5%  $\text{H}_2\text{O}$  & 5%  $\text{CO}_2$  in all steps

# Steady state points illustrate wide operating window of fresh Cu zeolite SCR catalyst



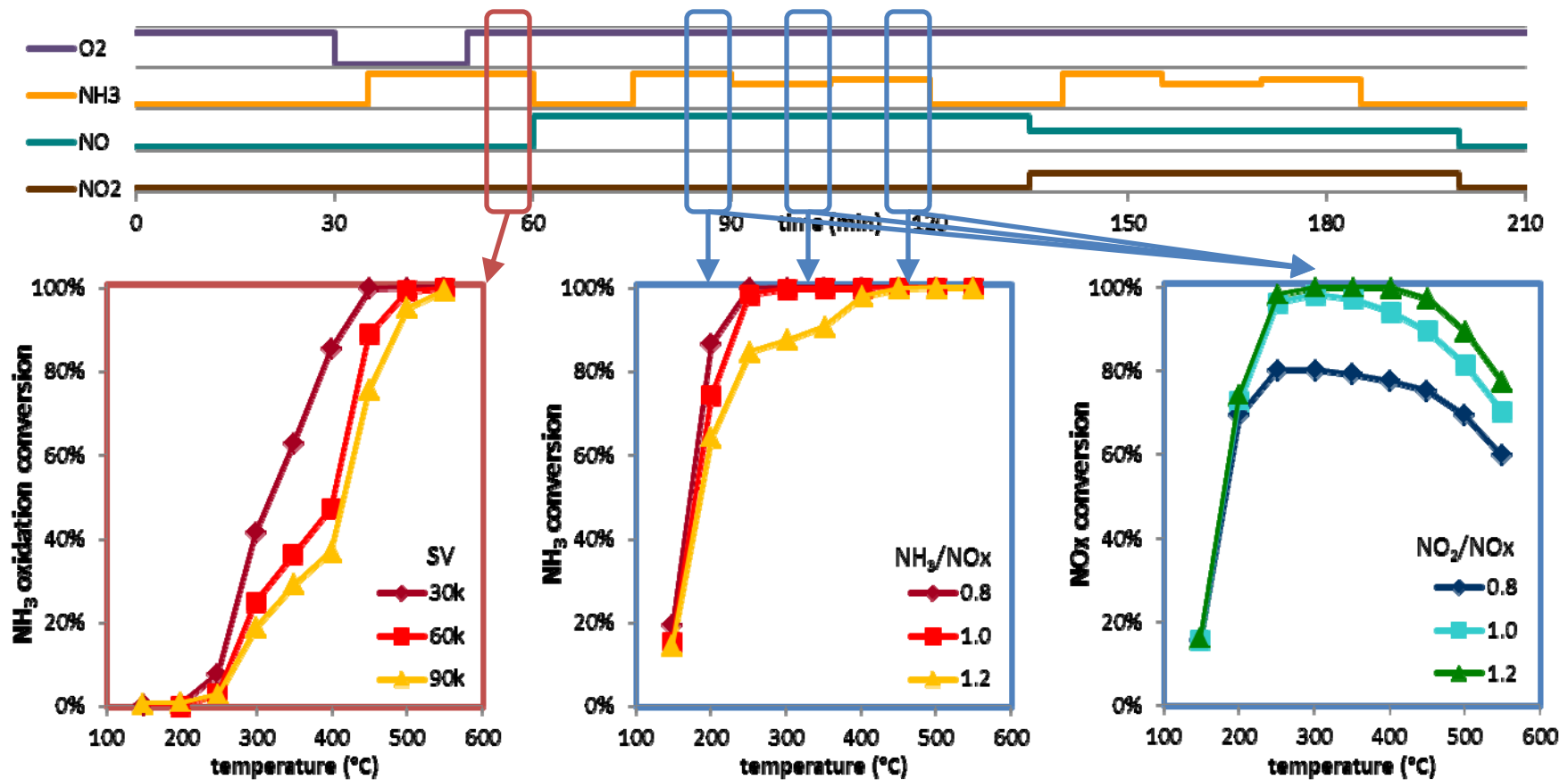
- Fresh commercial Cu SCR shows:
  - minimal NH<sub>3</sub> slip
  - good NO<sub>x</sub> conversion for 250 °C ≤ T ≤ 450 °C, but drop off at high T
  - high selectivity to N<sub>2</sub>

# Catalyst has relatively low sensitivity to NO<sub>2</sub>/NO<sub>x</sub>



- Inclusion of NO<sub>2</sub> increases NO<sub>x</sub> conversion near light-off
- NO<sub>2</sub> increases N<sub>2</sub>O formation, but high N<sub>2</sub> selectivity maintained
- High NO oxidation could reduce need for NO<sub>2</sub> in feed

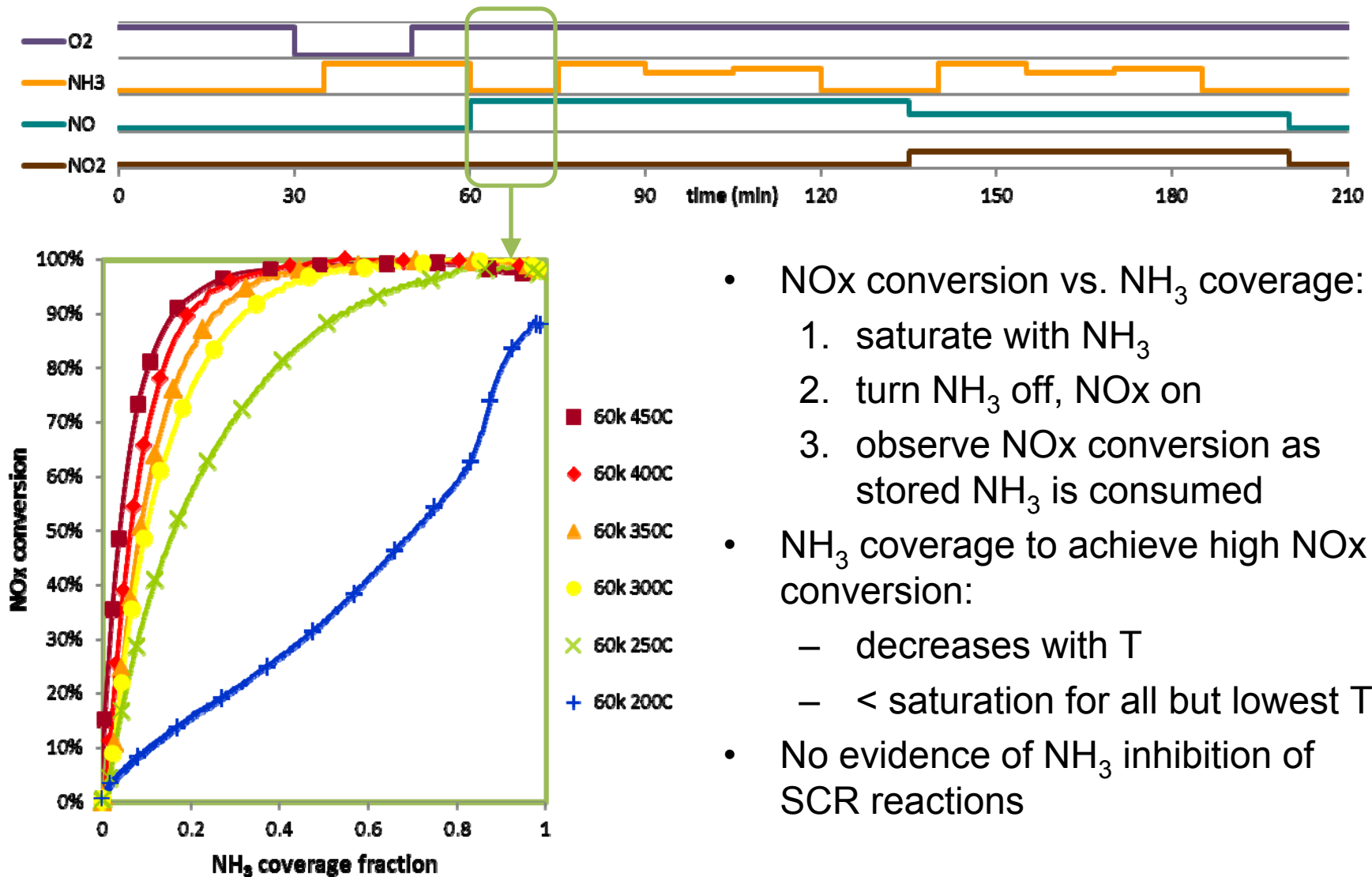
# High T NOx conversion limited by NH<sub>3</sub> oxidation



- All NH<sub>3</sub> consumed at high T
- NO<sub>x</sub> conversion improves with increasing NH<sub>3</sub> dose
- High NH<sub>3</sub> oxidation activity: competes with SCR at high T

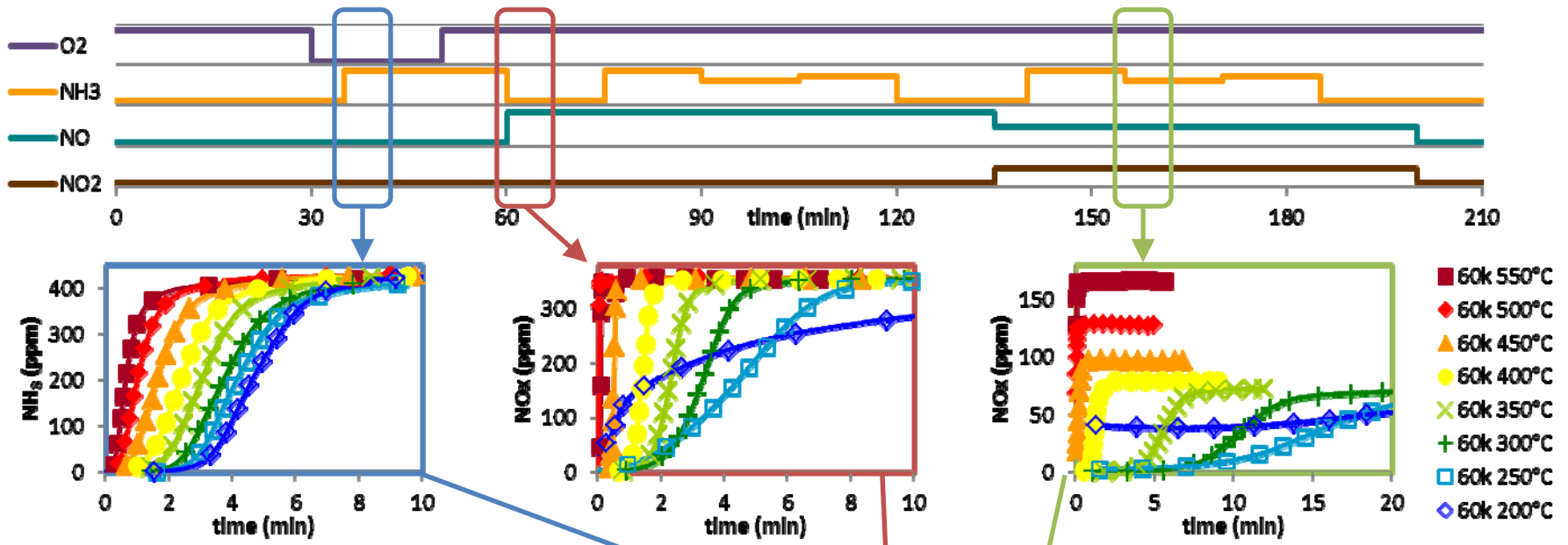


# Transients reveal critical NH<sub>3</sub> coverage

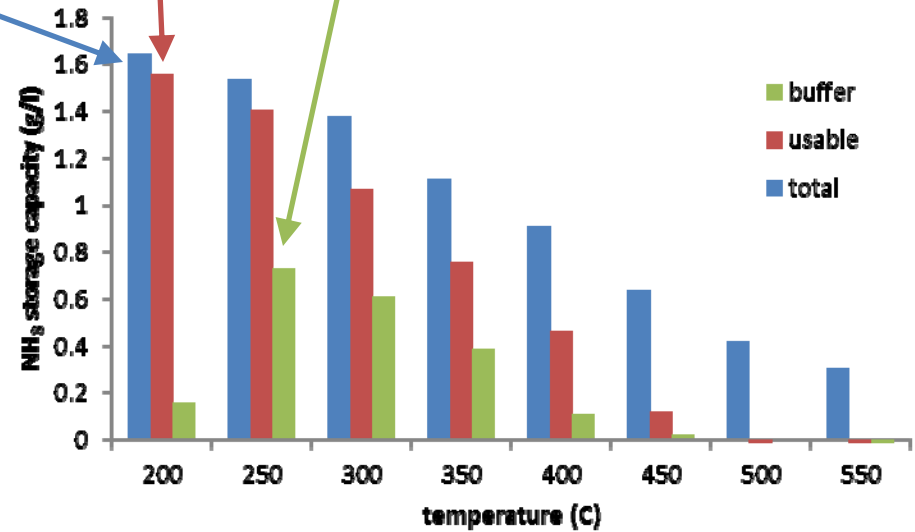


- NO<sub>x</sub> conversion vs. NH<sub>3</sub> coverage:
  1. saturate with NH<sub>3</sub>
  2. turn NH<sub>3</sub> off, NO<sub>x</sub> on
  3. observe NO<sub>x</sub> conversion as stored NH<sub>3</sub> is consumed
- NH<sub>3</sub> coverage to achieve high NO<sub>x</sub> conversion:
  - decreases with T
  - < saturation for all but lowest T
- No evidence of NH<sub>3</sub> inhibition of SCR reactions

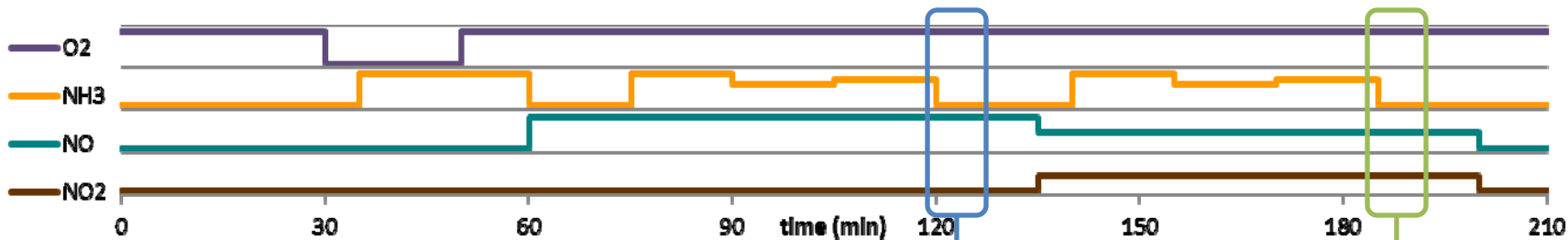
# Transients quantify details of NH<sub>3</sub> storage capacity



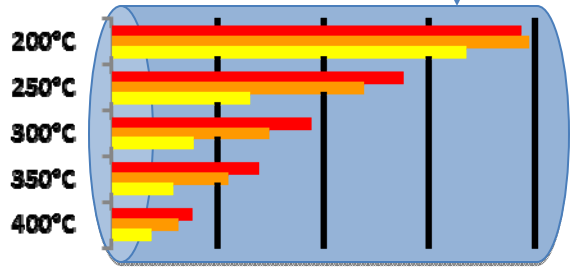
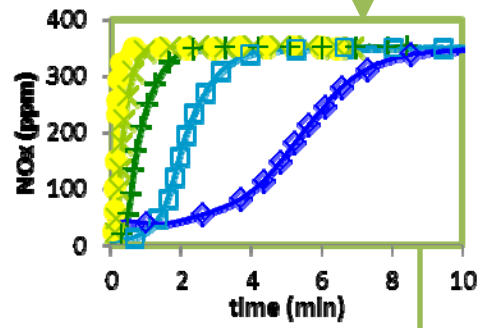
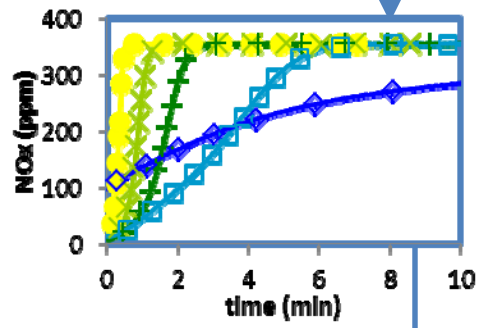
- Example capacities:
  - Total: NH<sub>3</sub> uptake without O<sub>2</sub>
  - Usable: NH<sub>3</sub> stored under O<sub>2</sub>
  - Buffer: capacity for temporary NH<sub>3</sub> overdose/underdose
- Available NH<sub>3</sub> storage capacity changes with current conditions & operating history



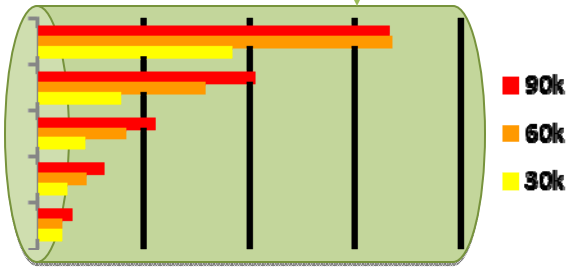
# SCR surface NH<sub>3</sub> inventory shows catalyst utilization



- Estimation of fractional catalyst utilization:
  1. Turn NH<sub>3</sub> off at end of SCR steps
  2. Integrate NO<sub>x</sub> reduced by stored NH<sub>3</sub>
  3. Divide by Usable NH<sub>3</sub> capacity at same T
- Utilization decreases with
  - higher T
  - lower SV
  - NO<sub>2</sub> in feed



NH<sub>3</sub> coverage  
(catalyst utilization)  
NO<sub>2</sub>/NO<sub>x</sub> = 0.0  
NH<sub>3</sub>/NO<sub>x</sub> = 1.0  
'standard' SCR



NH<sub>3</sub> coverage  
(catalyst utilization)  
NO<sub>2</sub>/NO<sub>x</sub> = 0.5  
NH<sub>3</sub>/NO<sub>x</sub> = 1.0  
'fast' SCR

# Single Site NH<sub>3</sub> Storage Model

- All SCR models developed in Matlab/Simulink
- First order Euler integration in space – 100 elements (cells) along the axis
- Simulated using a variable step solver (ode 23tb) in Simulink
- Nonlinear constrained minimization (fmincon) used to identify rate parameters using Matlab's Optimization toolbox

$$\frac{\partial c_{g,NH_3}}{\partial t} = -\frac{u}{\varepsilon} \frac{\partial c_{g,NH_3}}{\partial x} + \frac{\Omega}{\varepsilon} (r_{des} - r_{ads})$$

$$\frac{d\theta_{NH_3}}{dt} = r_{ads} - r_{des}$$

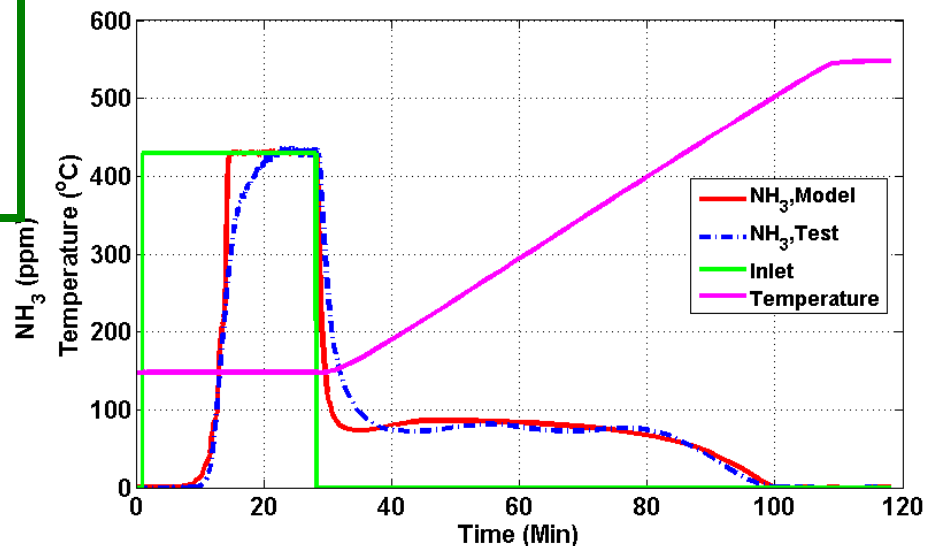
## Adsorption and Desorption Rates

$$r_{ads} = A_{ads} c_{g,NH_3} (1 - \theta_{NH_3})$$

$$r_{des} = A_{des} e^{\frac{-E_{des}(1-\gamma\theta_{NH_3})}{RT}} \theta_{NH_3}$$

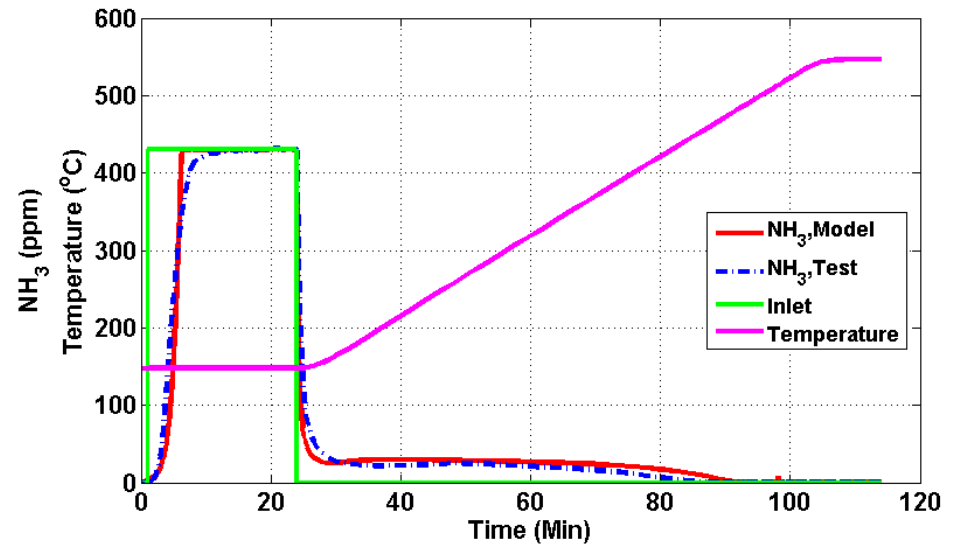
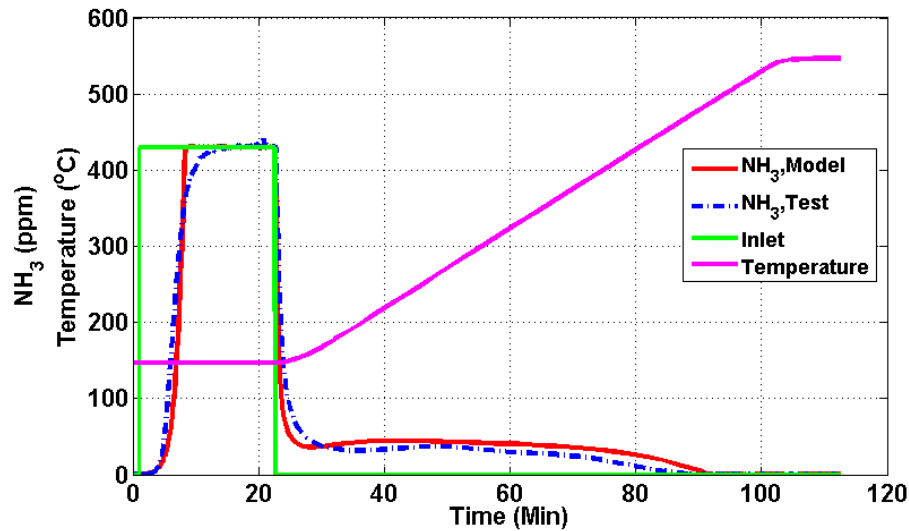
Rate parameters identified on TPD data at 30000/hr SV

430 ppm of NH<sub>3</sub>, 5% H<sub>2</sub>O, 5% CO<sub>2</sub> at T = 150°C



L. Olsson's single site rate parameters on Cu-ZSM-5 (ACatB, 2008) considered as initial conditions

# Single Site Storage Model Validation on TPD Tests

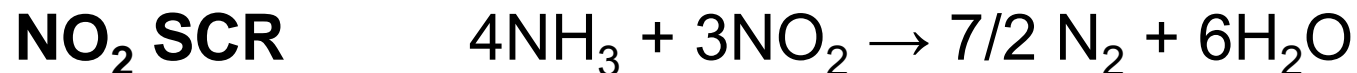
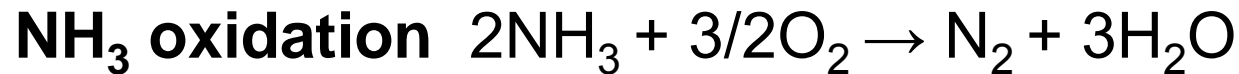


$A_{ads}$	$m^3/mol/s$	0.99
$A_{des}$	$1/s$	1.01E11
$E_{des}$	$kJ/mol$	180.2
$\gamma$	-	0.81
$\Omega$	$mol/m^3$	225

Validation at 60000/hr and 90000/hr SV data

# NO<sub>x</sub> Reaction Pathways

In addition to NH<sub>3</sub> adsorption and desorption on SCR catalyst surface, the following reactions have been incorporated in this version of Cu-Z SCR model

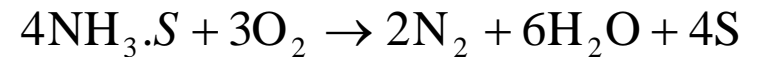


# NH<sub>3</sub> Oxidation Model

$$\frac{\partial c_{g,NH_3}}{\partial t} = -\frac{u}{\varepsilon} \frac{\partial c_{g,NH_3}}{\partial x} + \frac{\Omega}{\varepsilon} (r_{des} - r_{ads})$$

$$\frac{d\theta_{NH_3}}{dt} = r_{ads} - r_{des} - r_{NH_3,oxi}$$

$$\frac{\partial c_{g,O_2}}{\partial t} = -\frac{u}{\varepsilon} \frac{\partial c_{g,O_2}}{\partial x} - \frac{\Omega}{\varepsilon} \left( \frac{3}{4} r_{NH_3,oxi} \right)$$



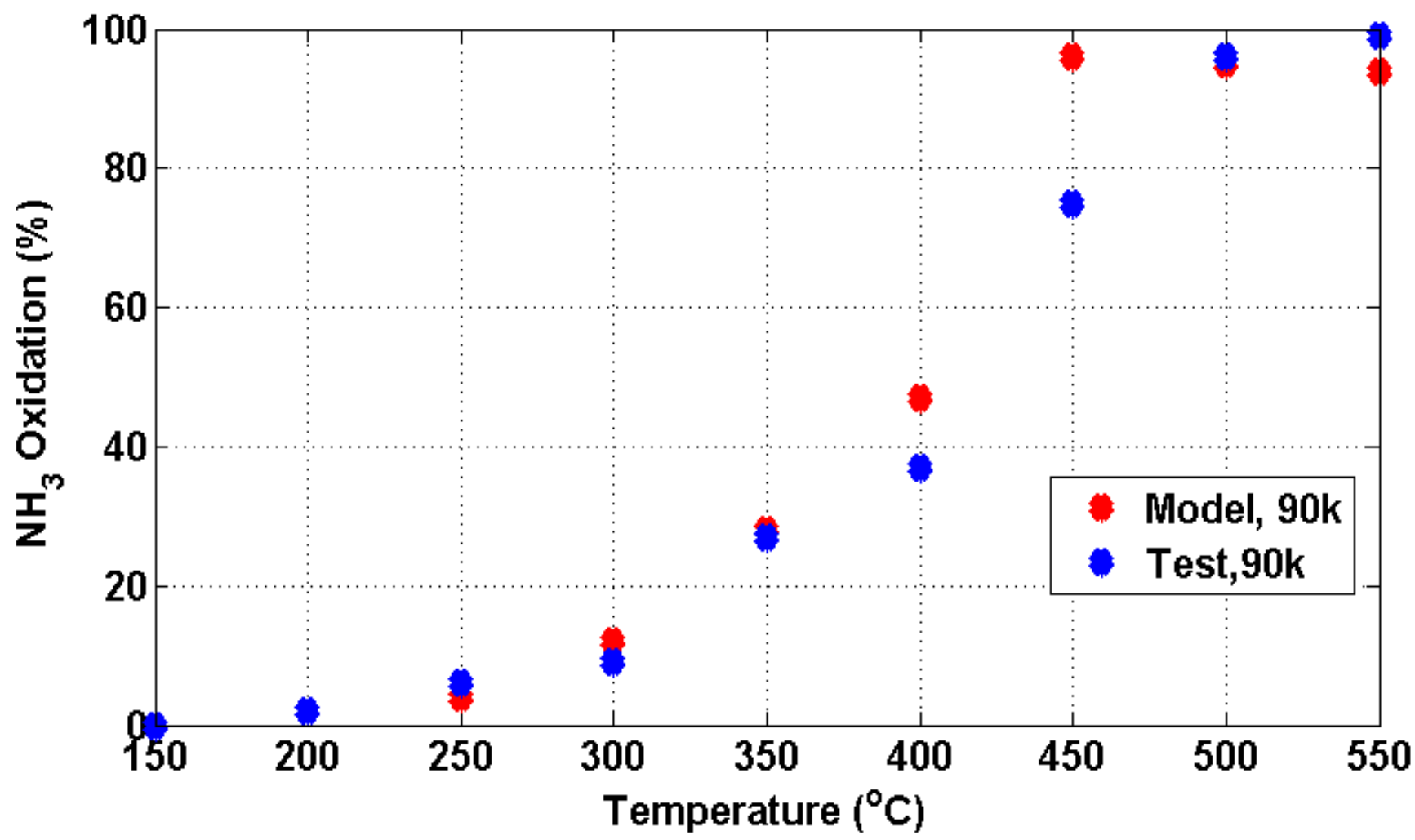
$$r_{NH_3,oxi} = k_{NH_3,oxi} c_{g,O_2} \theta_{NH_3}$$

$$A = 2.22E3 \text{ m}^3/\text{mol}/\text{s}$$

$$E = 74 \text{ kJ/mol}$$

- Parameters identified at 60k/hr data using unconstrained nonlinear minimization function in Matlab (*fminsearch*).
- Cost function to be minimized is defined as the average sum of absolute error between the test and simulated NH<sub>3</sub> concentrations.

$$J = \frac{\sum_{i=1}^N |c_{NH_3,s} - c_{NH_3,t}|}{N}$$





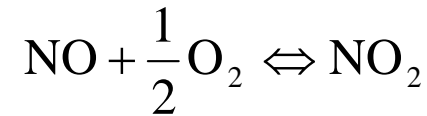
# NO Oxidation Model

$$\frac{\partial c_{g,NO}}{\partial t} = -\frac{u}{\varepsilon} \frac{\partial c_{g,NO}}{\partial x} - \frac{1}{\varepsilon} (r_{NO,oxi})$$

$$\frac{\partial c_{g,NO_2}}{\partial t} = -\frac{u}{\varepsilon} \frac{\partial c_{g,NO_2}}{\partial x} + \frac{1}{\varepsilon} (r_{NO,oxi})$$

$$r_{NO,oxi} = k_{NO,oxi} \left( c_{g,NO} c_{g,O_2}^{\frac{1}{2}} - \frac{c_{g,NO_2}}{k_{eq}} \right)$$

$$k_{eq} = A_{eq} \sqrt{T} e^{\frac{E_{eq}}{RT}}$$



$$A = 9.4E3 \text{ m}^3/\text{mol/s}$$

$$E = 43 \text{ kJ/mol}$$

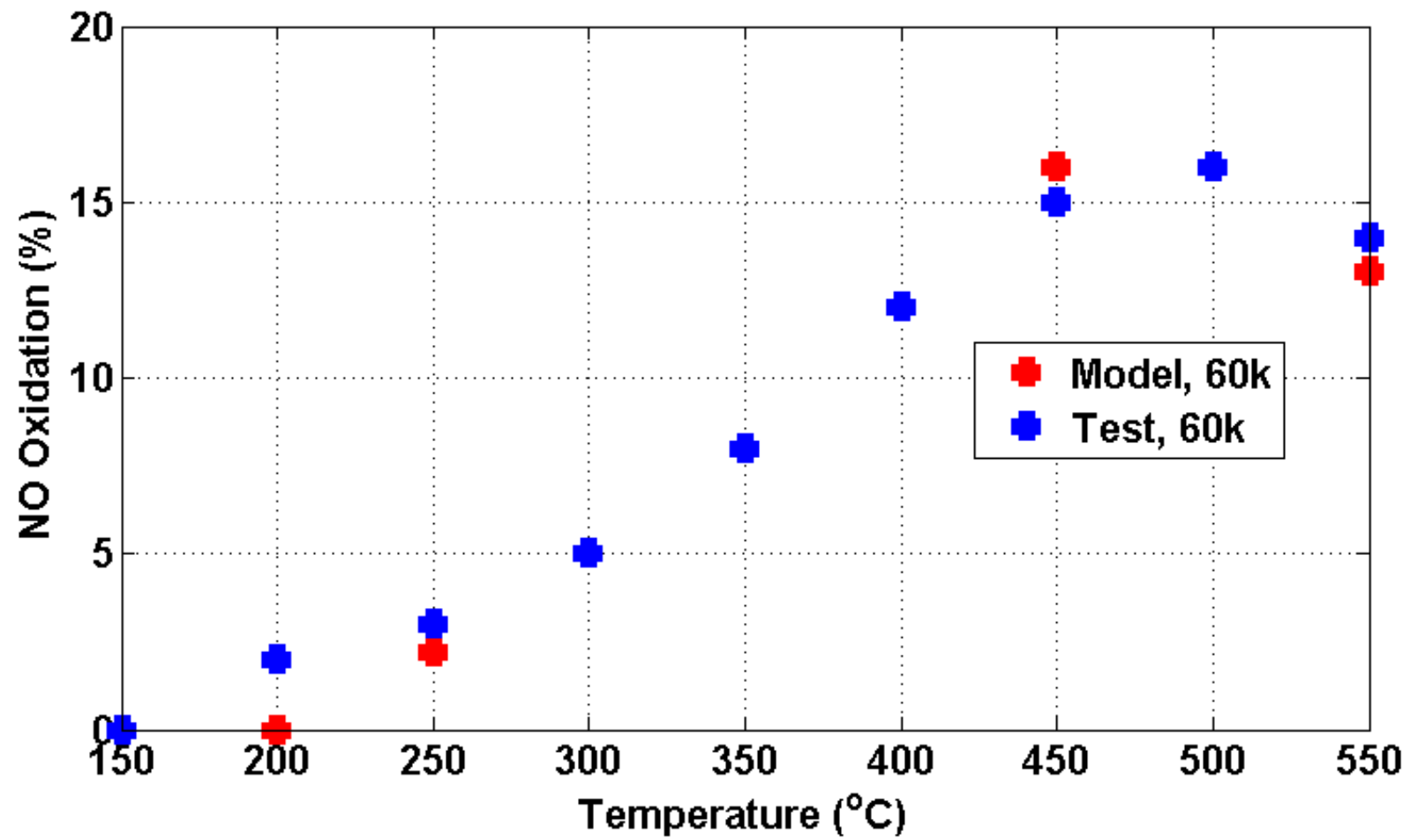
$$A_{eq} = 9.42E-7$$

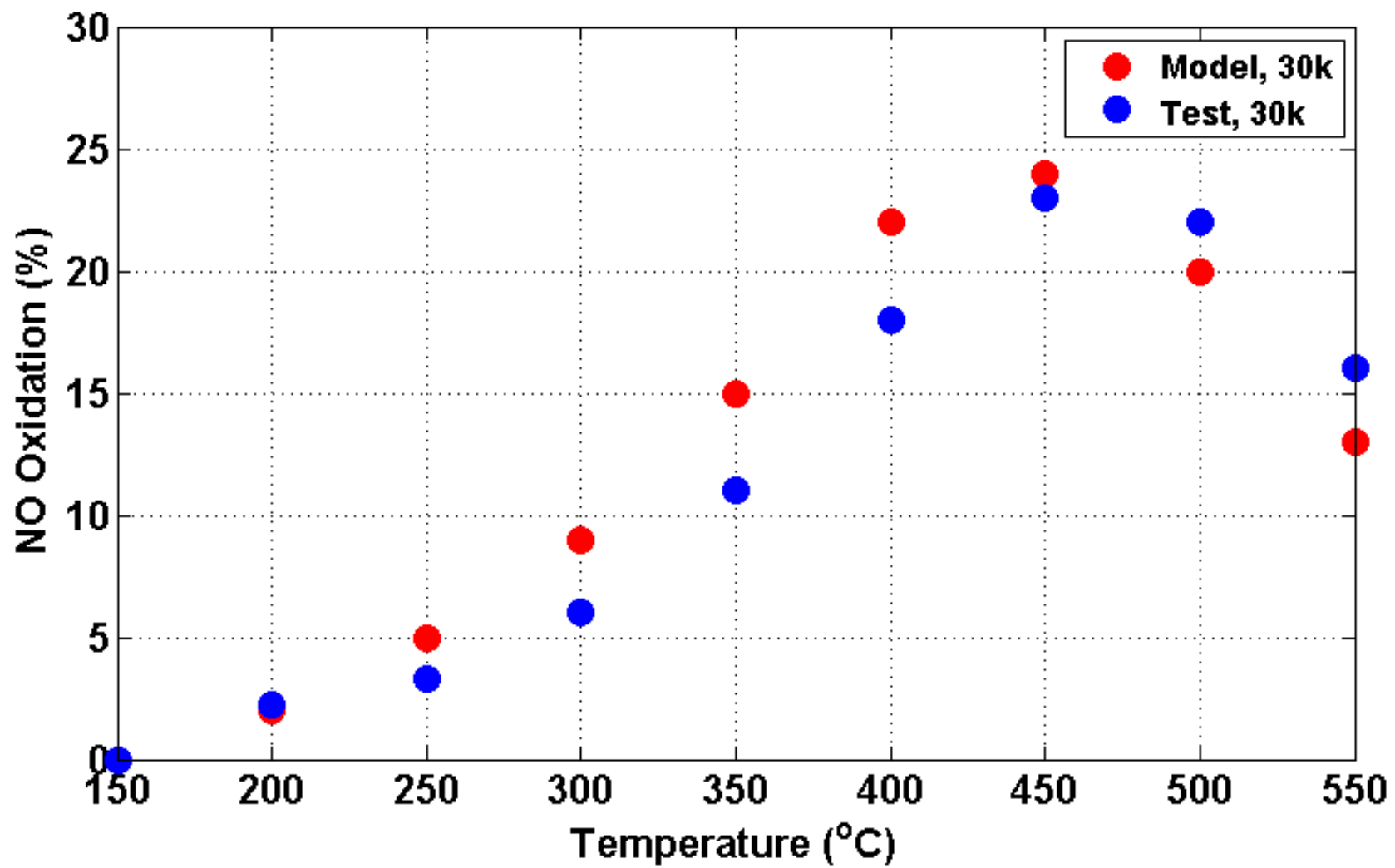
$$E_{eq} = 58 \text{ kJ/mol}$$

Ø Parameters identified using 4 data points at 60k/hr and 90k/hr using unconstrained nonlinear minimization function in Matlab (*fminsearch*).

Ø Cost function to be minimized is defined as the average sum of absolute error between the test and simulated NO and NO<sub>2</sub> concentrations.

$$J = \frac{\sum_{i=1}^N \left| (c_{NO,s} - c_{NO,t}) \right| + \left| (c_{NO_2,s} - c_{NO_2,t}) \right|}{N}$$





# Standard SCR Model

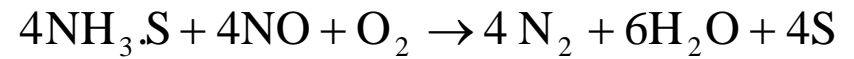
$$\frac{\partial c_{g,NO}}{\partial t} = -\frac{u}{\varepsilon} \frac{\partial c_{g,NO}}{\partial x} - \frac{1}{\varepsilon} (r_{NO,oxi} + \Omega r_{std-scr})$$

$$\frac{\partial c_{g,NO_2}}{\partial t} = -\frac{u}{\varepsilon} \frac{\partial c_{g,NO_2}}{\partial x} + \frac{1}{\varepsilon} (r_{NO,oxi})$$

$$\frac{\partial c_{g,NH_3}}{\partial t} = -\frac{u}{\varepsilon} \frac{\partial c_{g,NH_3}}{\partial x} + \frac{\Omega}{\varepsilon} (r_{des} - r_{ads})$$

$$\frac{d\theta_{NH_3}}{dt} = r_{ads} - r_{des} - r_{NH_3,oxi} - r_{std-scr}$$

$$\frac{\partial c_{g,O_2}}{\partial t} = -\frac{u}{\varepsilon} \frac{\partial c_{g,O_2}}{\partial x} - \frac{\Omega}{\varepsilon} \left( \frac{3}{4} r_{NH_3,oxi} + \frac{1}{4} r_{std-scr} \right)$$



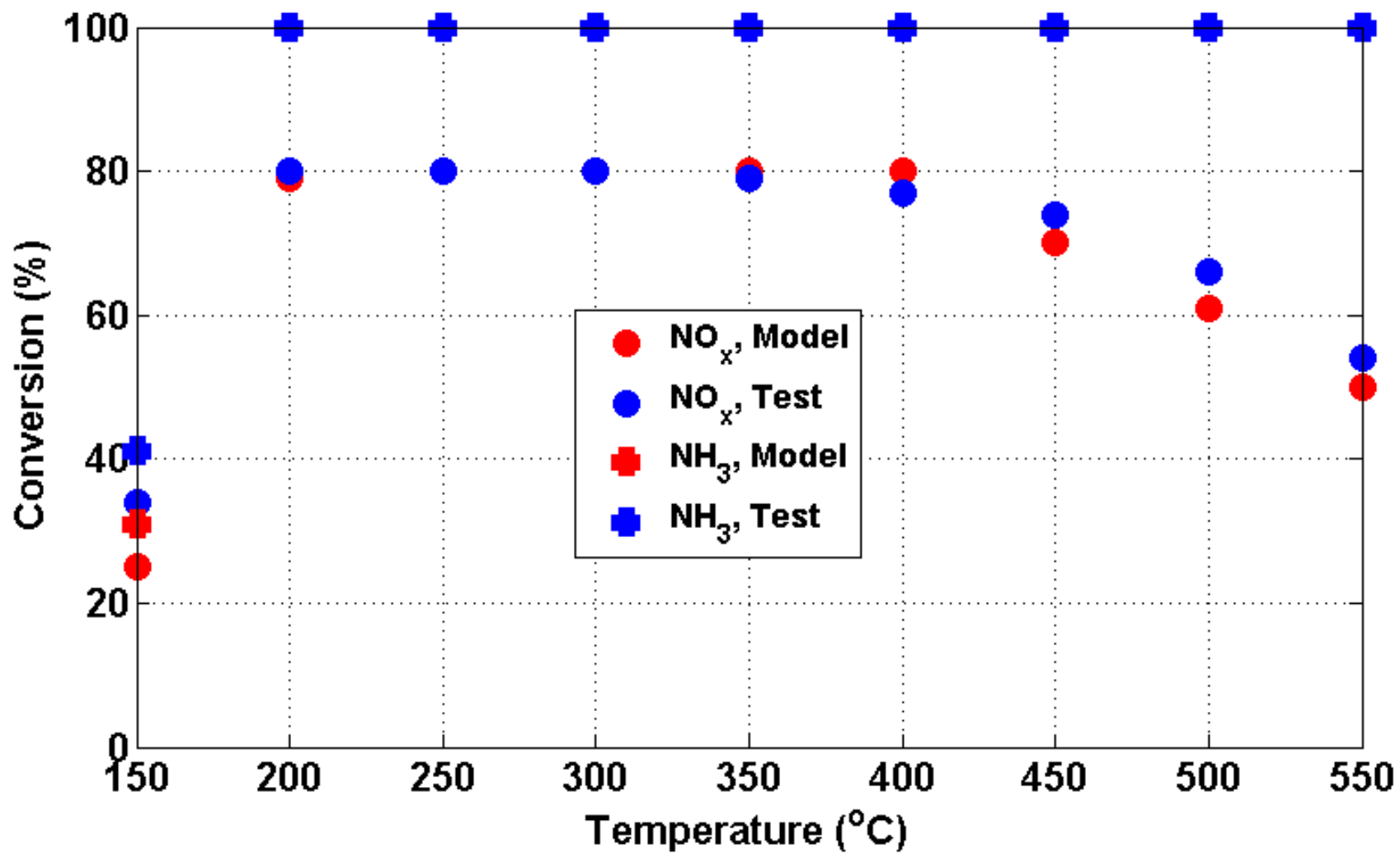
$$r_{std-scr} = A_{std-scr} e^{\frac{-E_{std-scr}}{RT}} c_{g,NO} \theta_{NH_3}$$

$$A_{std-scr} = 9.89E8 \text{ m}^3/\text{mol/s}$$

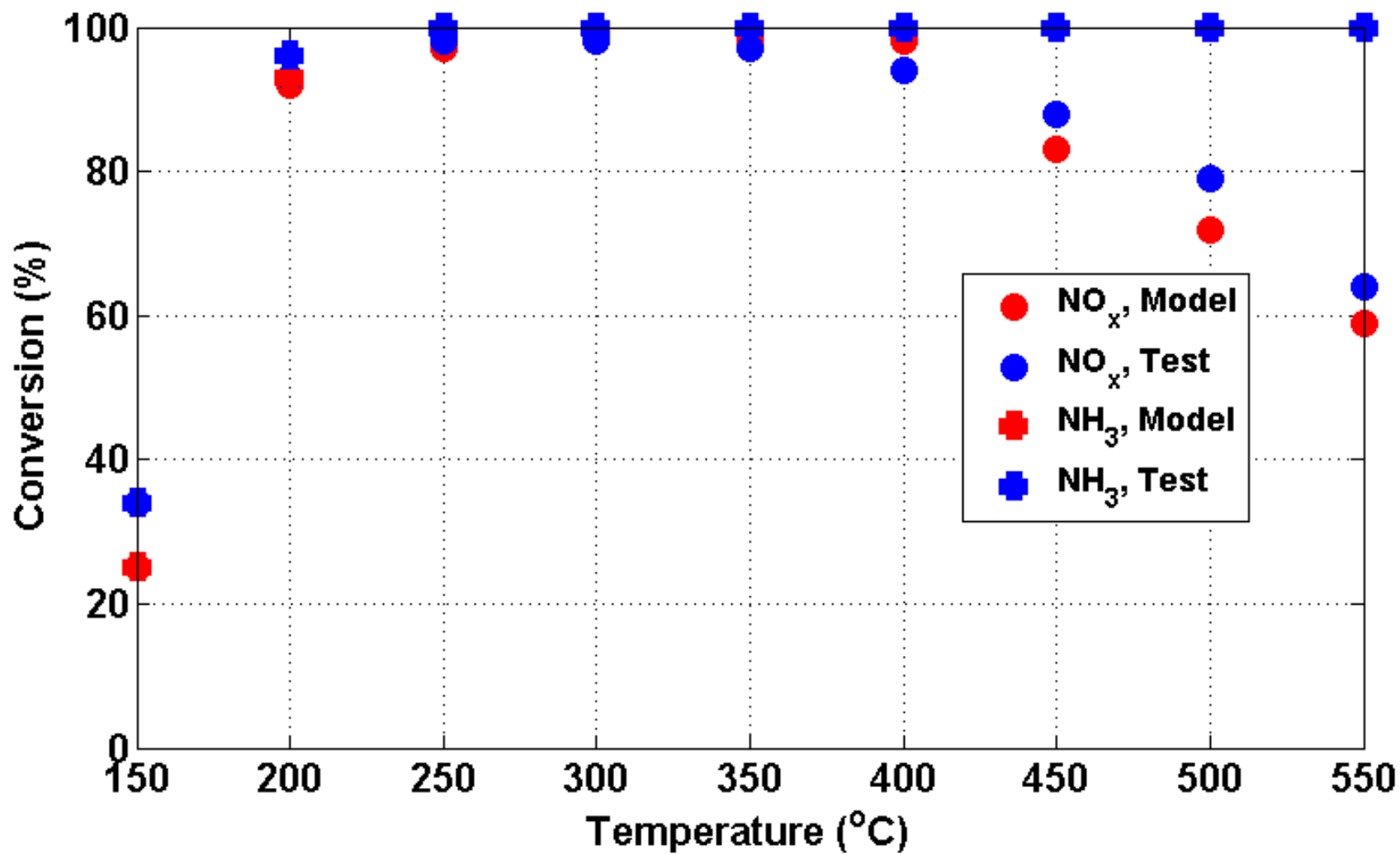
$$E_{std-scr} = 84.9 \text{ kJ/mol}$$

Ø Standard SCR pre-exponential was manually adjusted at 150°C, 30k/hr SV and the model was validated at the remaining data points.

Ø Model mismatch in NO<sub>x</sub> conversion at T > 450°C was observed at higher space velocities, possibly due to NH<sub>3</sub> oxidation to NO, which is not considered in the model.



**Alpha = 0.8**



**Alpha = 1.0**

# Fast SCR Model

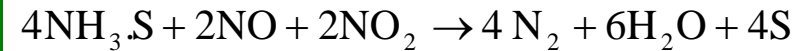
$$\frac{\partial c_{g,NO}}{\partial t} = -\frac{u}{\varepsilon} \frac{\partial c_{g,NO}}{\partial x} - \frac{1}{\varepsilon} (r_{NO,oxi} + \Omega(r_{std-scr} + 0.5r_{fast-scr}))$$

$$\frac{\partial c_{g,NO_2}}{\partial t} = -\frac{u}{\varepsilon} \frac{\partial c_{g,NO_2}}{\partial x} + \frac{1}{\varepsilon} (r_{NO,oxi} - \Omega(r_{NO_2-scr} + 0.5r_{fast-scr}))$$

$$\frac{\partial c_{g,NH_3}}{\partial t} = -\frac{u}{\varepsilon} \frac{\partial c_{g,NH_3}}{\partial x} + \frac{\Omega}{\varepsilon} (r_{des} - r_{ads})$$

$$\frac{d\theta_{NH_3}}{dt} = r_{ads} - r_{des} - r_{NH_3,oxi} - r_{std-scr} - r_{NO_2-scr} - r_{fast-scr}$$

$$\frac{\partial c_{g,O_2}}{\partial t} = -\frac{u}{\varepsilon} \frac{\partial c_{g,O_2}}{\partial x} - \frac{\Omega}{\varepsilon} \left( \frac{3}{4} r_{NH_3,oxi} + \frac{1}{4} r_{std-scr} \right)$$

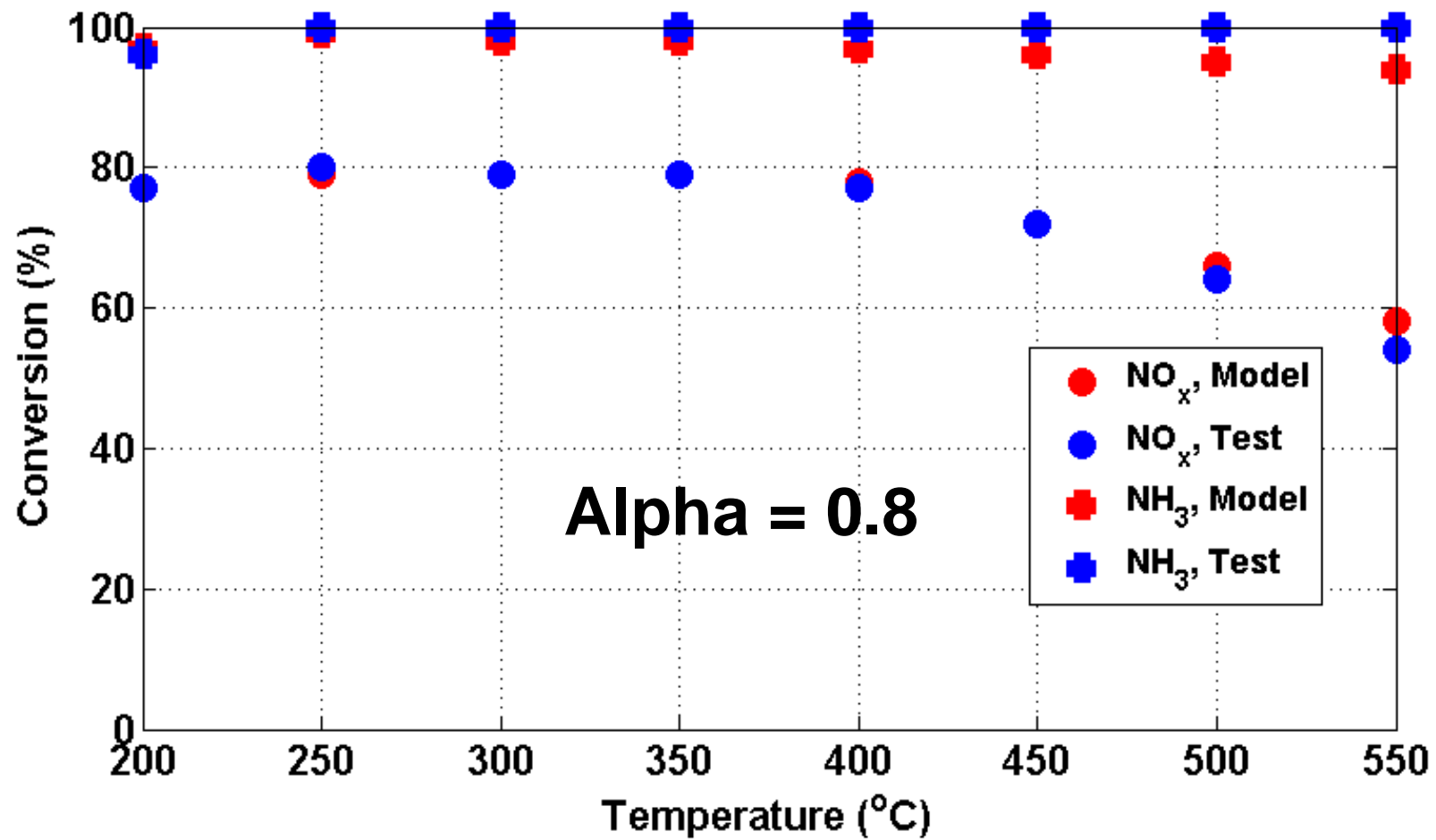


$$r_{fast-scr} = A_{fast-scr} e^{\frac{-E_{fast-scr}}{RT}} c_{g,NO} c_{g,NO_2} \theta_{NH_3}$$

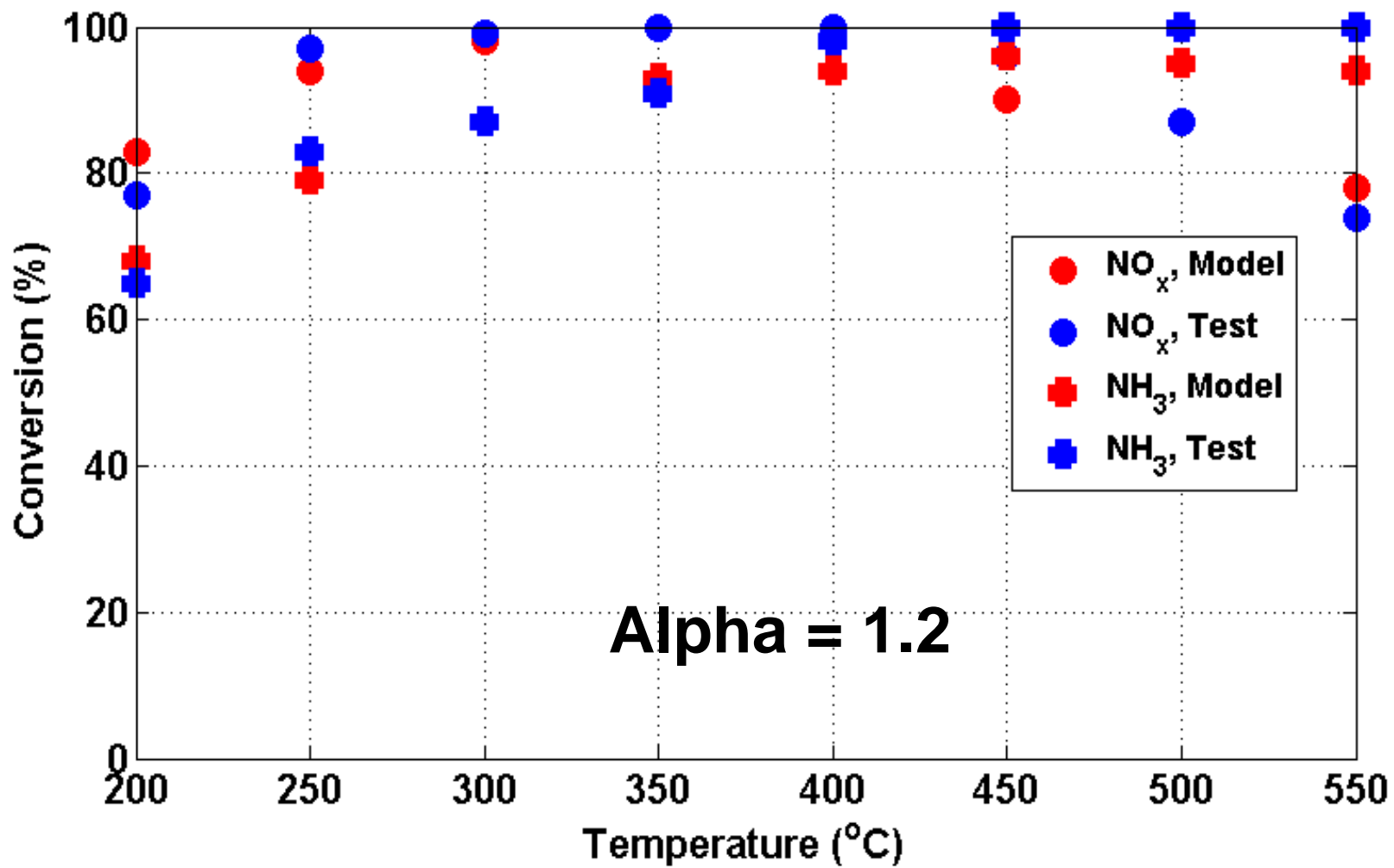
$$A_{fast-scr} = 1.9E12 \text{ m}^3/\text{mol/s}$$

$$E_{fast-scr} = 85.1 \text{ kJ/mol}$$

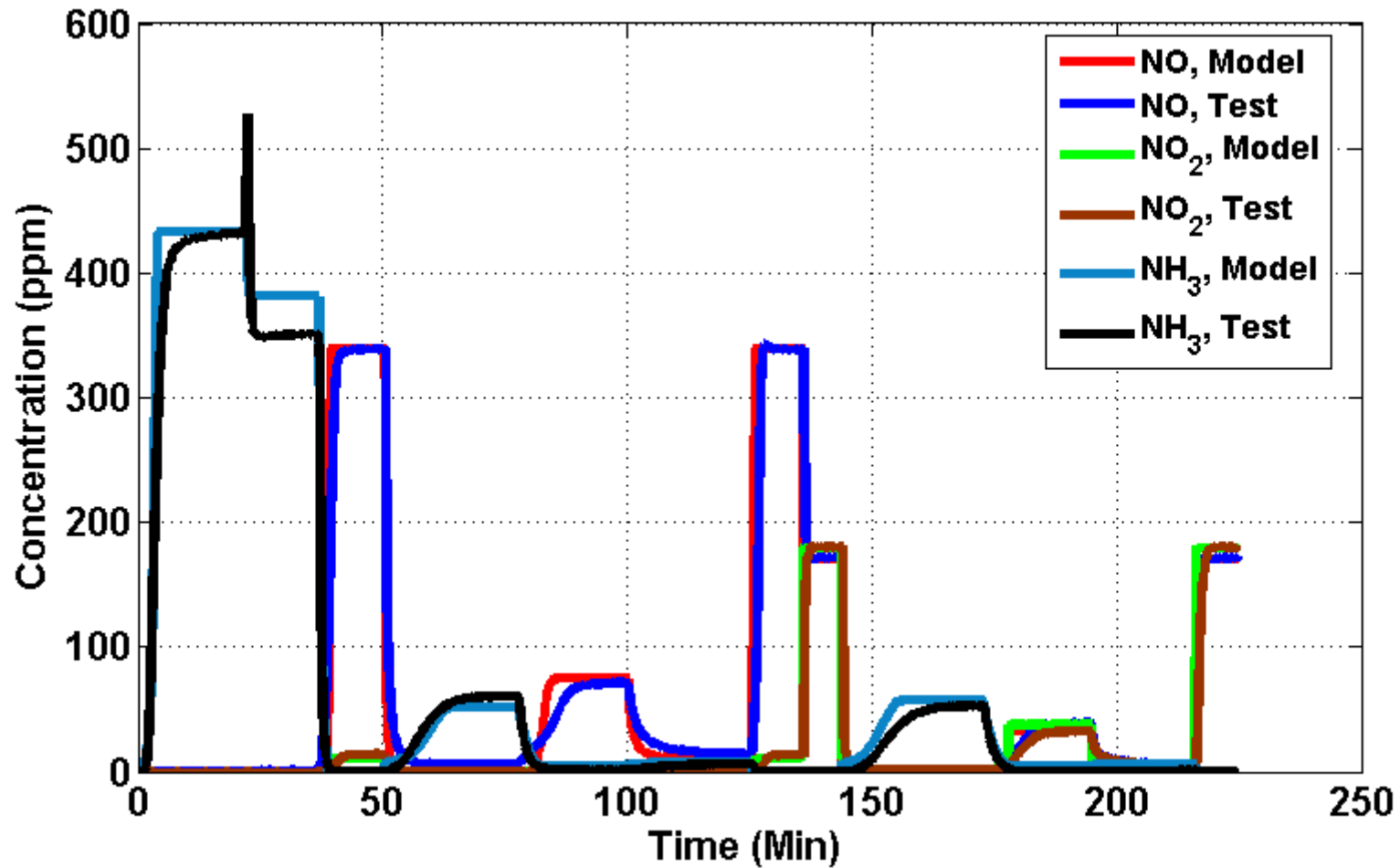
- Model validation shown only for  $T > 150^\circ\text{C}$  due to poor model match with the test data at lower temperatures. Mis-match possibly due to the absence of nitrate formation kinetics, etc in the model.
- $\text{NO}_2$ -SCR kinetic model included for better match at low temperatures. At high temperatures  $\text{NO}_2$ -SCR can be neglected.
- No parameter tuning was done – Fast SCR &  $\text{NO}_2$ -SCR parameters from Olsson et al., (2008) on Cu-Z SCR model were used in the model directly.



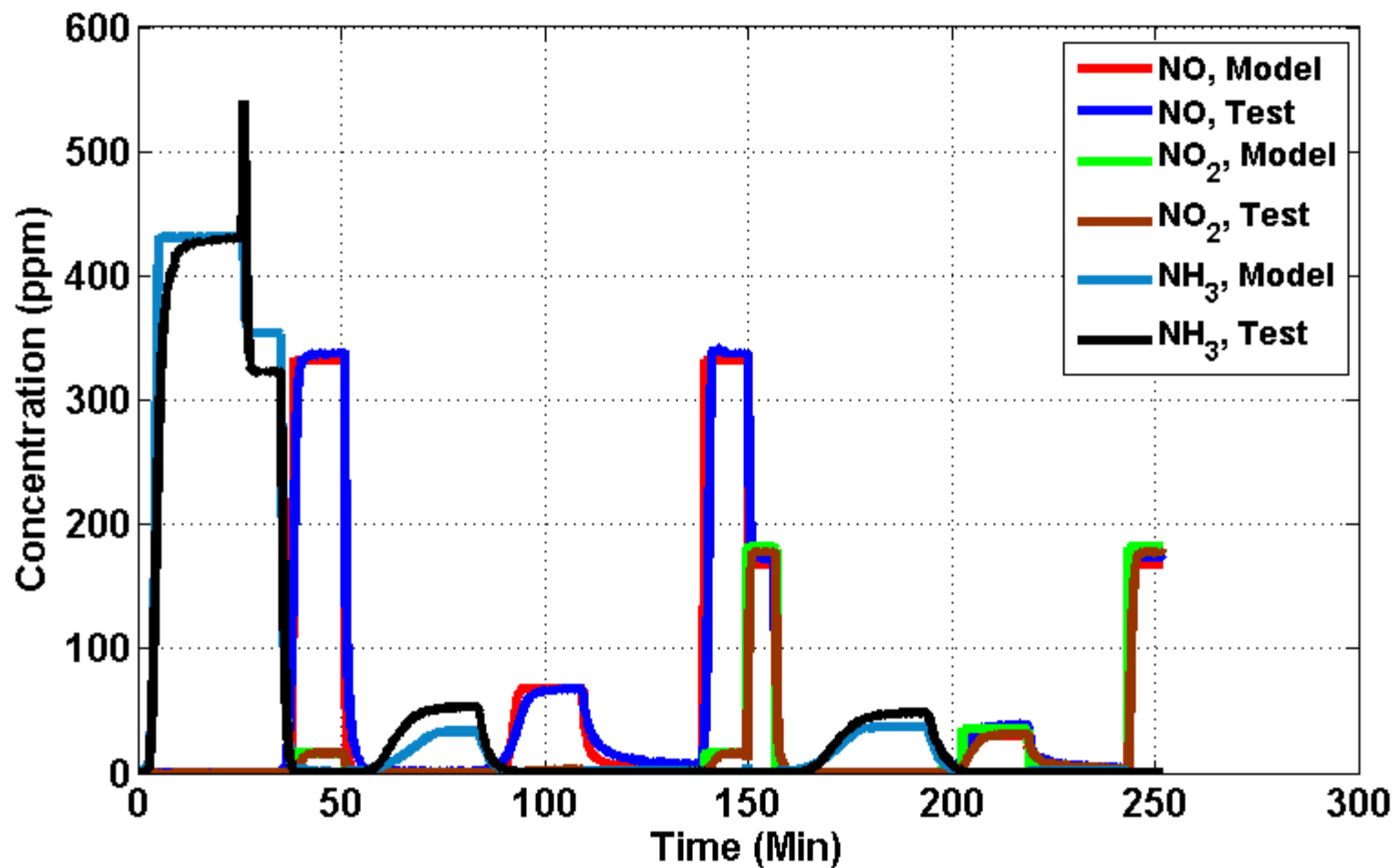




# Model Validation I: Protocol Run – 300°C (90k/hr SV)



# Model Validation II: Protocol Run – 300°C (60k/hr SV)



# Rate Parameter Comparison

Reaction	E (kJ/mol)	E (kJ/mol) from Published Literature	Reference
✓NH <sub>3</sub> Desorption	180.2	181.5	Olsson, 2008
✓NH <sub>3</sub> Oxidation	74	68.7±6.3 <sup>1</sup>	Kamasamudram, 2010
✓NO Oxidation	39	43	Chakravarthy, 2007
Standard SCR	84.9	84.9	Olsson, 2008
Fast SCR	85.1	85.1	Olsson, 2008

<sup>1</sup>Parameter reported on Fe-Z by Kamasamudram et al., Catalysis Today 151 (2010) 212-222

# Summary

- Fresh commercial Cu zeolite shows:
  - wide operating window
  - SCR performance limited by  $\text{NH}_3$  oxidation at high temperatures
  - low sensitivity to  $\text{NO}_2/\text{NO}_x$  in feed
- Protocol transients generate vital information for model-based control design:
  - target  $\text{NH}_3$  coverage for high  $\text{NO}_x$  conversion
  - “usable”  $\text{NH}_3$  storage
  - fractional catalyst utilization
- Baseline SCR model developed and validated against the reactor data for  $0.8 \leq \text{NH}_3/\text{NO}_x \leq 1.2$  and  $30\text{k} \leq \text{SV} \leq 90\text{k}$
- Low temperature performance needs to be improved by incorporating global nitrate formation kinetics,  $\text{N}_2\text{O}$  formation and  $\text{NO}_2$ -SCR reaction

# Next Steps

- Improve the baseline Cu SCR model prediction at lower temperatures
- Investigate the competitive adsorption kinetics on a model Cu/beta SCR catalyst through experiments and modeling
- Determine need for incorporating NO<sub>2</sub> SCR in protocol
- Investigate the effects of catalyst aging on the kinetic parameters and physicochemical properties of Cu SCR catalyst
- Identify critical rate/model parameters that need to be adapted for catalyst aging/deactivation and develop maps/math expressions to support model-based controls
- Incorporate the Cu SCR model into Autonomie for system-level performance simulation

# Acknowledgments

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