

# From zero to four-dimensional after-treatment models: needs and challenges

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*Exothermia SA, Greece*



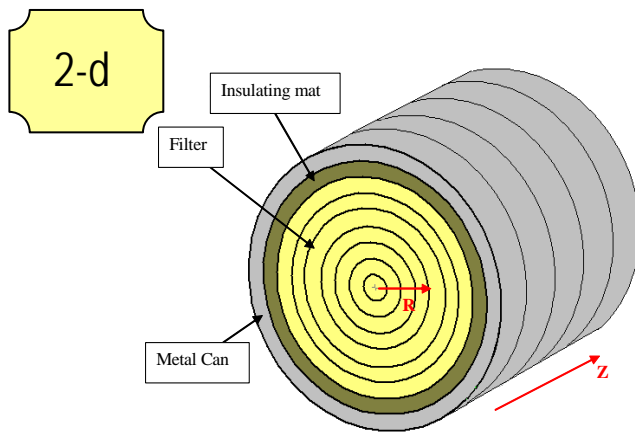
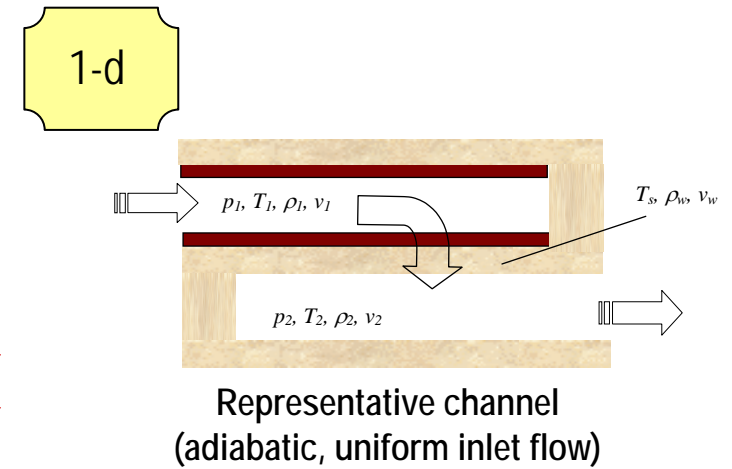
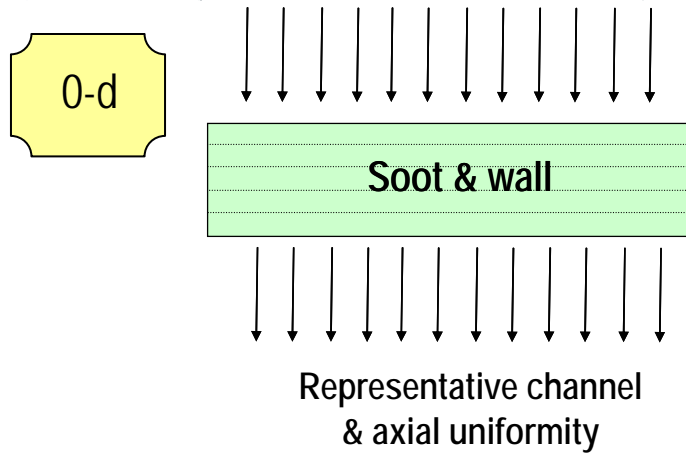
- ⚡ *How many dimensions we need for after-treatment modeling?*
- ⚡ Definitions – fundamentals
- ⚡ DPF modeling
  - Significance intra-layer modeling
  - Channel and filter scale
  - “3-dimensional” effects
  - DOC, LNT, SCR integration in wall-flow DPFs
- ⚡ Flow-through catalyst modeling
  - Flow maldistribution
  - Reductant maldistribution
- ⚡ Integrated 1d/3d exhaust system modeling
  - Components in series
  - Components in parallel

# Fundamentals

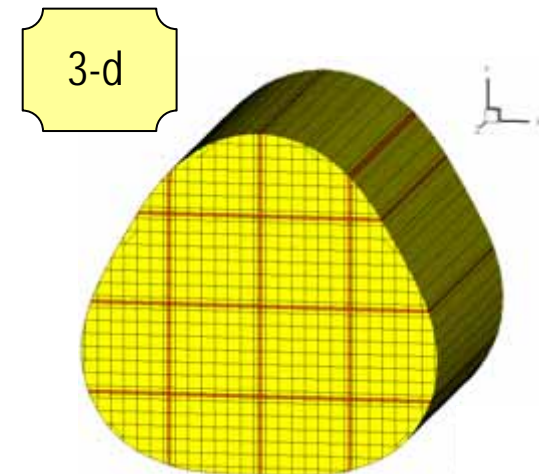
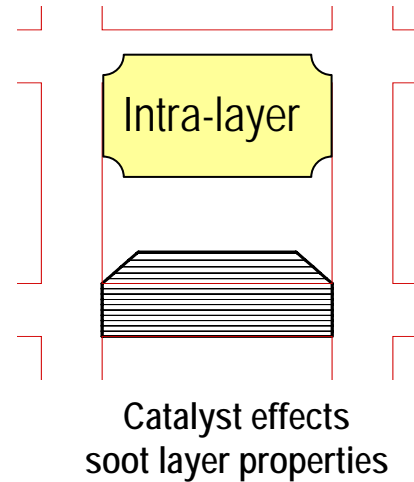
Definitions and modeling scales  
in the case of wall-flow DPF modeling



# Definitions



Axi-symmetric, non-segmented filter  
(circular shape, symmetric flow distribution)

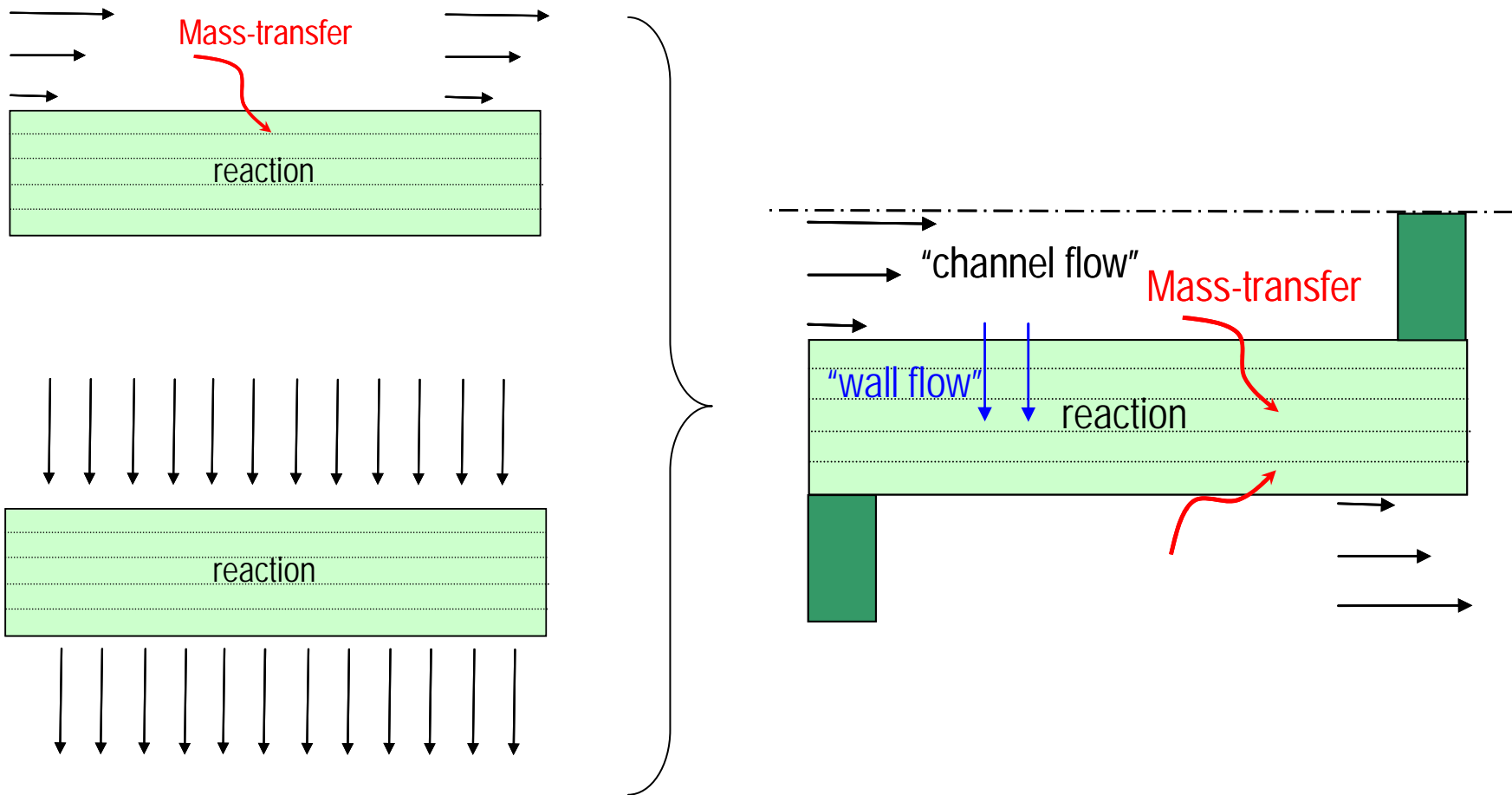


Random shape, segmentation  
any flow distribution



# The challenge of catalyzed DPF modeling

## Mixed reactor



# Species balance

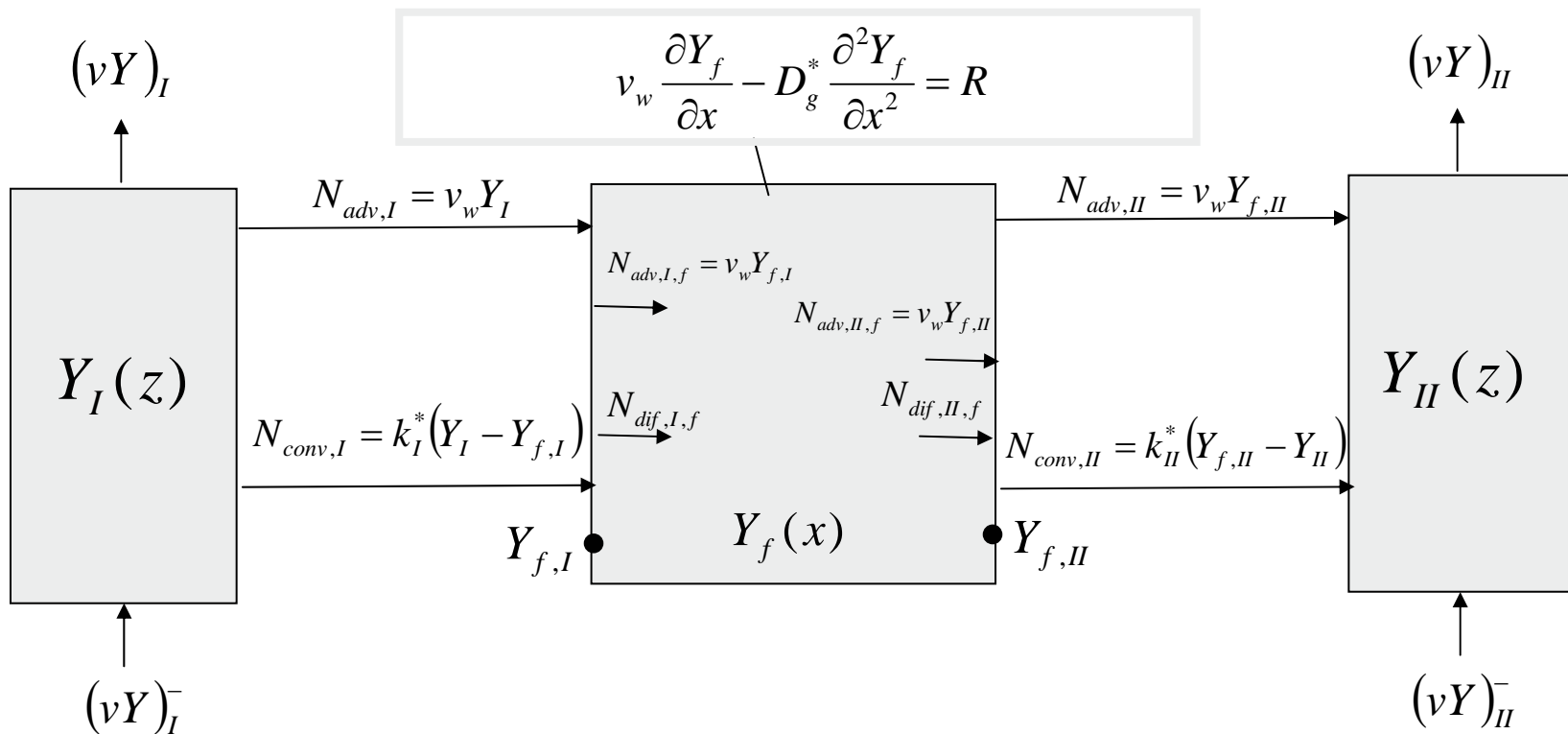


# Species equations quasi-steady, $k_w = \text{infinite}$ ( $Y_w = Y_f$ )



$$v_w Y_I + k_I (Y_I - Y_w) = v_w Y_{f,I} - D_g^* \frac{\partial Y_f}{\partial x}$$

$$-D_g^* \frac{\partial Y_f}{\partial x} = k_{II} (Y_{f,II} - Y_{II})$$



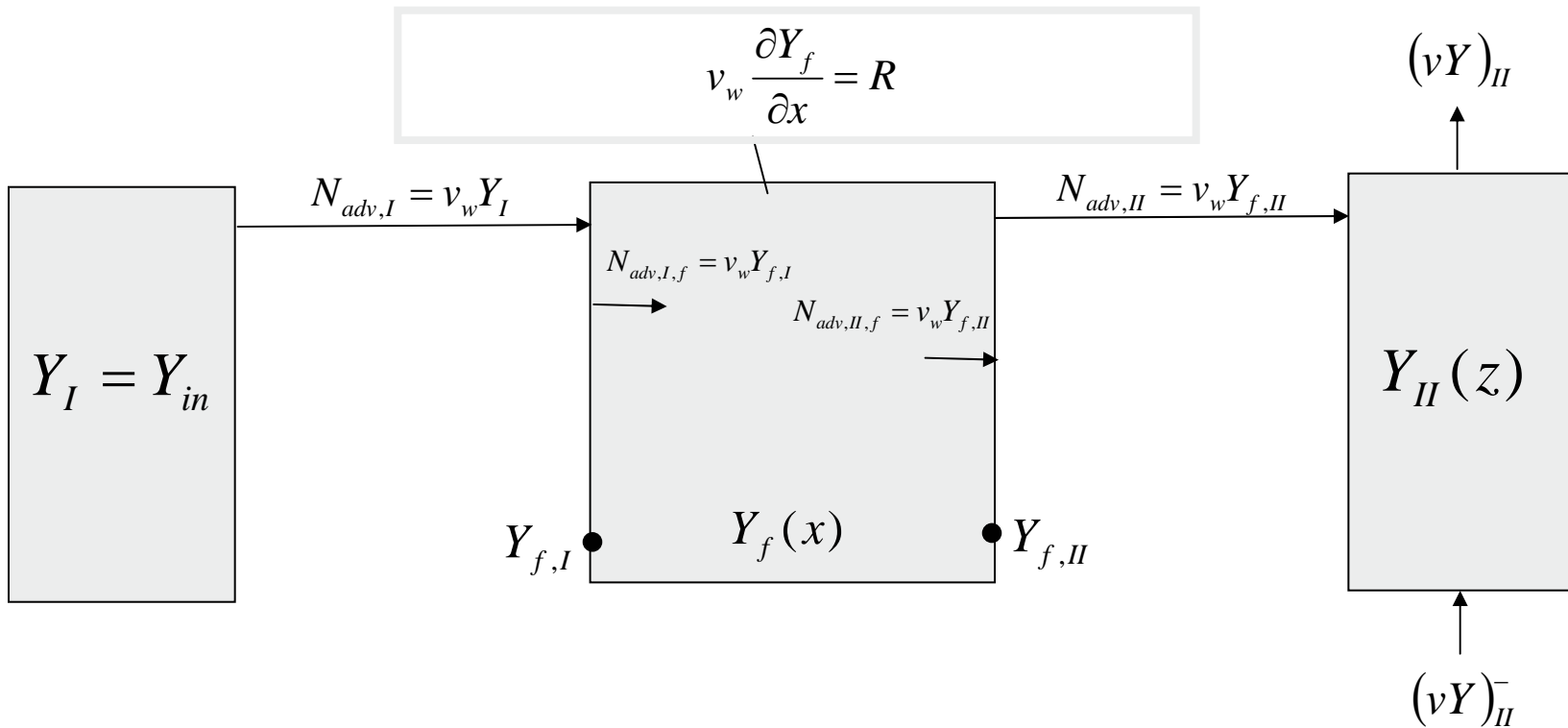
# Species equations

quasi-steady,  $k_w = \text{infinite}$ ,  $k_f = k_{II} = 0$ ,  $D_g^* = 0$



$$Y_I = Y_{f,I}$$

$$v_w \frac{\partial Y_f}{\partial x} = R$$



Bissett E. J., *Chemical Engineering Science* Vol. 39, Nos 7/8, pp. 1233-1244 (1984). "1-d model"

Bissett E. J., Shadman F., *AIChE Journal* (Vol31, No5), p. 753, May 1985. "0-d model"





# Energy balance

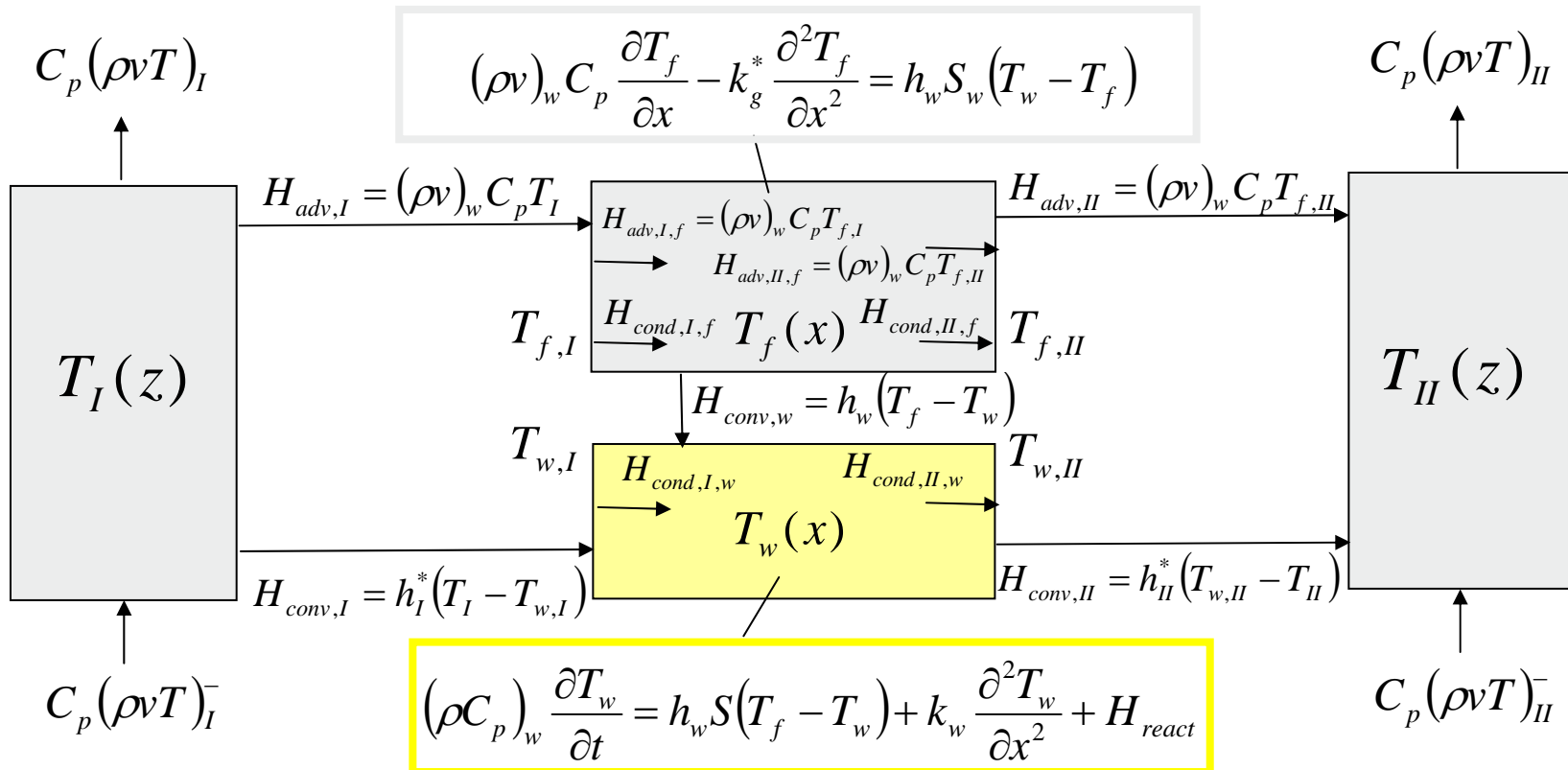


# Energy equations



$$(\rho v)_w C_p T_I = (\rho v)_w C_p T_{f,I} - k_g^* \frac{\partial T_f}{\partial x}$$

$$-k_g^* \frac{\partial T_f}{\partial x} = 0$$



$$(\rho C_p)_w \frac{\partial T_w}{\partial t} = h_w S (T_f - T_w) + k_w \frac{\partial^2 T_w}{\partial x^2} + H_{react}$$

$$h_I^* (T_I - T_{w,I}) = -k_w \left. \frac{\partial T_w}{\partial x} \right|_{x=0}$$

$$h_{II}^* (T_{w,II} - T_{II}) = -k_w \left. \frac{\partial T_w}{\partial x} \right|_{x=w}$$



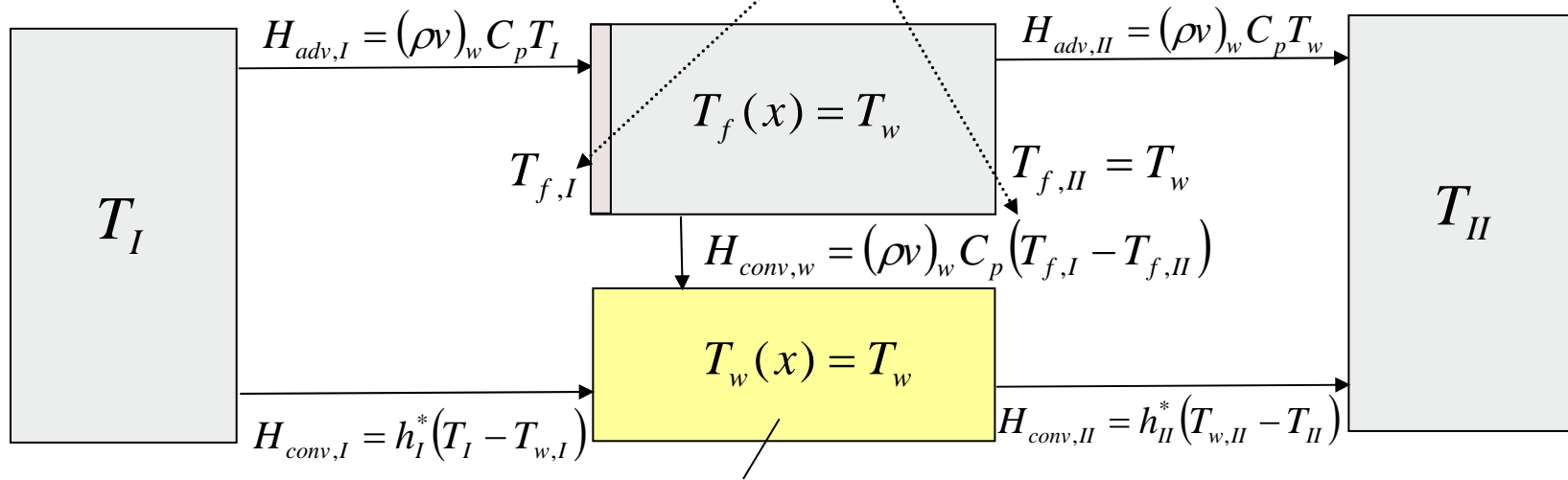
# Energy equations simplification, $h_w$ infinite, $T_f = T_w$ after $dx$



$$T_I = T_{f,I}$$

$$T_{f,II} = T_w$$

In Bissett's 1984 model:  $T_{f,I} = T_w$



$$(\rho C_p)_w \frac{\partial T_w}{\partial t} = H_{conv,w} + H_{react} + H_{conv,I} + H_{conv,II}$$

Bissett E. J., *Chemical Engineering Science* Vol. 39, Nos 7/8, pp. 1233-1244 (1984). "1-d model"

Koltsakis G. C., Stamatelos A. M., *Ind. Eng. Chem. Res.*, 1997 Vol. 36 p. 4155-4165. "catalytic 1-d model, modified energy balance"

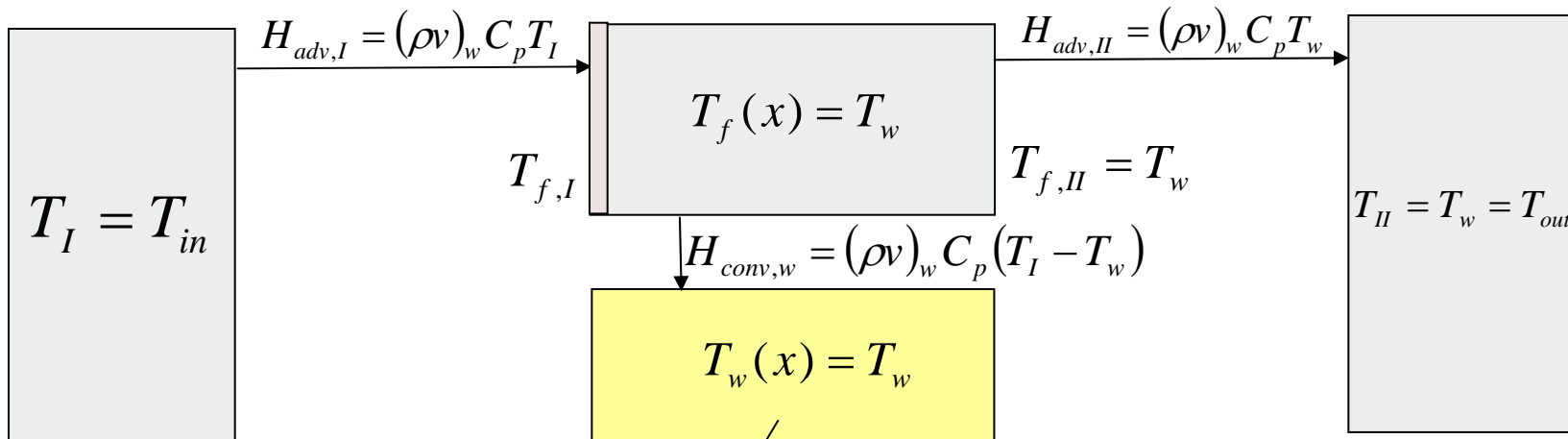


# Energy equations simplification, $h_i^* = 0, h_{ii}^* = 0$



$$T_I = T_{f,I}$$

$$T_{f,II} = T_w$$



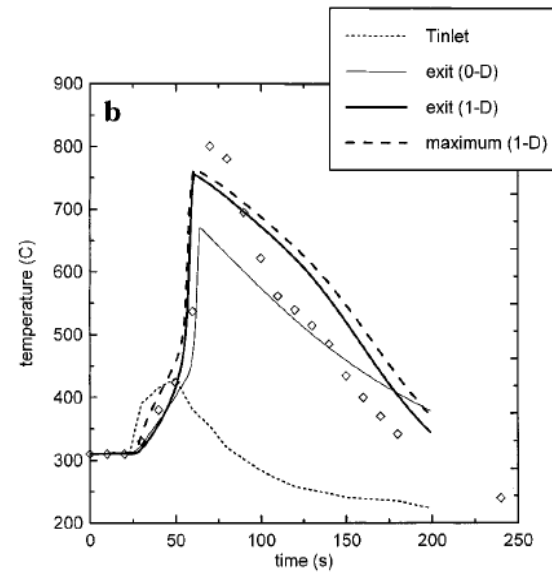
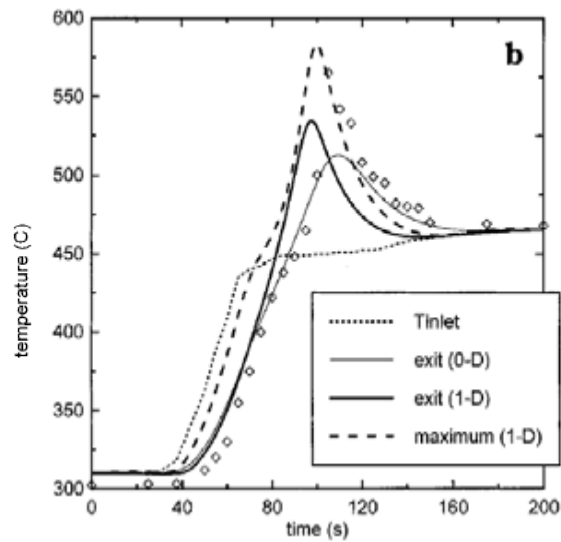
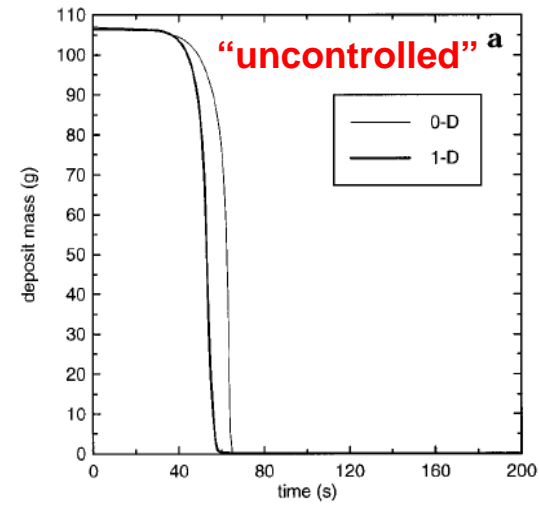
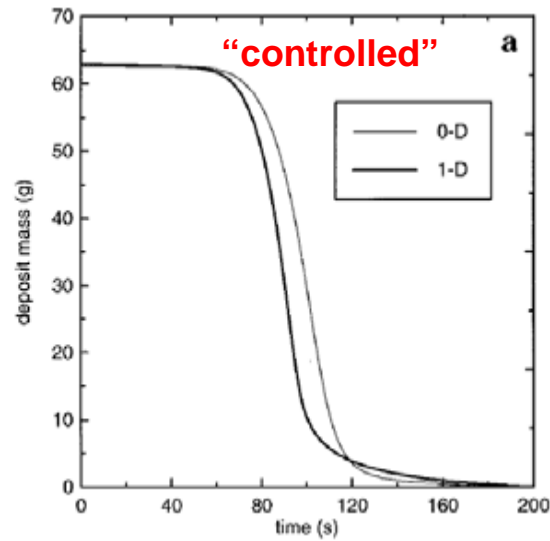
$$(\rho C_p)_w \frac{\partial T_w}{\partial t} = H_{conv,w} + H_{react}$$

Bissett E. J., Shadman F., *AIChE Journal* (Vol31, No5), p. 753, May 1985. "0-d model"

Koltsakis G. C., Stamatelos A. M., *Ind. Eng. Chem. Res.*, 1996, 35, 2-13 "catalytic 0-d model"



# 0-d vs 1-d modeling results



Koltsakis G. C., Stamatelos A. M., *Ind. Eng. Chem. Res.*, 1997, Vol. 36 p. 4155-4165.

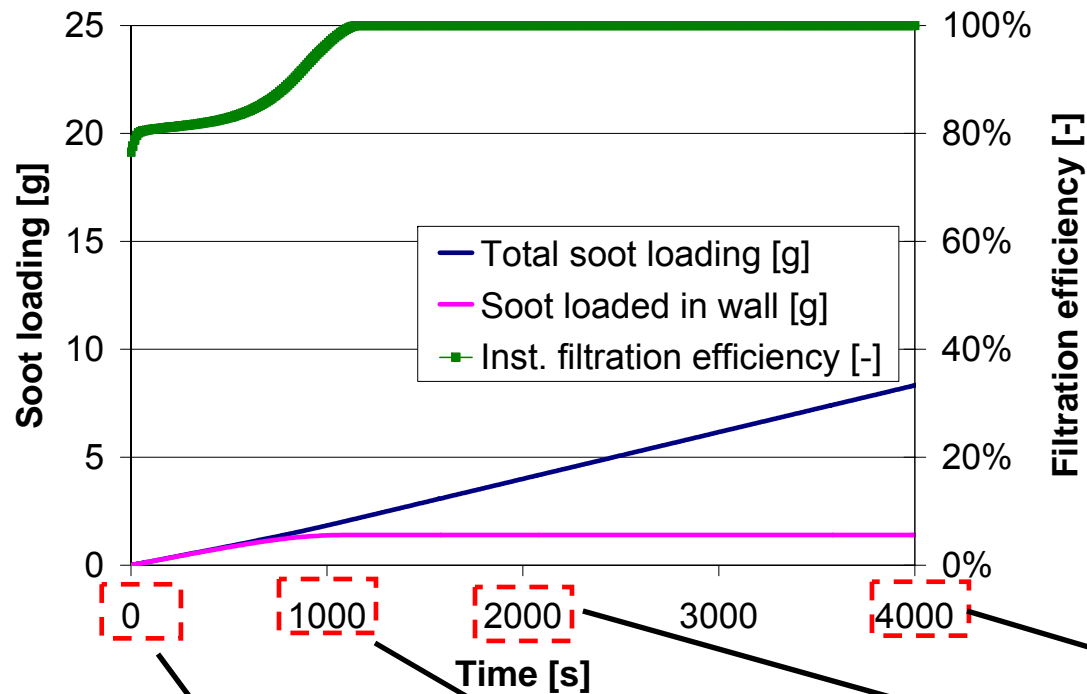


# Intra-layer dimension in DPF modeling

Soot filtration and pressure drop effects



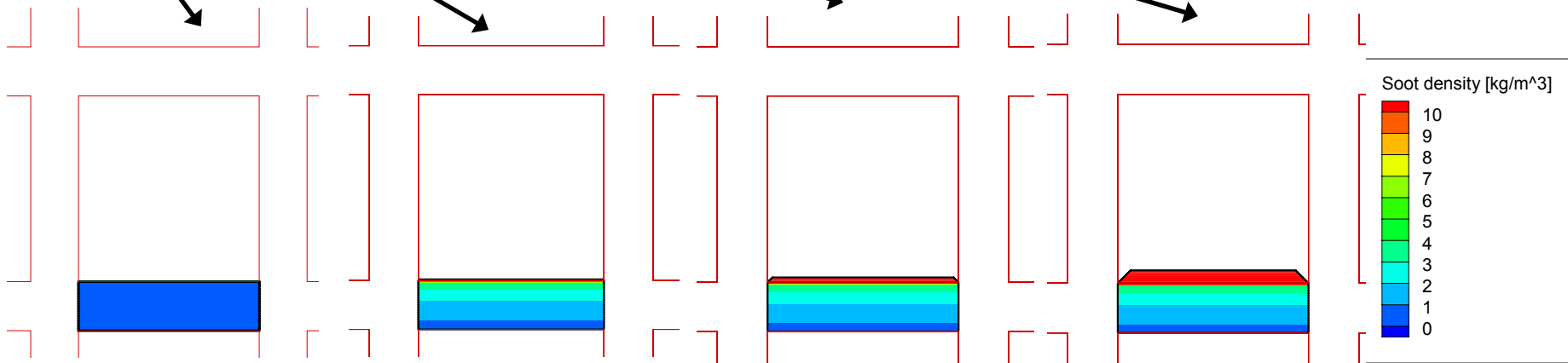
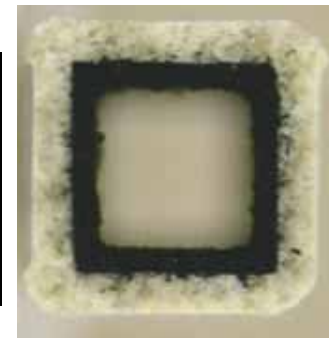
# Intra-layer dimension Filtration efficiency and soot accumulation



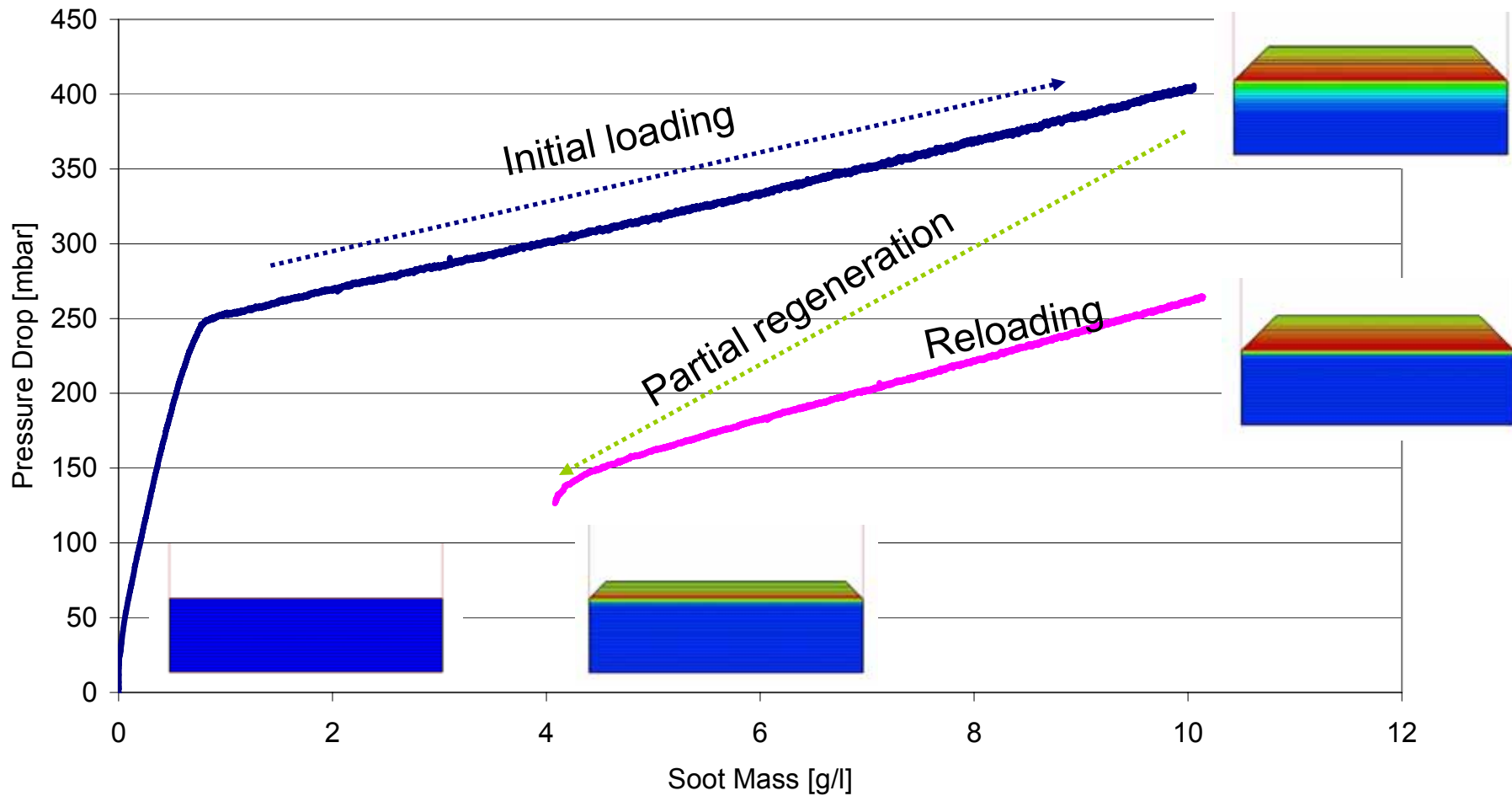
Transition from wall to cake filtration

Calculation of soot distribution within the wall

Model calibration with in-house single-channel studies



# Pressure drop "hysteresis" Wall-scale effects

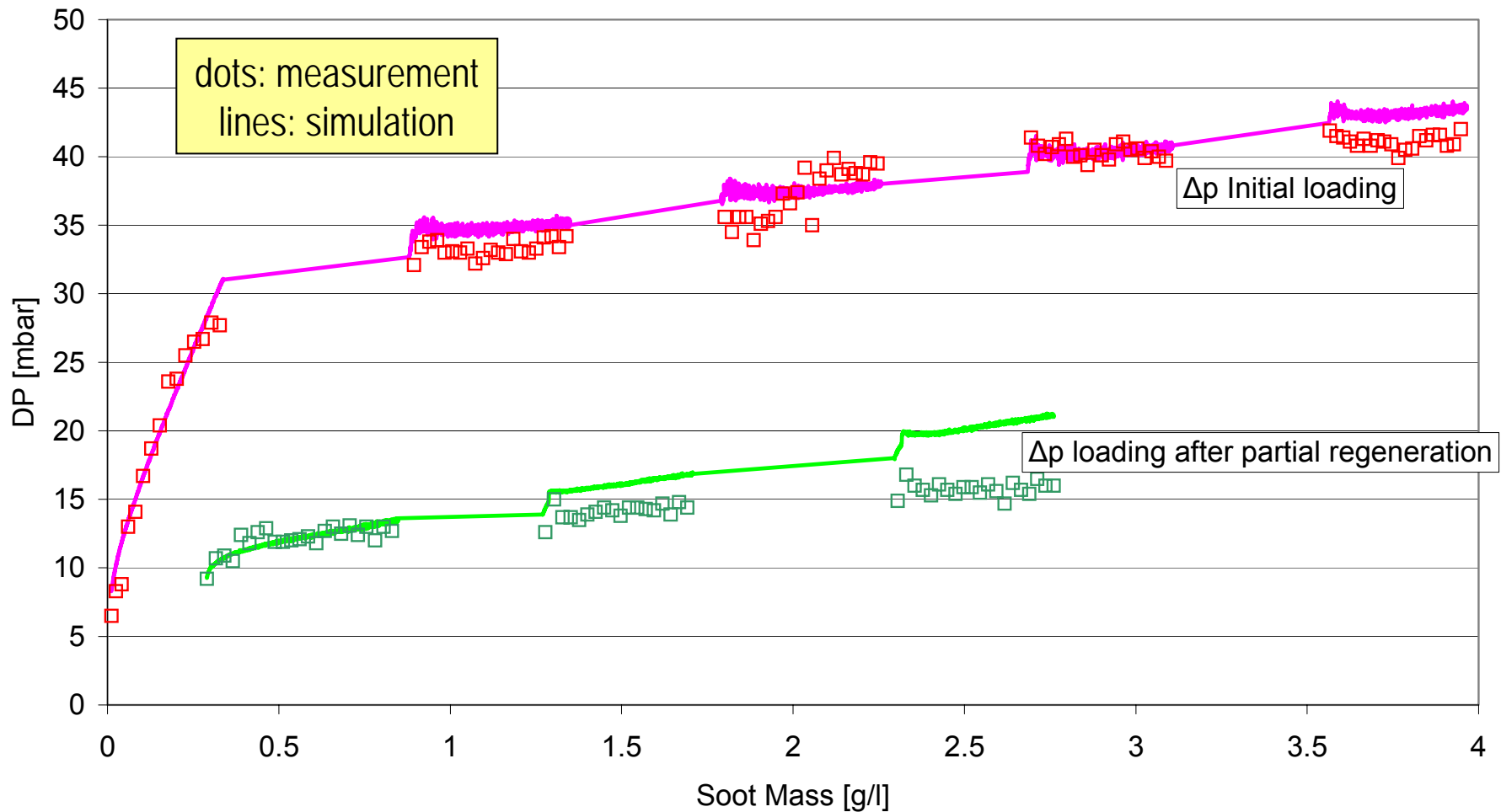


Incoming soot does not re-penetrate the wall. The correlation of pressure drop vs soot loading is depends on partial regeneration history.





# Pressure drop hysteresis effect



Following an incomplete regeneration, the cake soot does not allow the incoming soot to penetrate the wall. The pressure drop correlation with soot loading changes dramatically.



# Channel and filter scale effects on flow & soot distribution

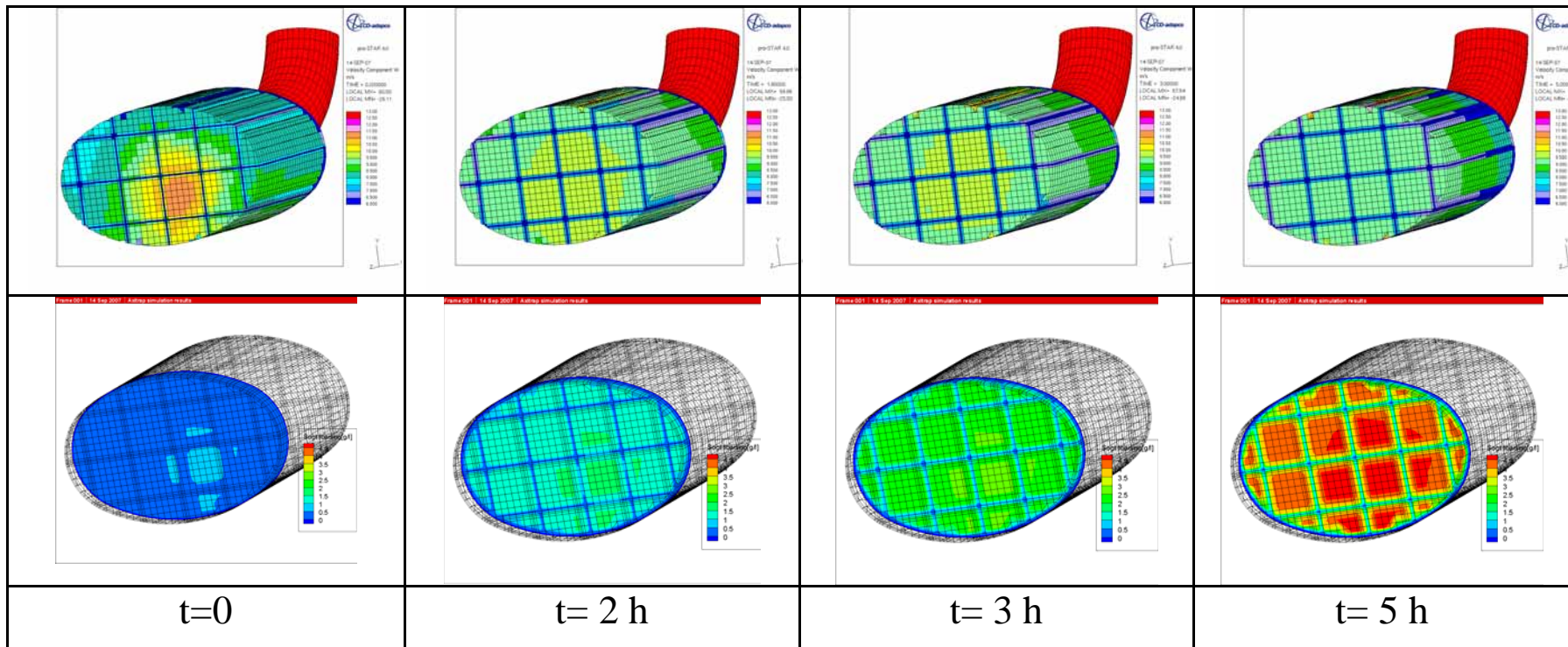


# Soot accumulation Filter scale



## Example : Coupling of *axitrap*<sup>TM</sup> with Adapco Star-CD

Transient soot accumulation (bottom) and flow redistribution (top) in an asymmetric DPF geometry



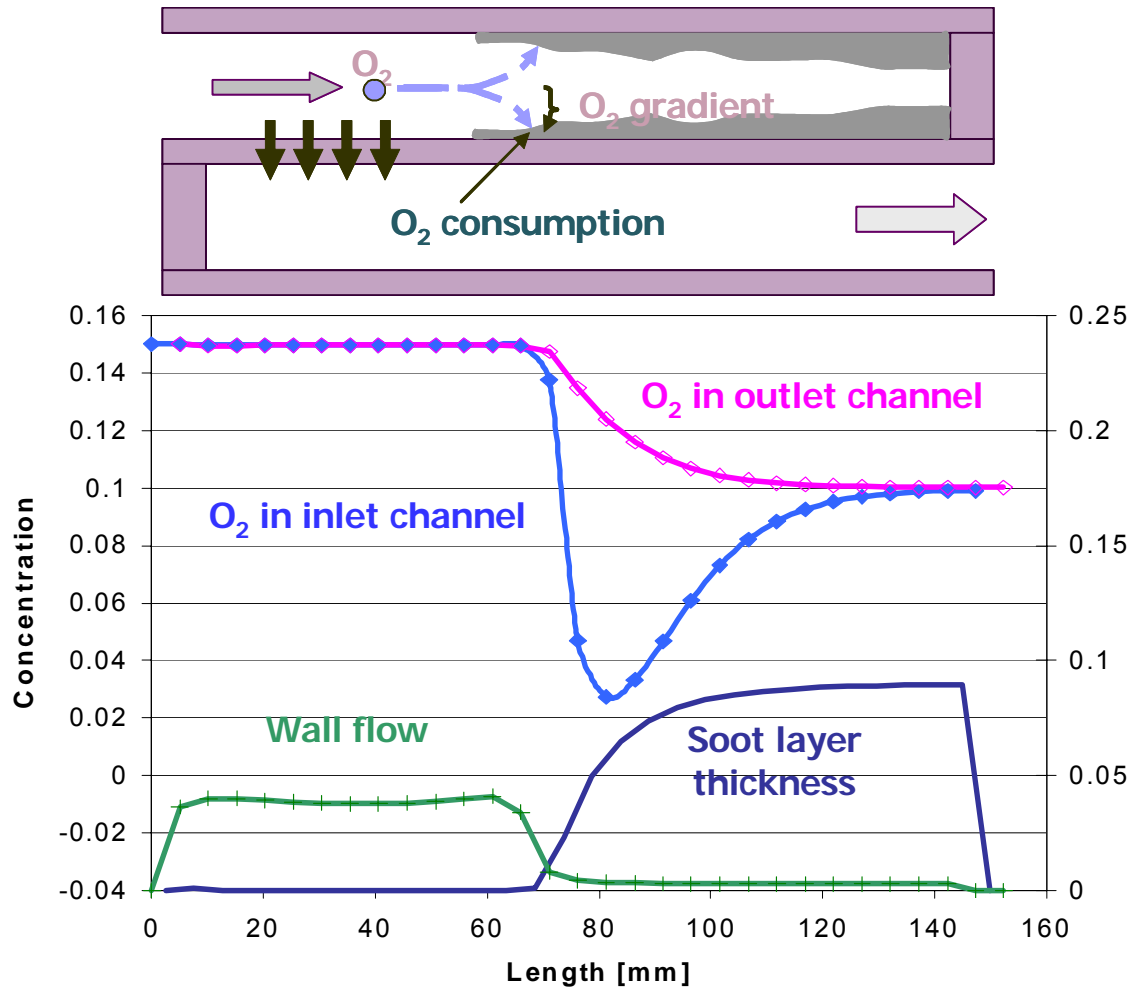
Knowledge of soot accumulation is important for pressure drop and regeneration predictions



# O<sub>2</sub> transfer effects on soot limit calculation



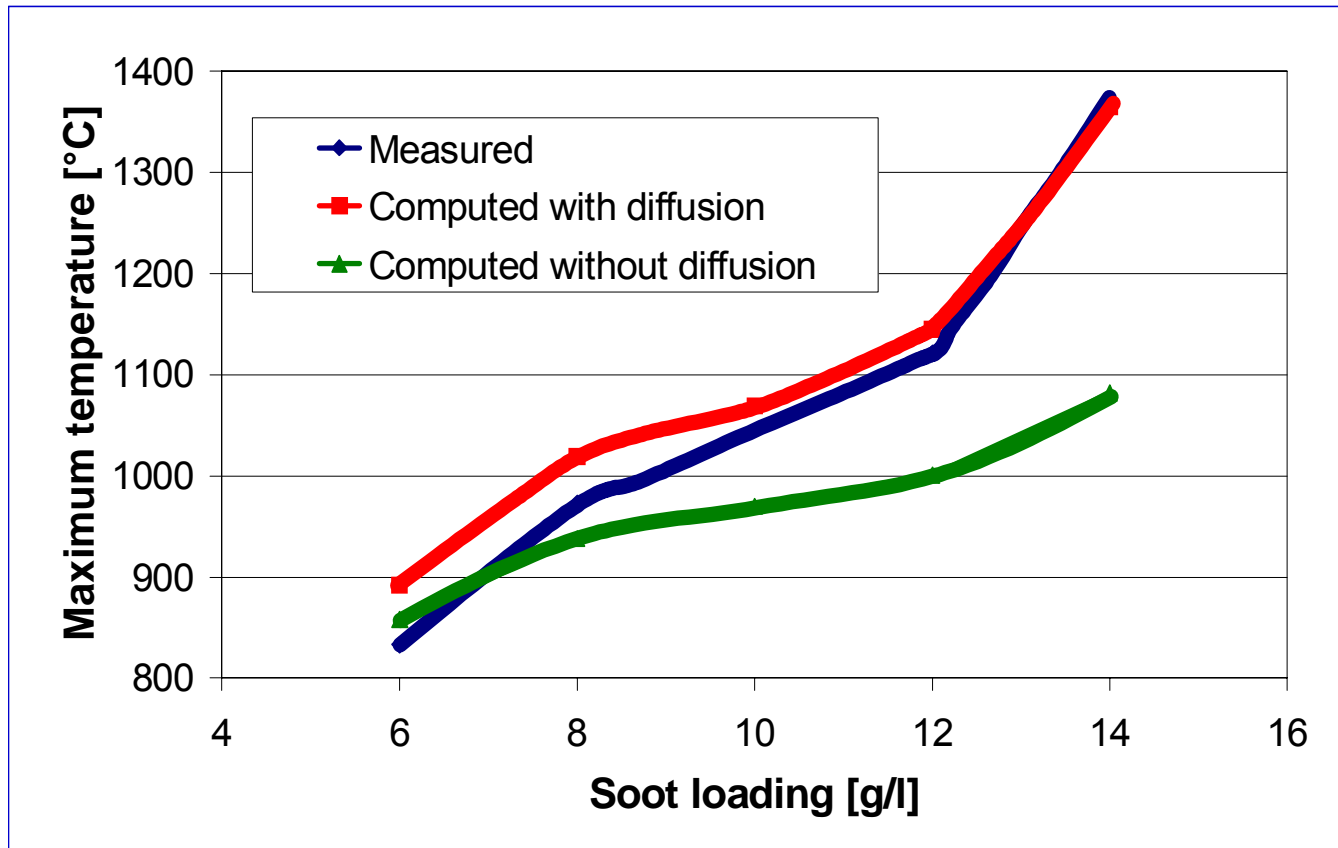
# O<sub>2</sub> transfer from channel gas to soot surface



Due to concentration gradient, O<sub>2</sub> is transferred from the axial flow to the soot layer and increases availability and reaction rates



# Importance of O<sub>2</sub> transfer for the prediction of filter temperature



*Test conditions: Gas burner, cordierite filter,  $T_{in}=600^{\circ}\text{C}$*

Ignoring O<sub>2</sub> mass-transfer effects (diffusive-convective) leads to serious under-prediction of peak temperatures

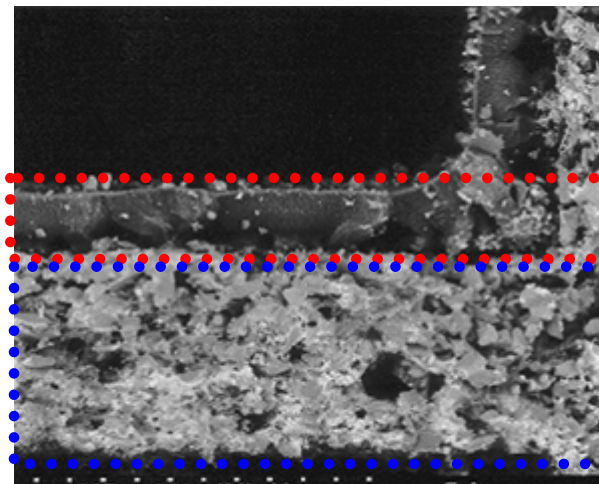


# NO<sub>2</sub> transfer effects on CDPF modeling

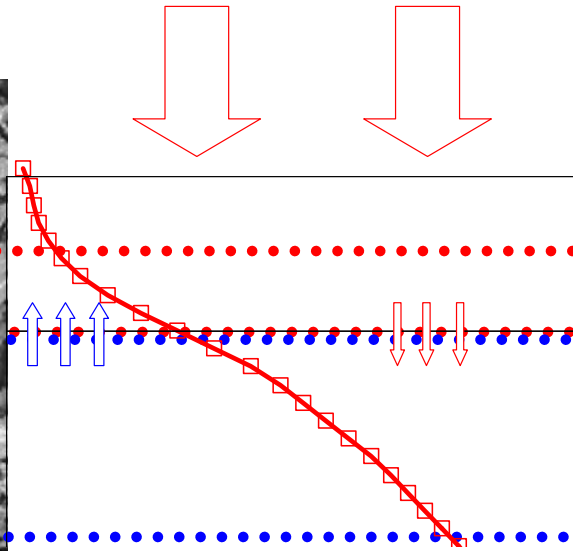
Back-diffusion  
NO<sub>2</sub> "recycling"  
WLNT modeling  
WSCR modeling



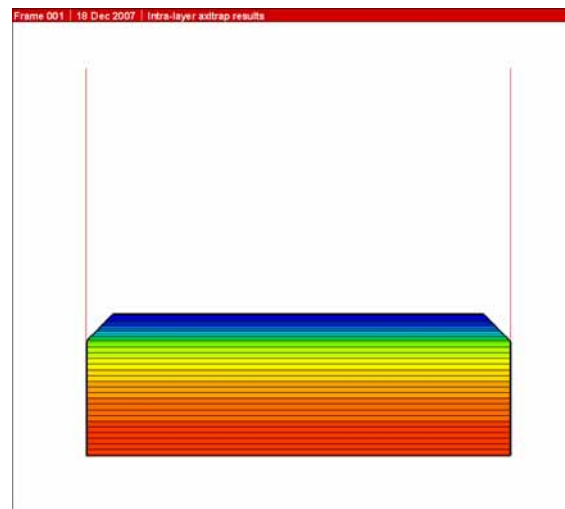
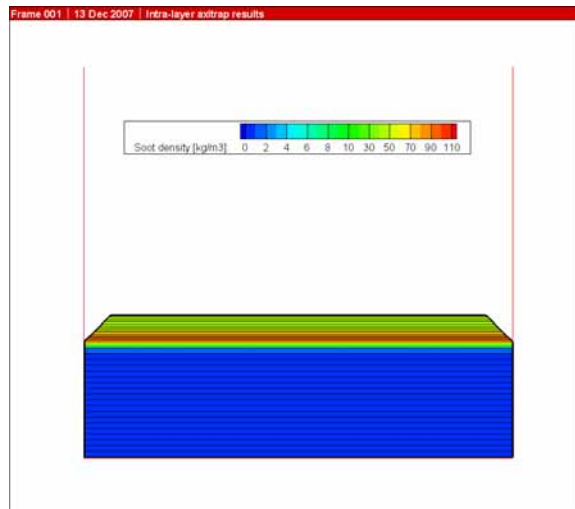
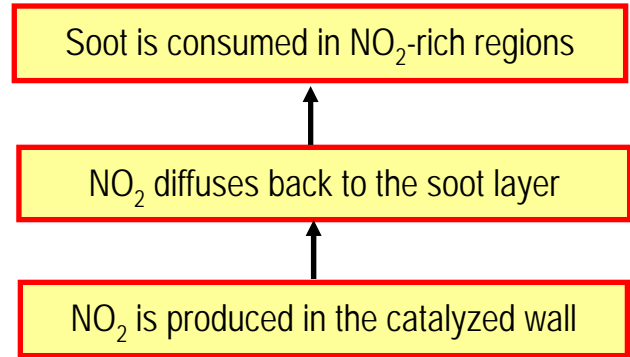
# "Passive" regeneration via $\text{NO}_2$ in catalyzed filters



Soot density



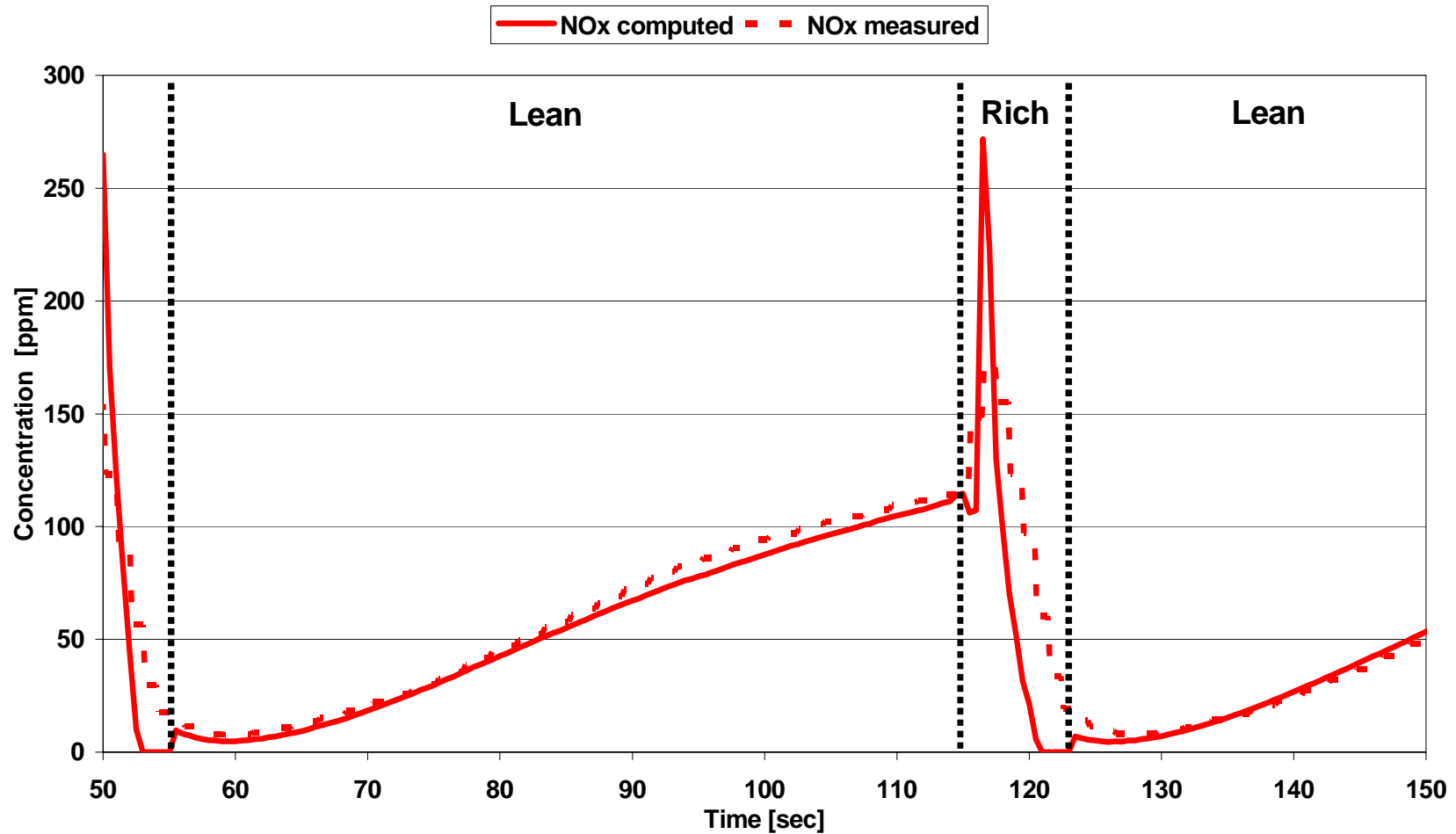
$\text{NO}_2$  concentration





# WLNT (DPNR) simulation example

## Lean-rich cycle at 350°C

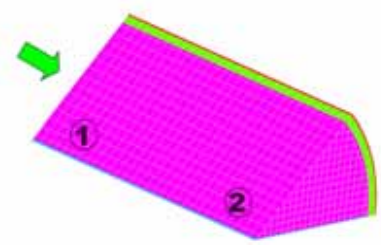
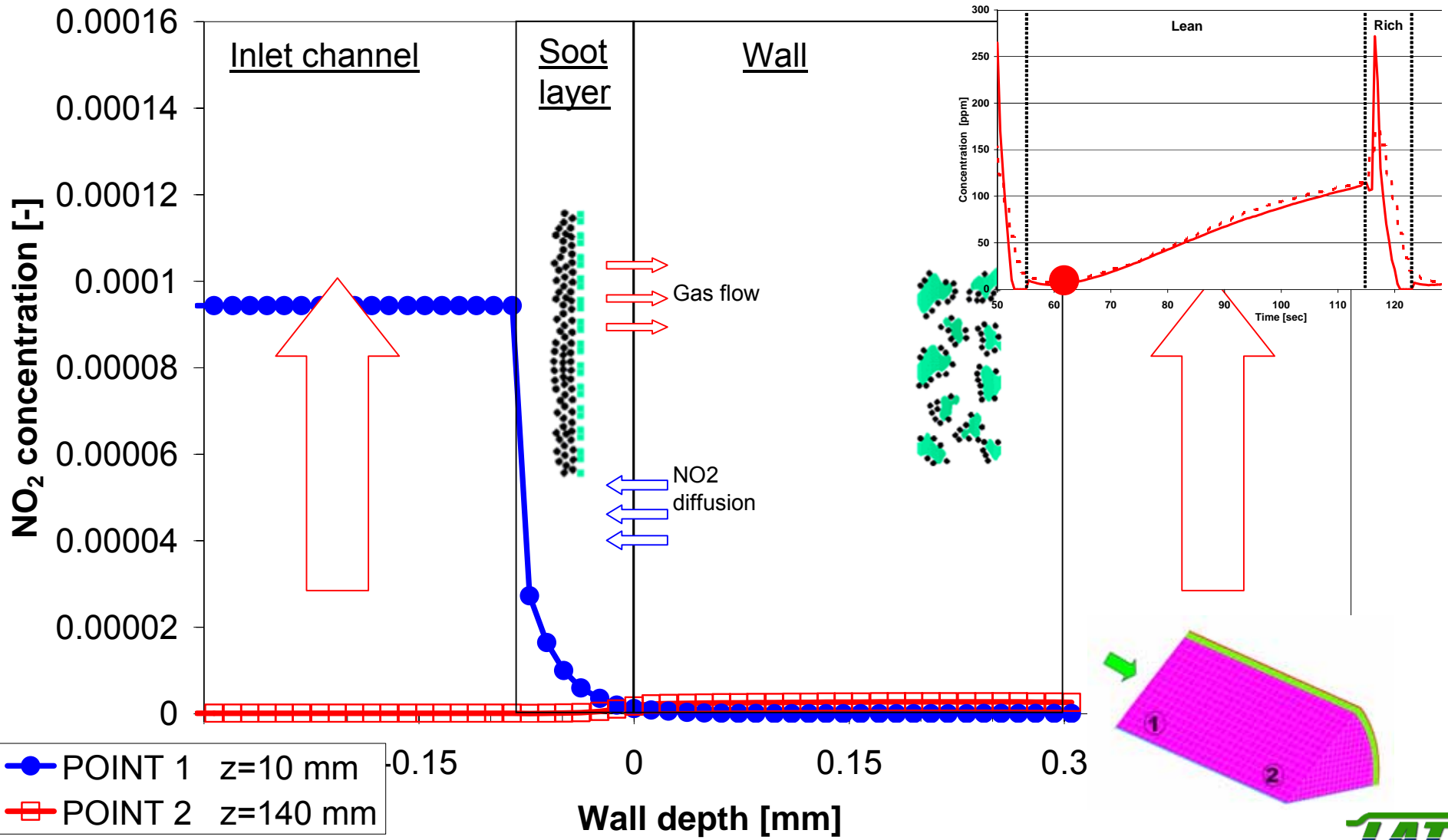


*Experimental data from engine testing at IAV GmbH*



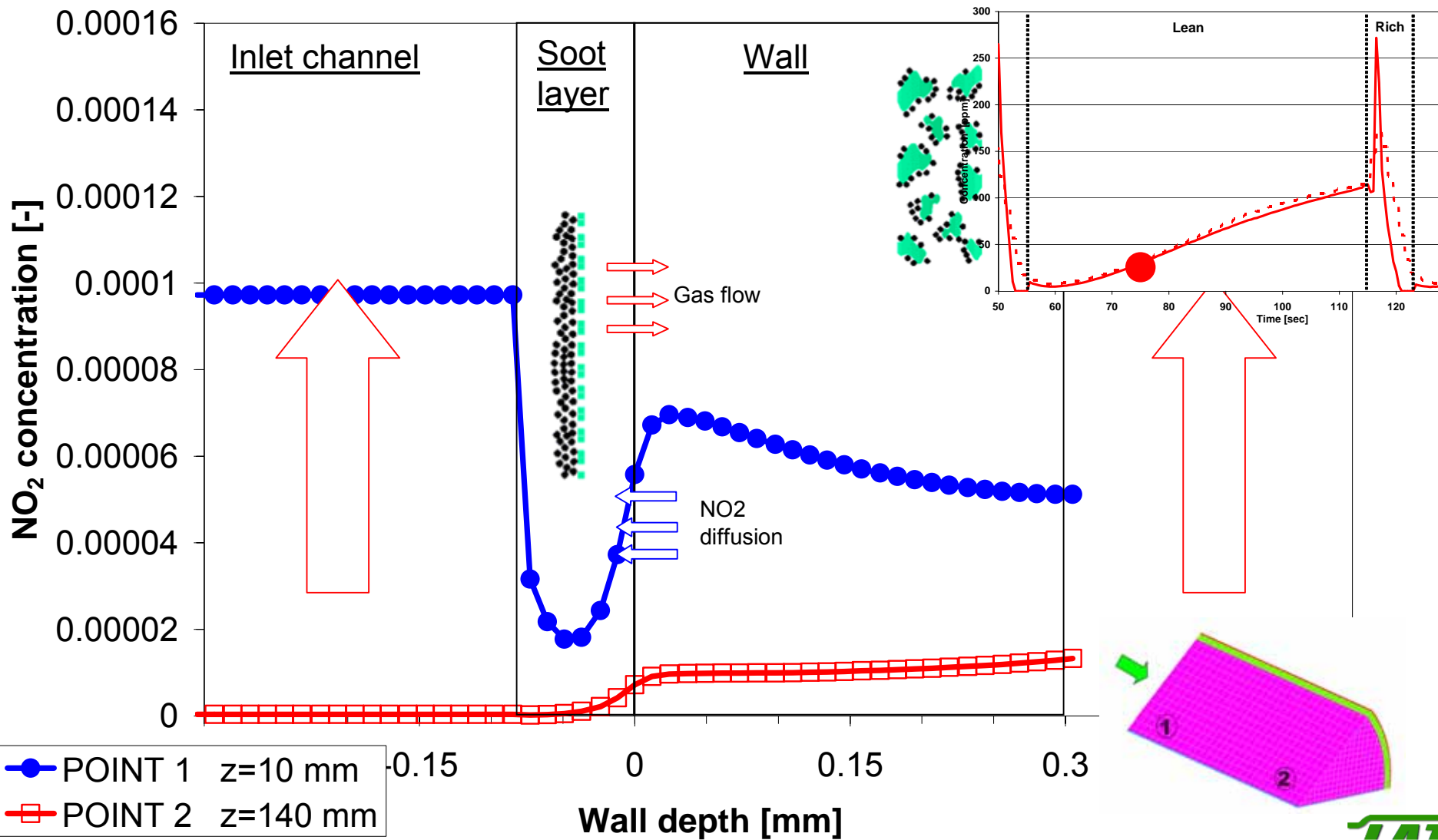
# Intra-layer NO<sub>2</sub> profiles

t=60 s



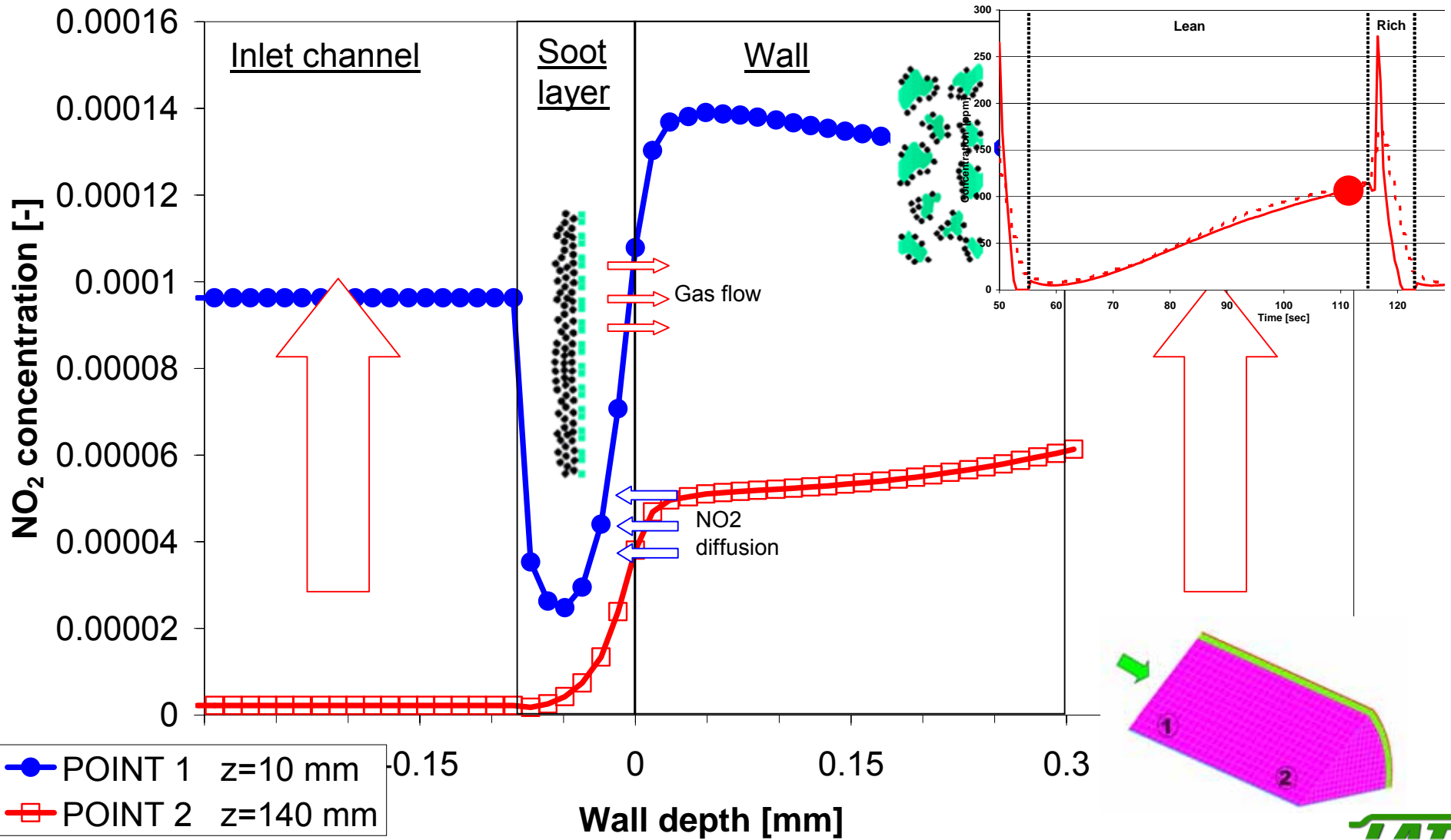
# Intra-layer NO<sub>2</sub> profiles

t=75 s



# Intra-layer NO<sub>2</sub> profiles

t=114 s



# DOC functionality

CO, HC oxidation  
DOC replacement  
Catalyst zoning



# Catalyzed DPF simulation

## Catalyst zoning (Precious Metal saving concept)



### ⚡ Uncoated DPF



### ⚡ "Axial" zoning

- More PGM in front part
- Better cold-start performance



### ⚡ "Intra-wall" zoning

- More catalyst close to soot layer
- Better passive regeneration performance

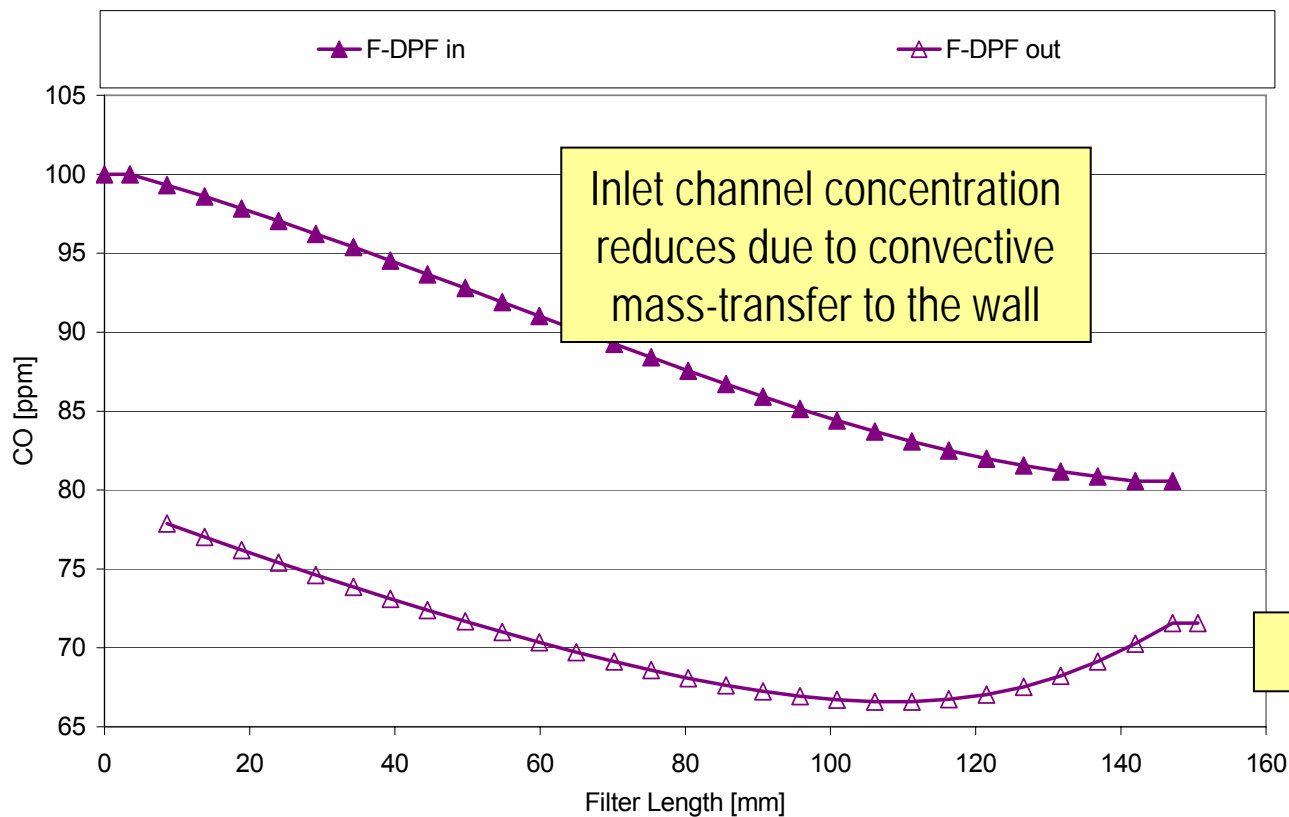
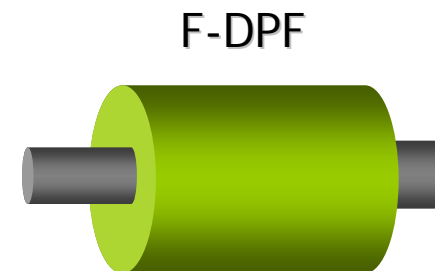
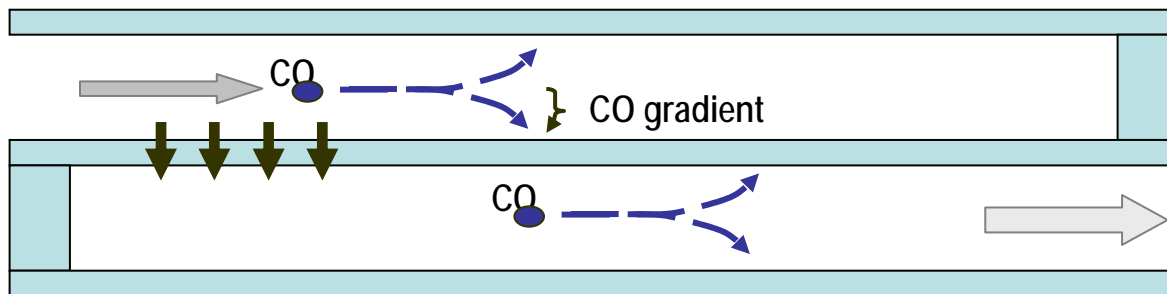


Transport/reaction coupling necessary to account for catalyst zoning

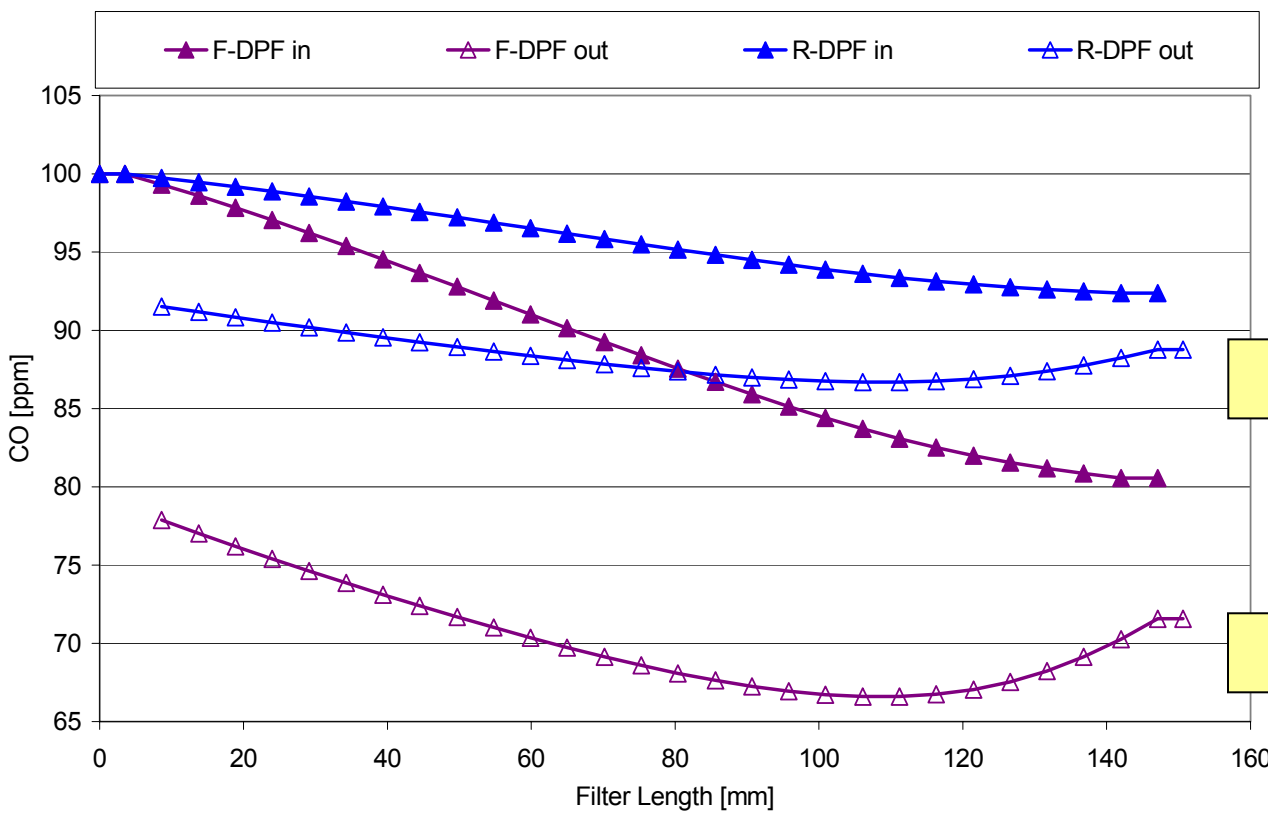
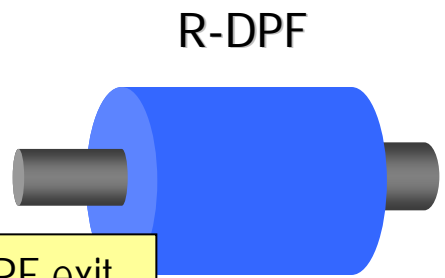
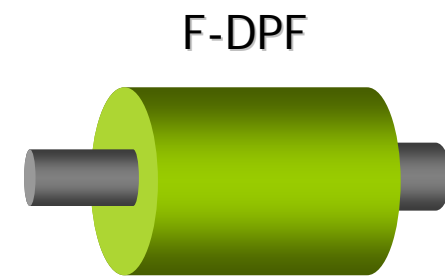
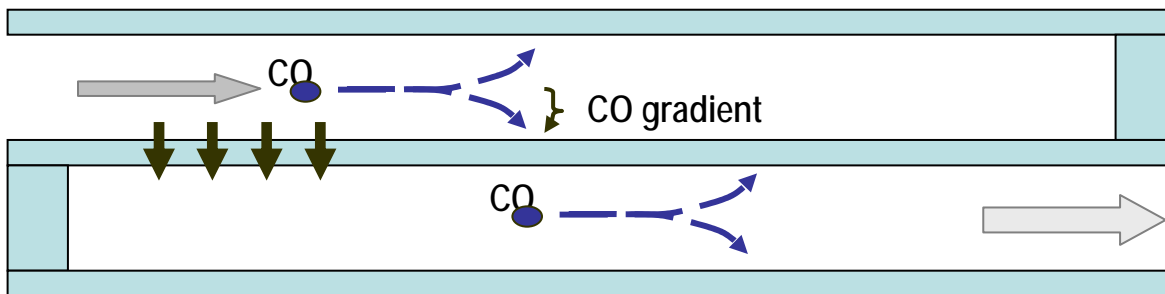
- Uncatalyzed wall
- Catalyzed with high PGM
- Catalyzed with low PGM
- Soot layer



# Computed concentration profiles in catalyzed filters @ T=150°C



# Computed concentration profiles in catalyzed filters @ T=150°C



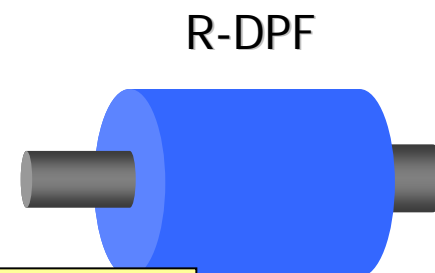
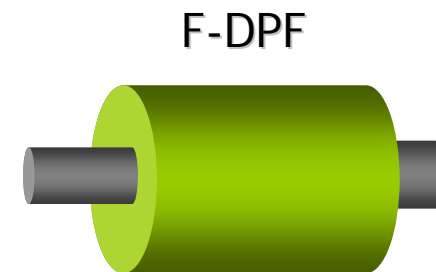
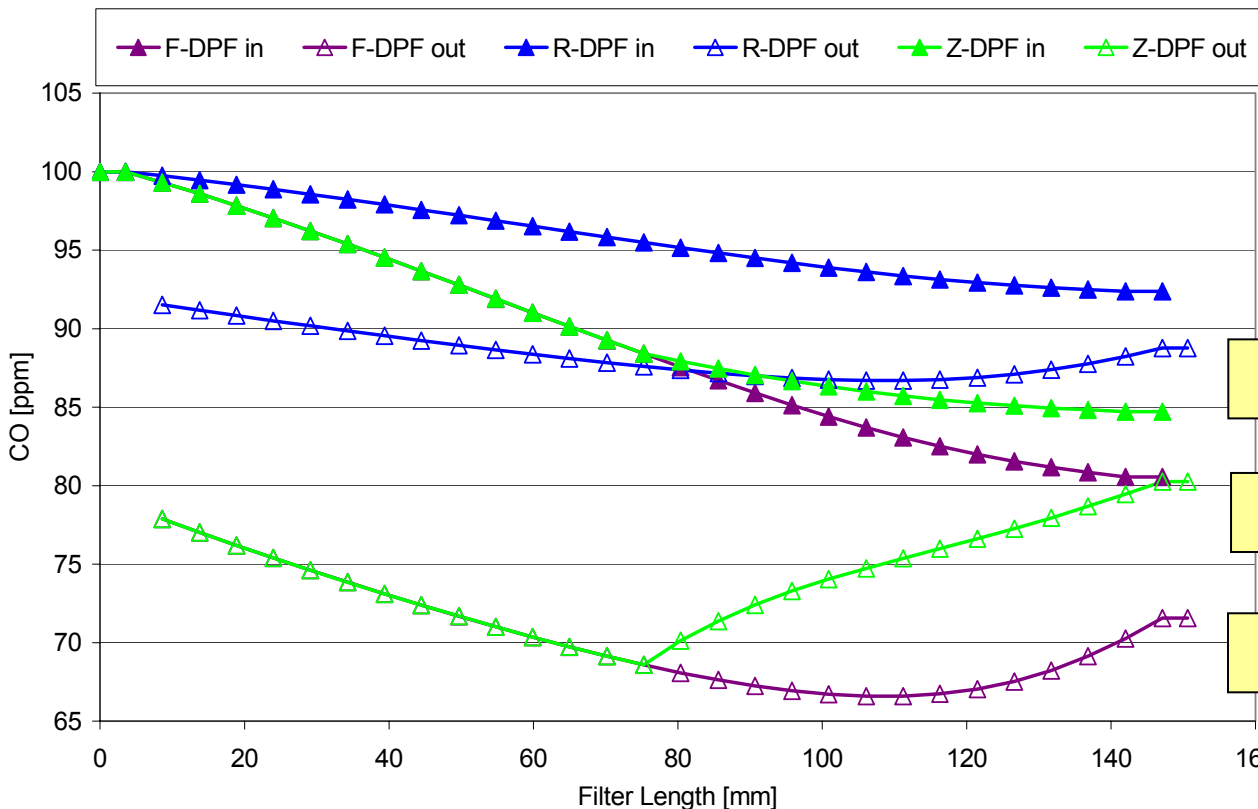
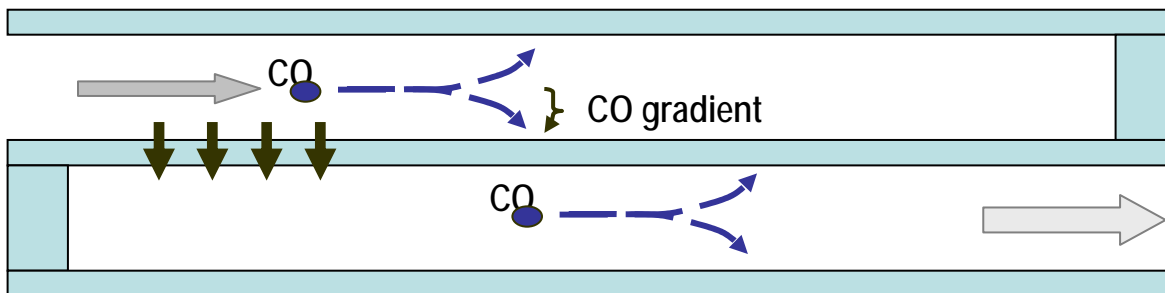
R-DPF exit

F-DPF exit





# Computed concentration profiles in catalyzed filters @ T=150°C



R-DPF exit

Z-DPF

F-DPF exit



# 3-d effects

Heat transfer

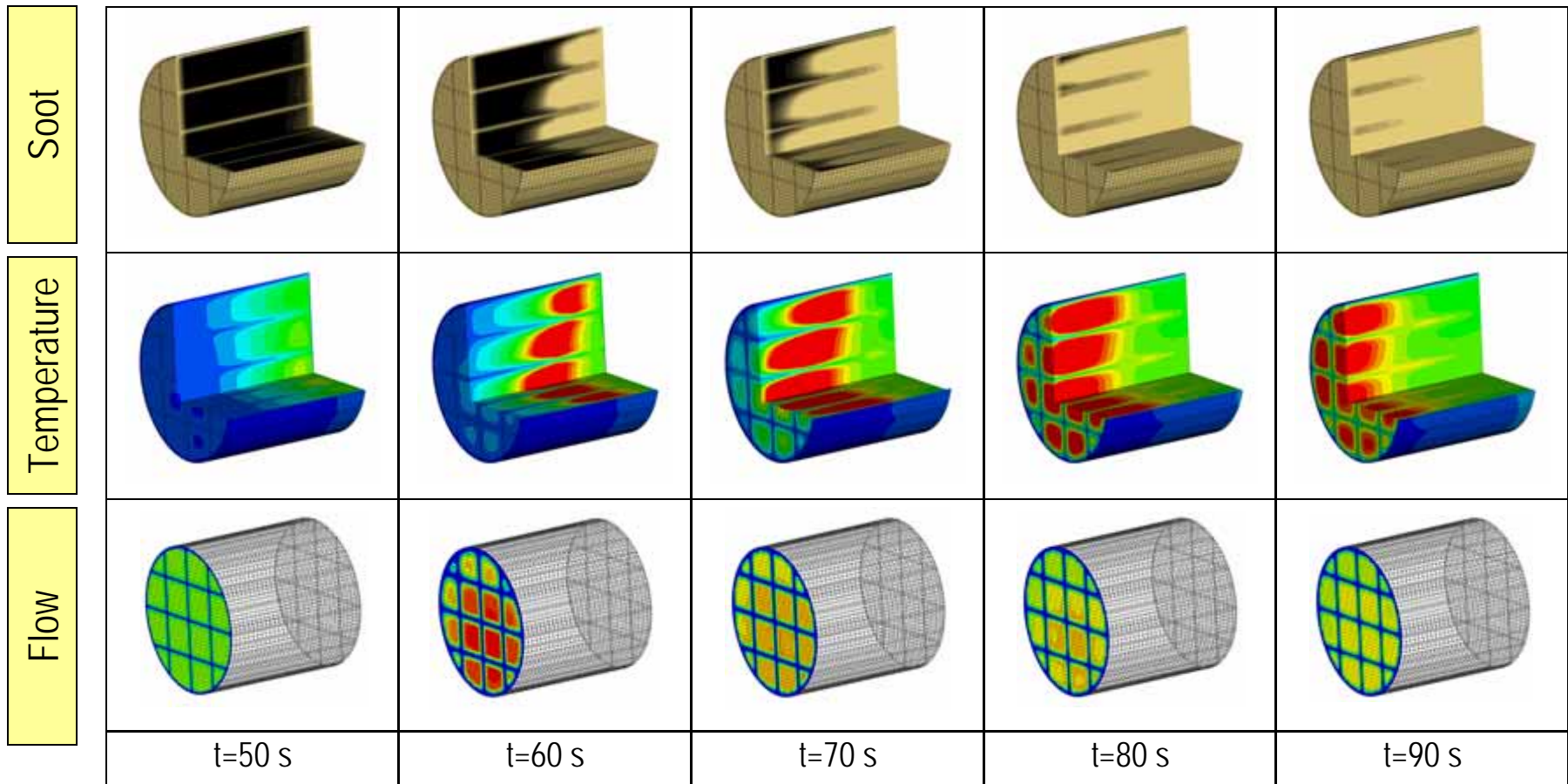
Flow

Stress analysis



# 3-d DPF regeneration simulation

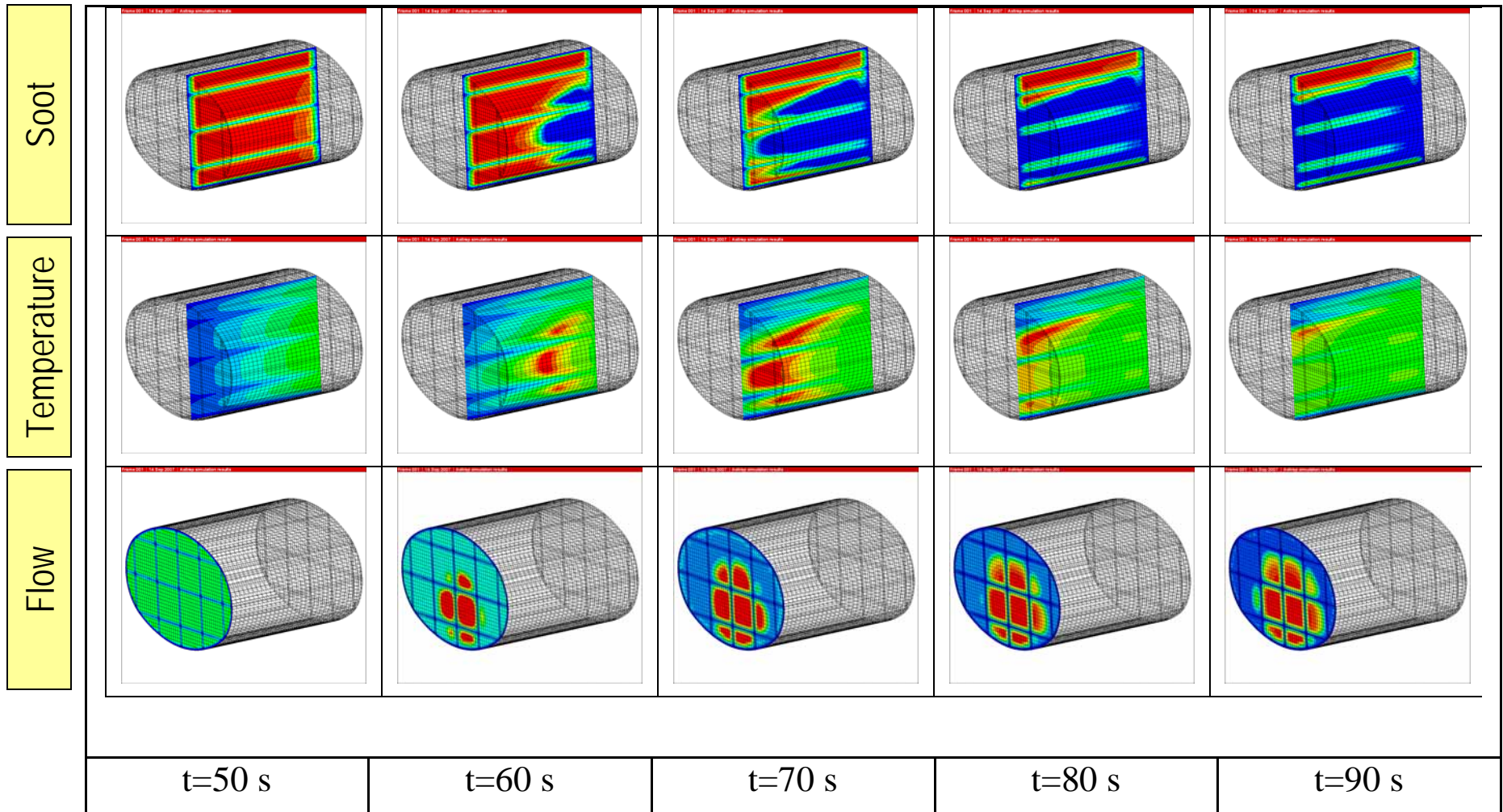
## Sources of "3-dimensionality"



**"3-d effects"**  
Heat losses, segmentation, asymmetric inlet temperature/flow, oval DPF geometry



# Oval geometries



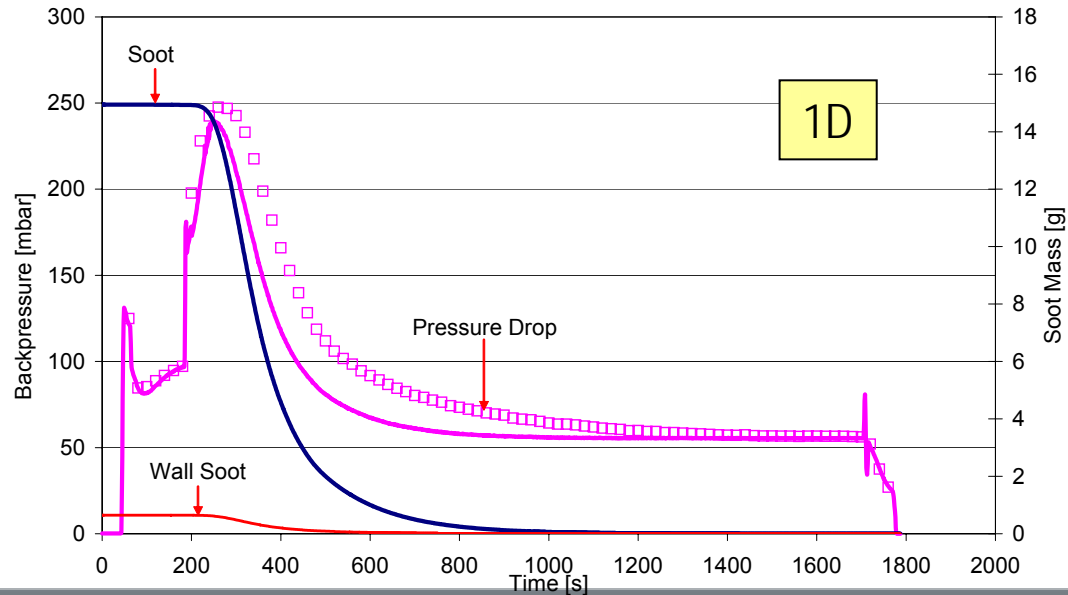
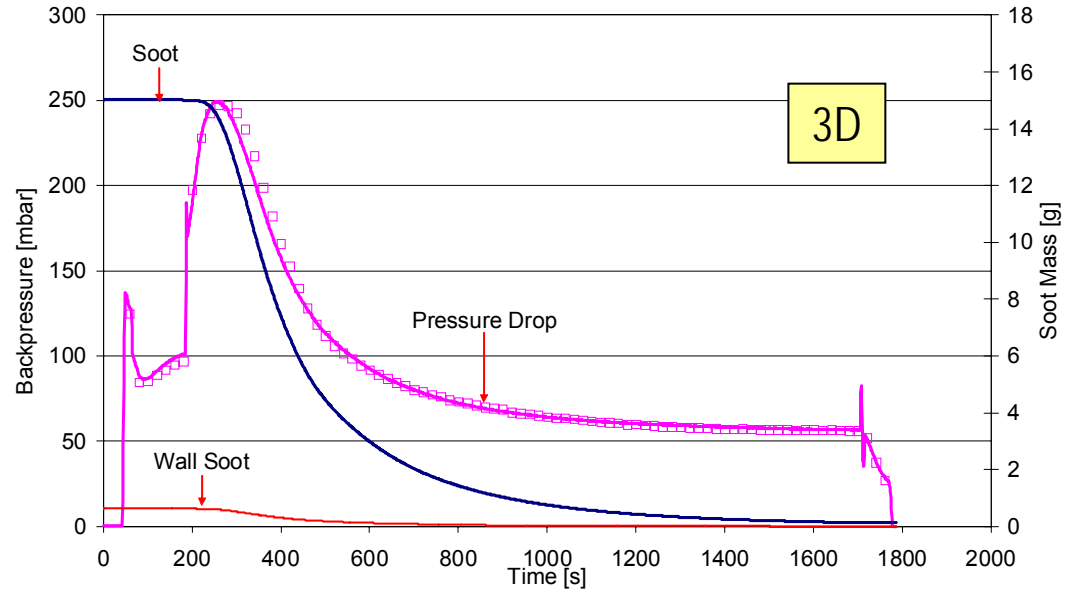
Regeneration simulations of oval filters with asymmetric flow profiles are completed with minimum CPU cost without CFD coupling



# Forced regeneration 3-d vs 1-d simulation results

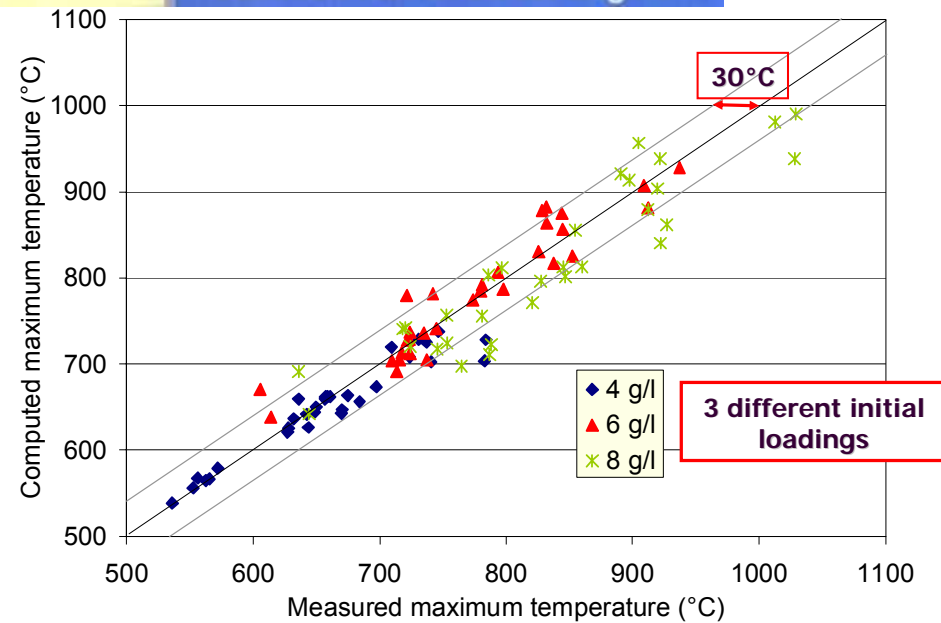
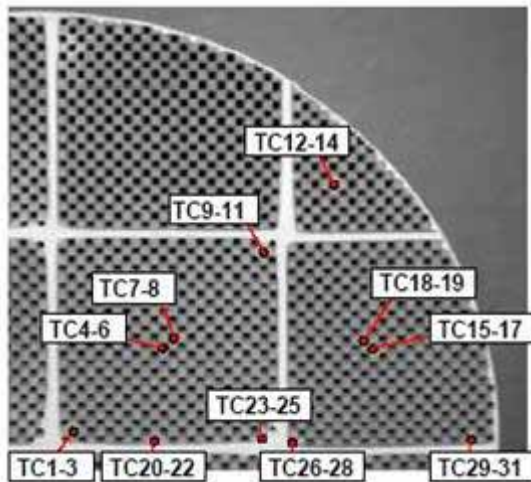
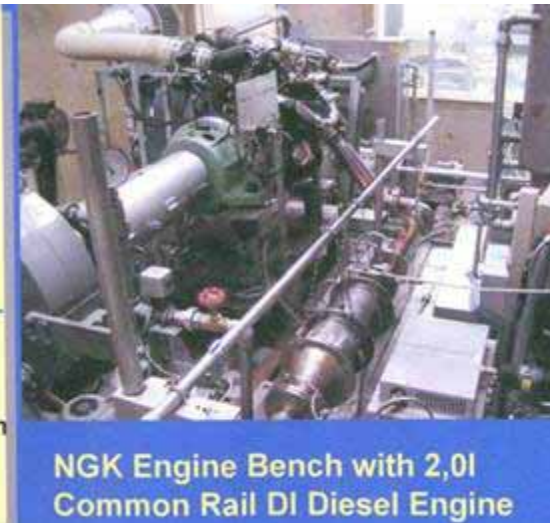
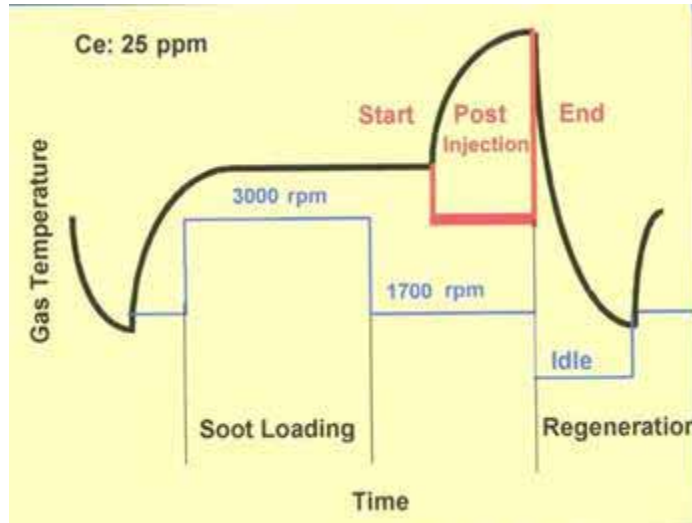


dots: measurement  
lines: simulation



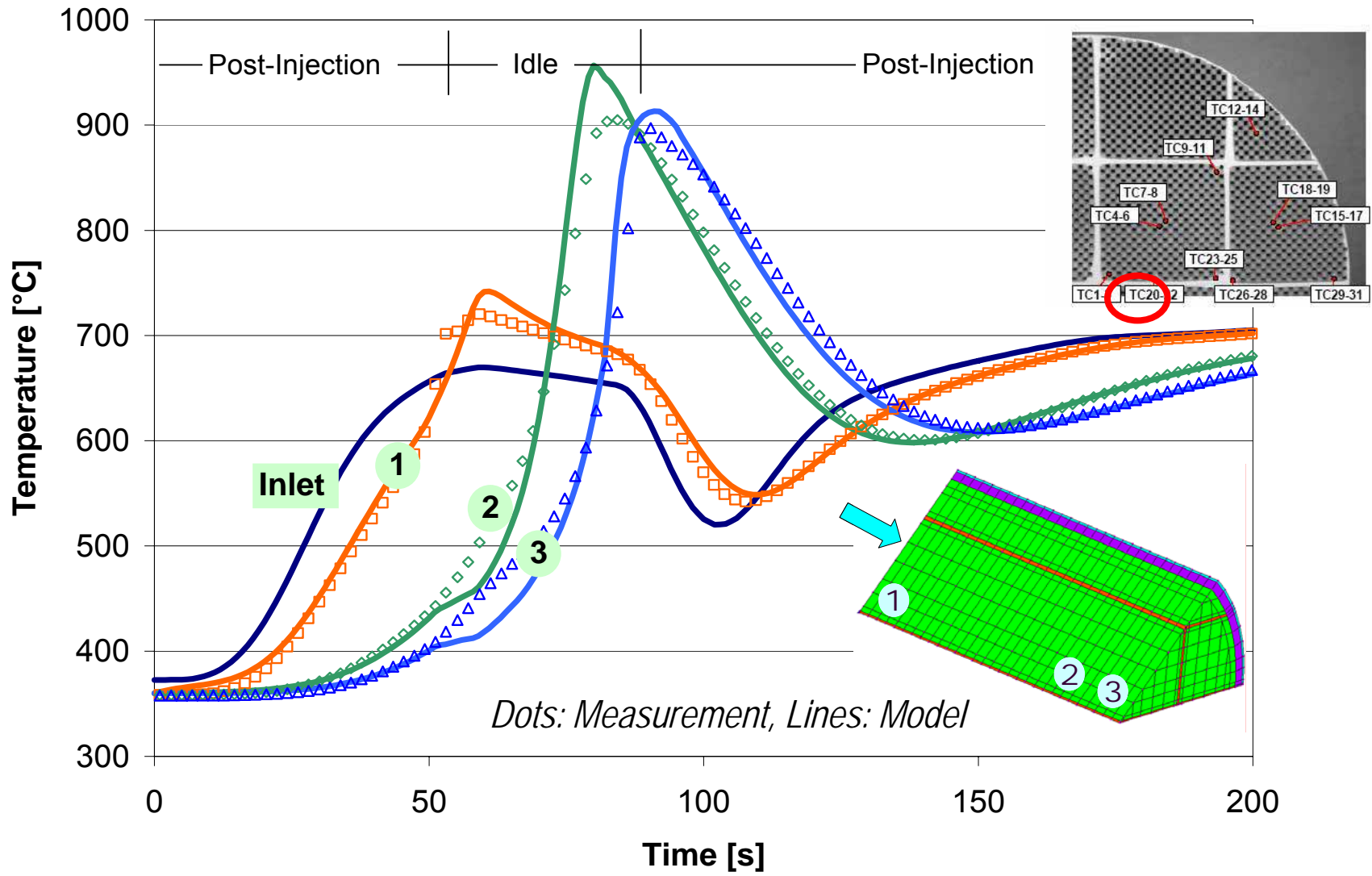


# Model validation vs experimental data (LAT & NGK: SAE 2005-01-0953)

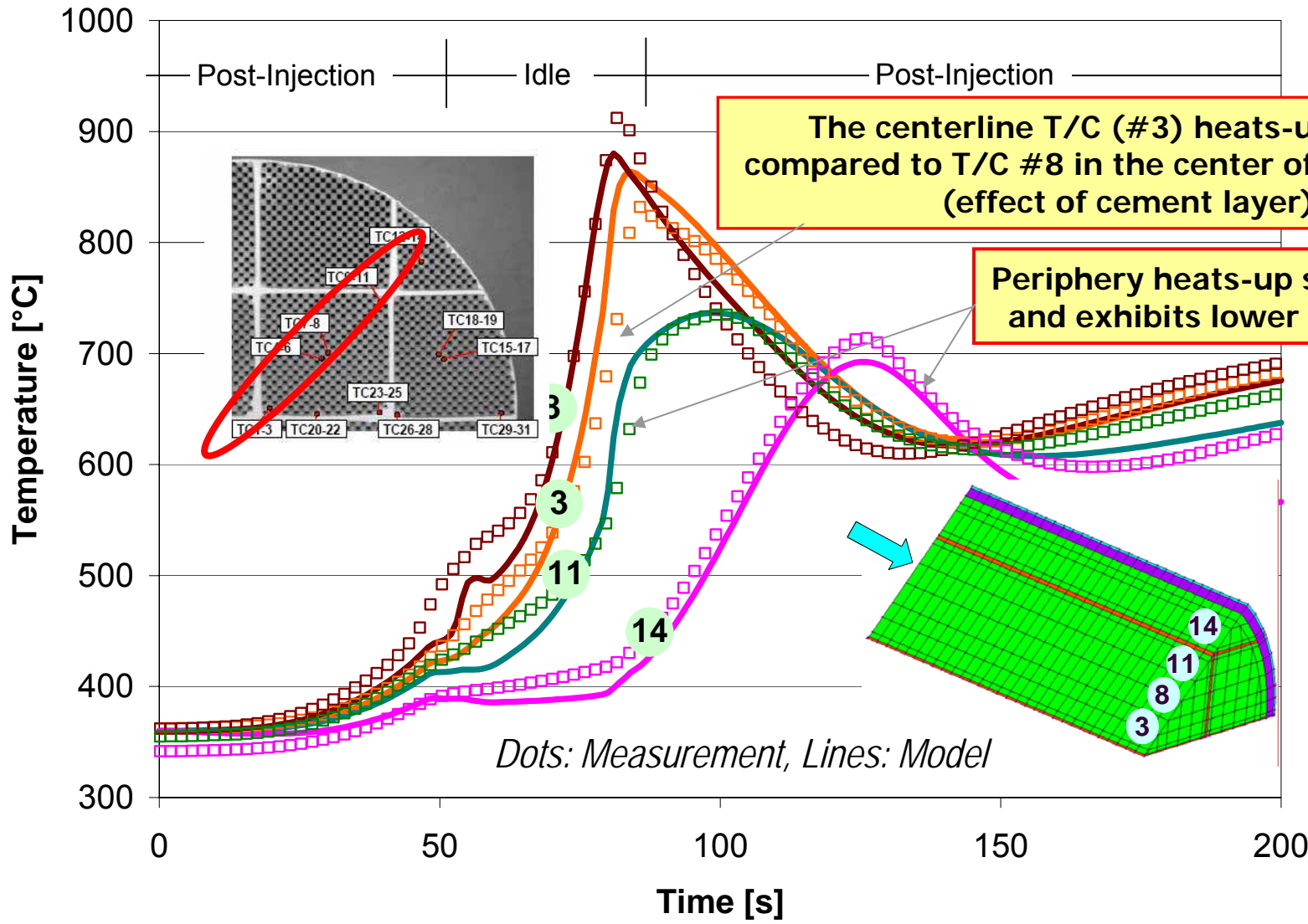


# Model validation – centerline channel

Initial soot loading: 8 g/l

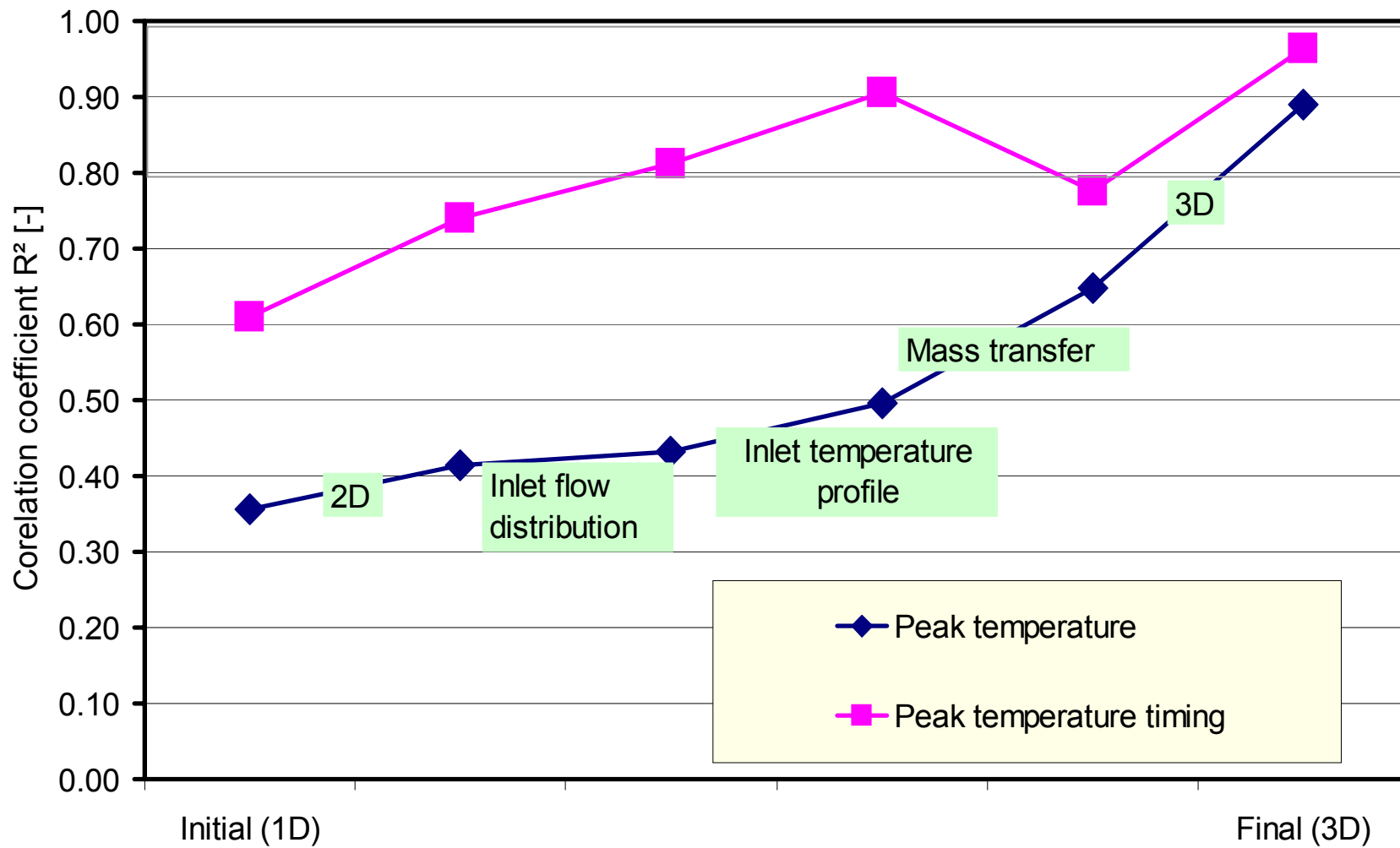


# Model validation – 8 g/l Filter exit – 45° plane



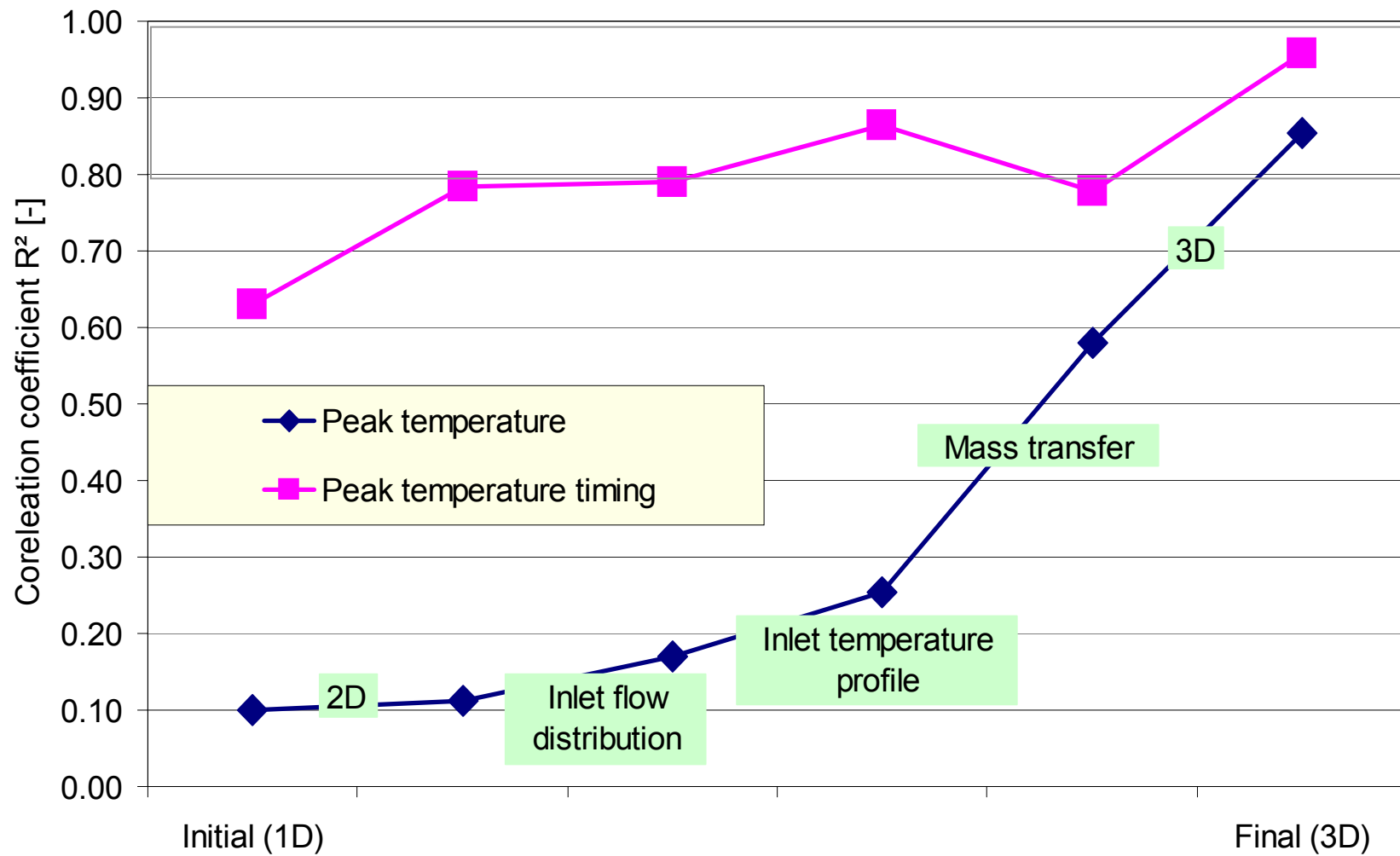


# Accuracy assessment FBC system - Initial soot loading: 6 g/l



# Accuracy assessment

## FBC system - Initial soot loading: 8 g/l



# Segmentation effects

Simulation results with same protocol, time=80 s

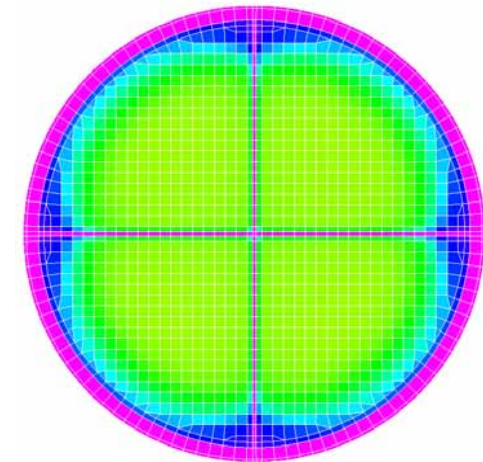
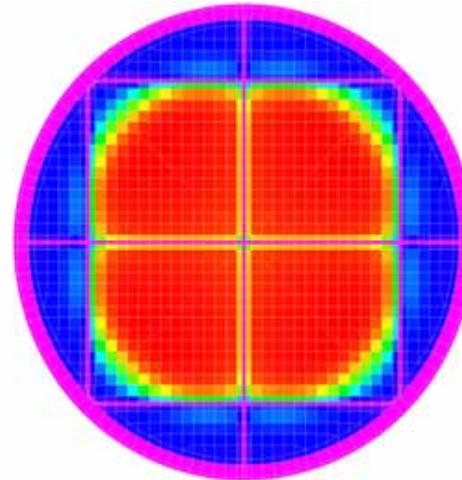
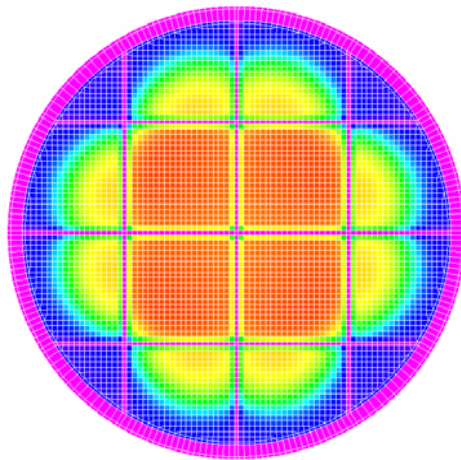


16 segments

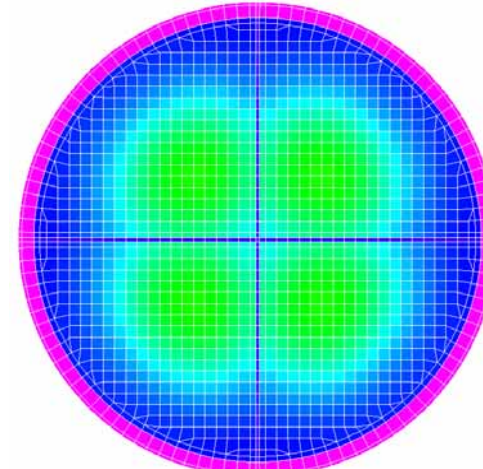
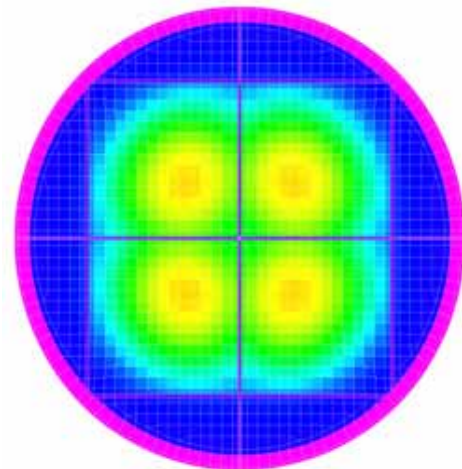
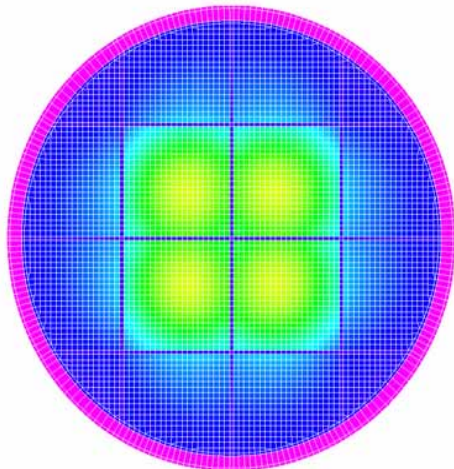
12 segments

4 segments

Flow rate (kg/m<sup>2</sup>s)



Exit temperature (°C)



# Stress analysis



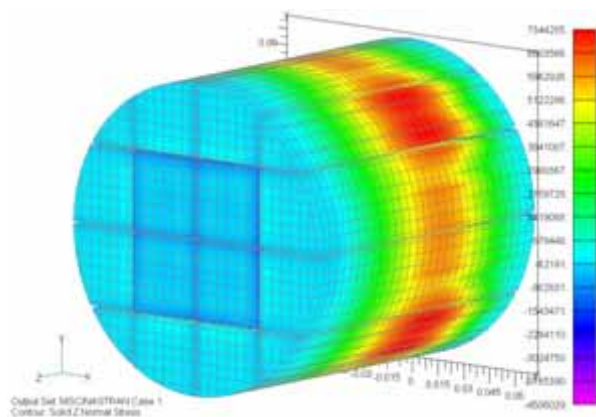
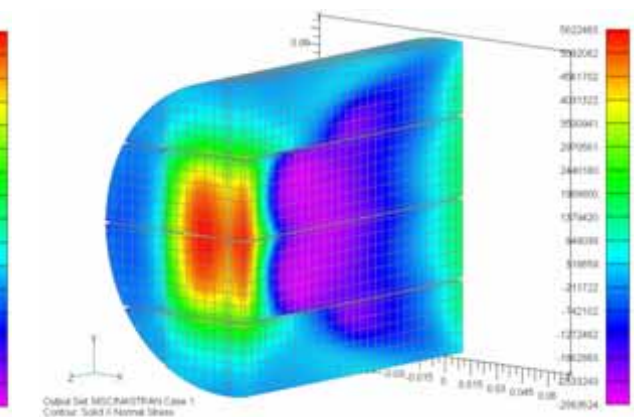
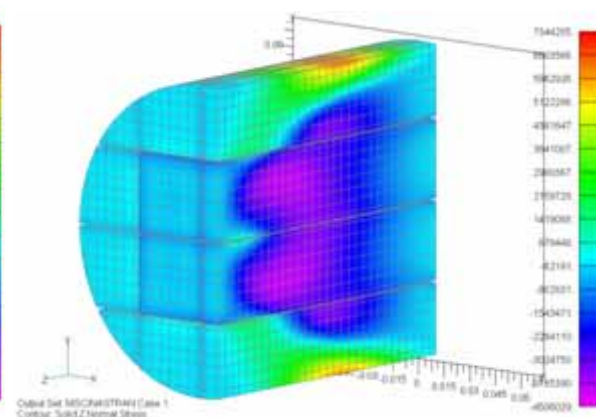
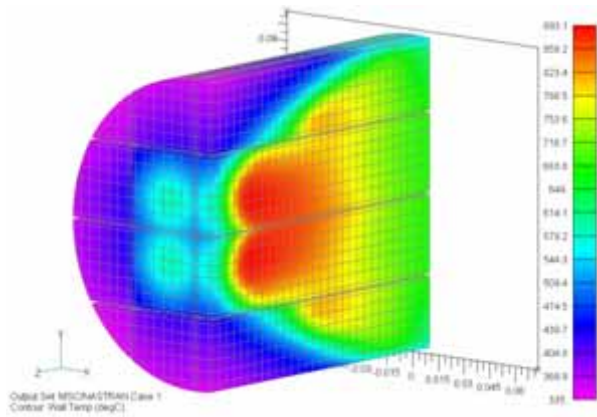
Axitrap™

Nastran™

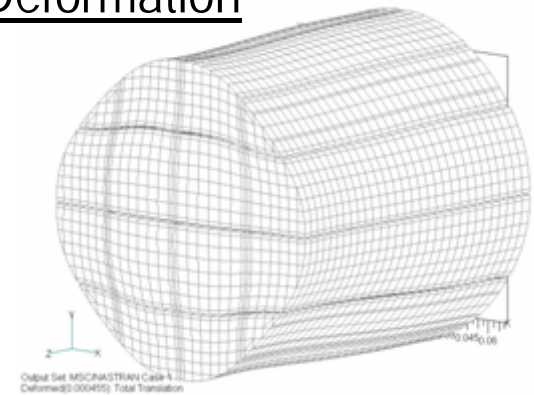
Temperature

$\sigma_z$

$\sigma_x$



Deformation



# DOC modeling

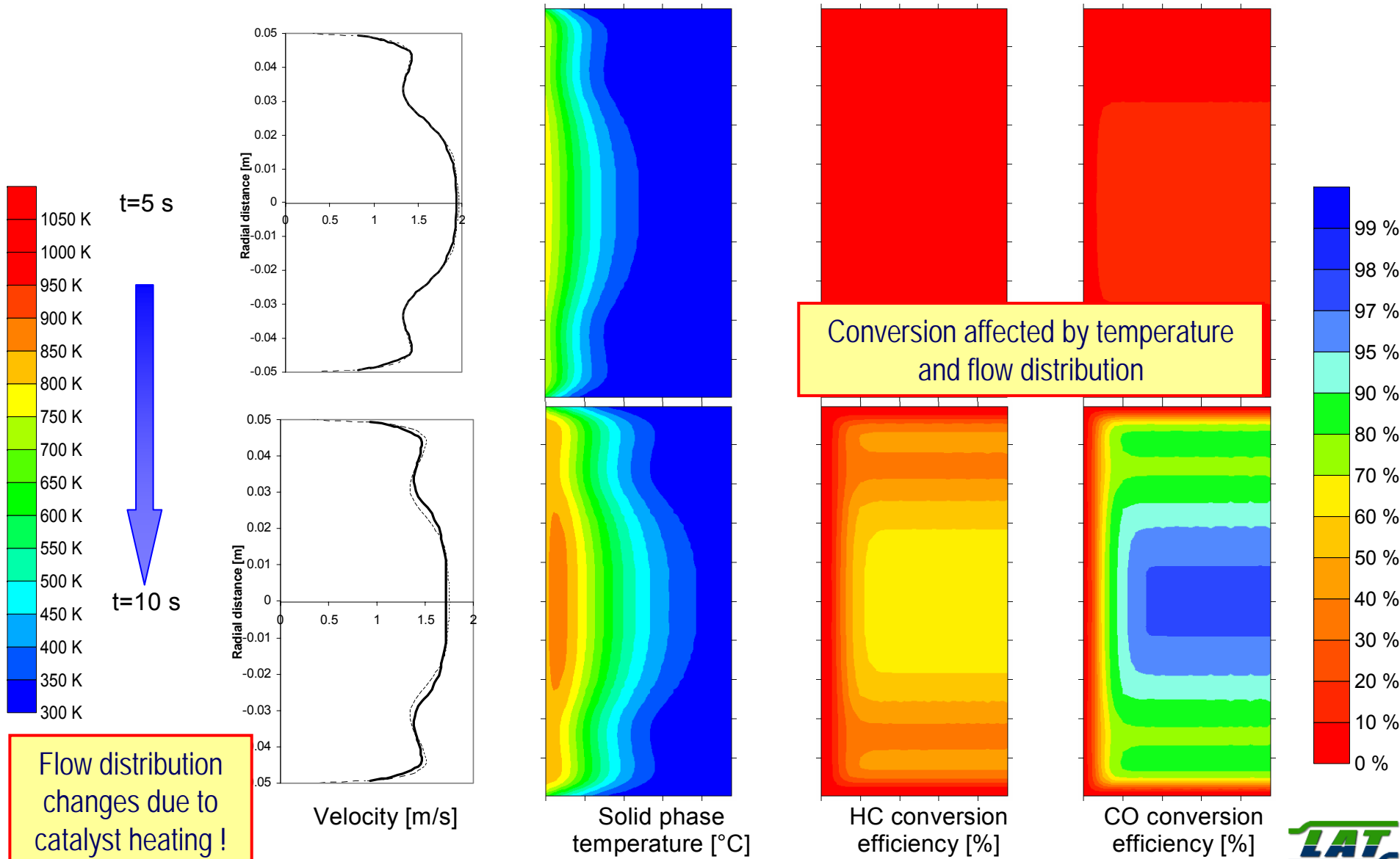
Multi-dimensional effects for the case of driving cycle performance prediction



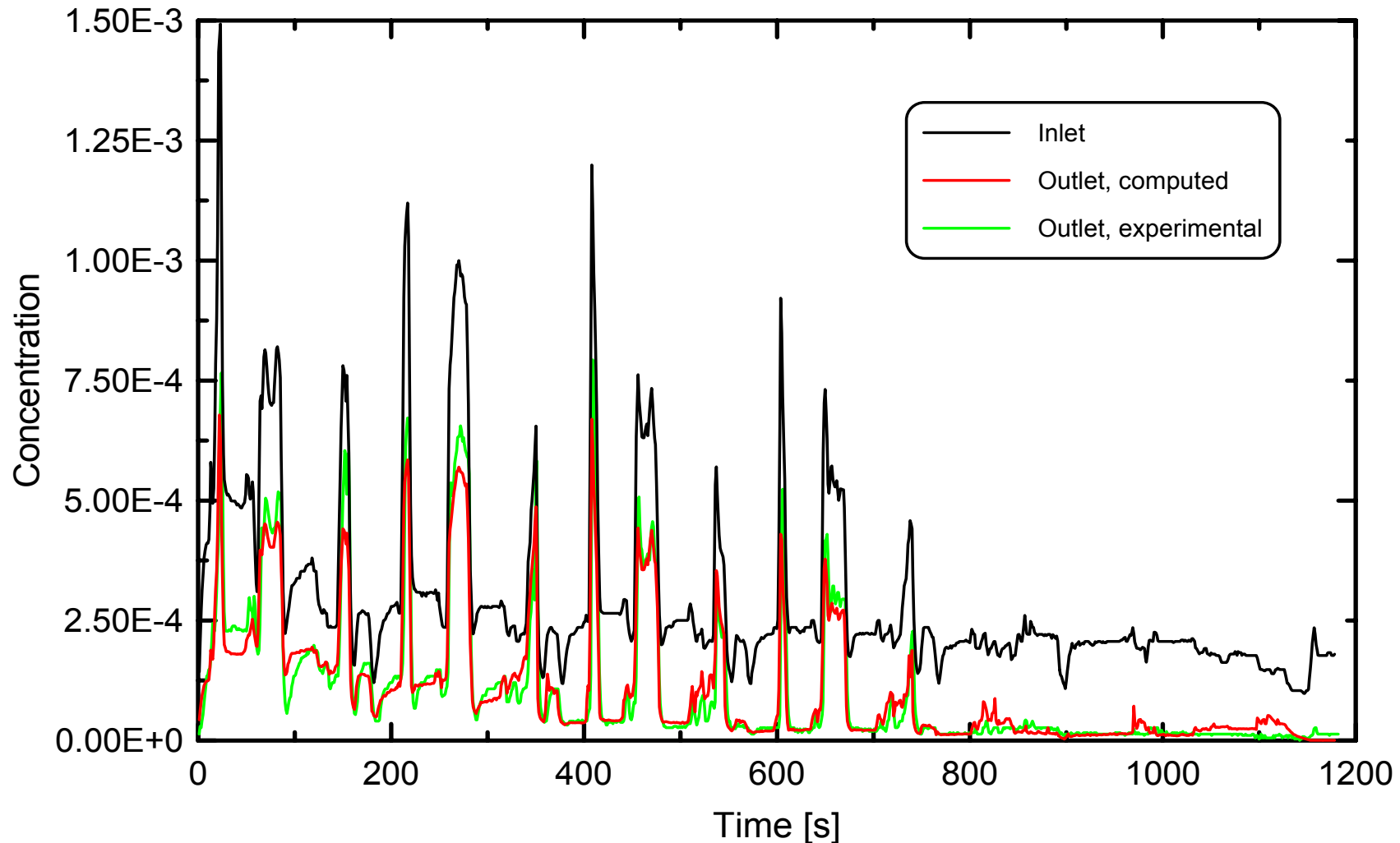


# 2-d effects

## Flow distribution effects during catalyst warm-up



# HC prediction instantaneous emissions



Pontikakis G. N., Koltsakis G. C., Stamatelos A. M., Noirod R., Agliany Y., Colas H., Versaevel Ph., Bourgeois C.:  
Experimental and Modeling Study on Zeolite Catalysts for Diesel Engines, Topics in Catalysis, 6/17, Nos. 1-4,  
September 2001, pp. 329-335.



	CO (efficiency [%])				HC (efficiency [%])			
	I	II	III	total	I	II	III	total
<i>Measurement</i>	11.4	32.1	99.1	42.1	45.3	55.1	91.8	62.5
<i>Model results</i>	2.5	32.5	99.6	40.3	46.6	56.7	86.9	62.3
<b>Assumptions</b>								
Uniform flow distribution	2.7	38.2	100	<b>43.4</b>	46.9	64.6	93.0	<b>68.1</b>
HC adsorption neglected	2.4	31.5	99.5	39.7	<b>3.8</b>	34.4	87.1	<b>41.3</b>
2 HC species (propene/propane)	2.4	32.2	99.6	40.1	<b>7.3</b>	50.6	83.7	<b>49.6</b>
H <sub>2</sub> O adsorption neglected	2.9	35.5	99.5	41.9	46.8	59.0	87.1	63.6

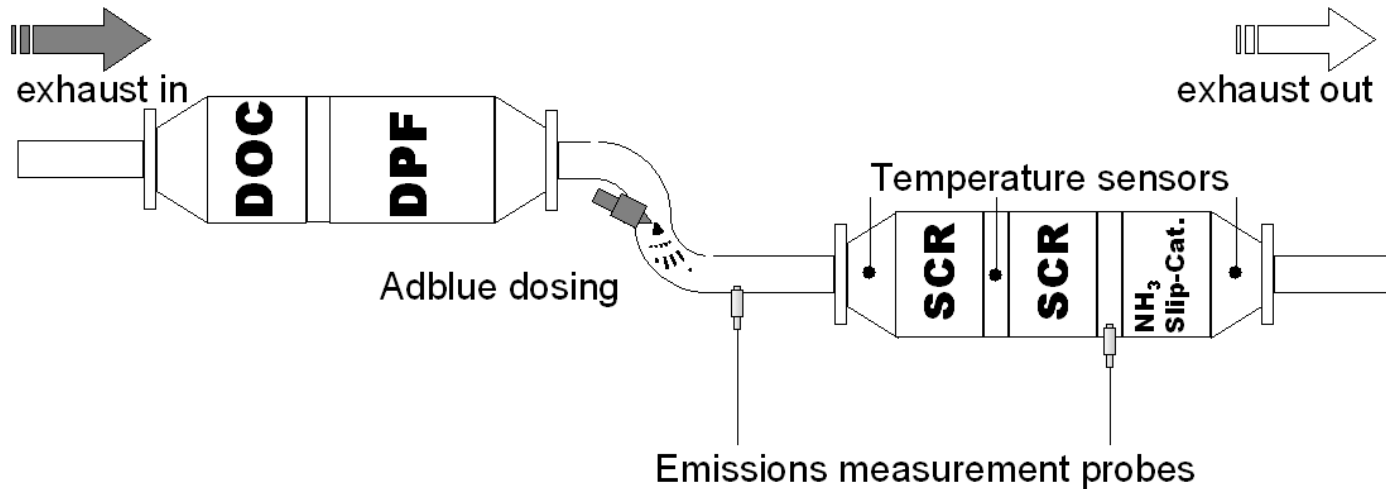
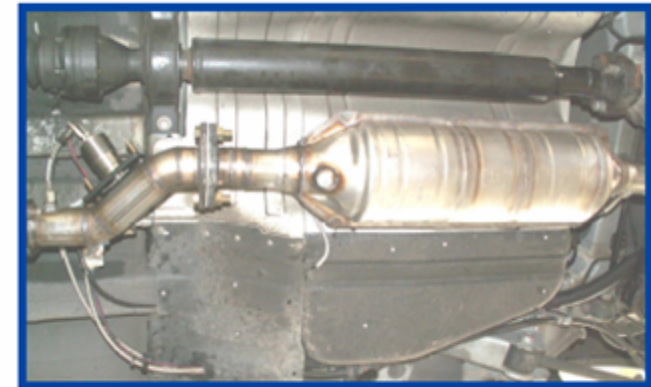
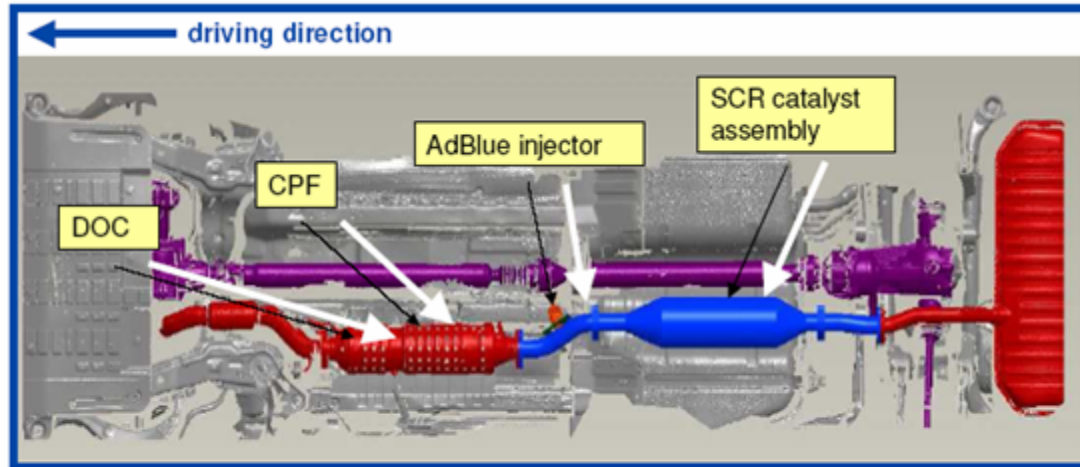
Pontikakis G. N., Koltsakis G. C., Stamatelos A. M., Noirot R., Agliany Y., Colas H., Versaevel Ph., Bourgeois C.:  
 Experimental and Modeling Study on Zeolite Catalysts for Diesel Engines, Topics in Catalysis, 6/17, Nos. 1-4,  
 September 2001, pp. 329-335.



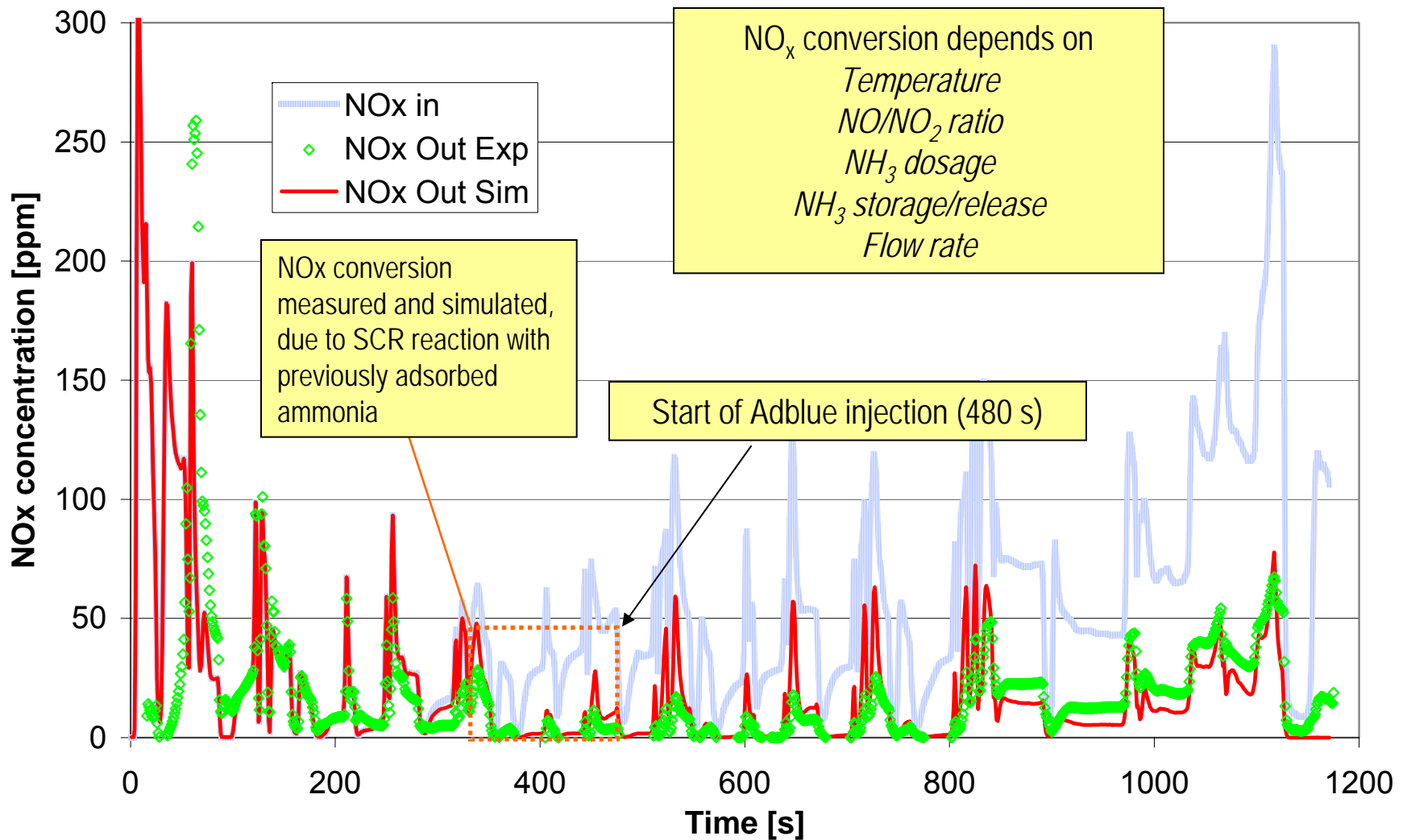
# SCR modeling



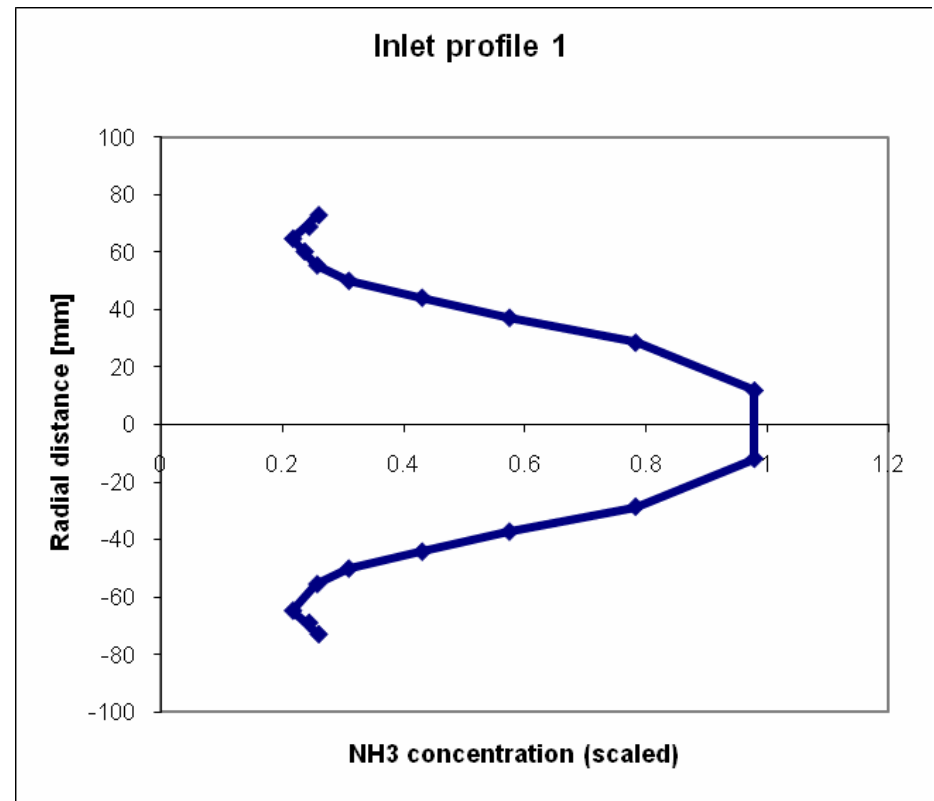
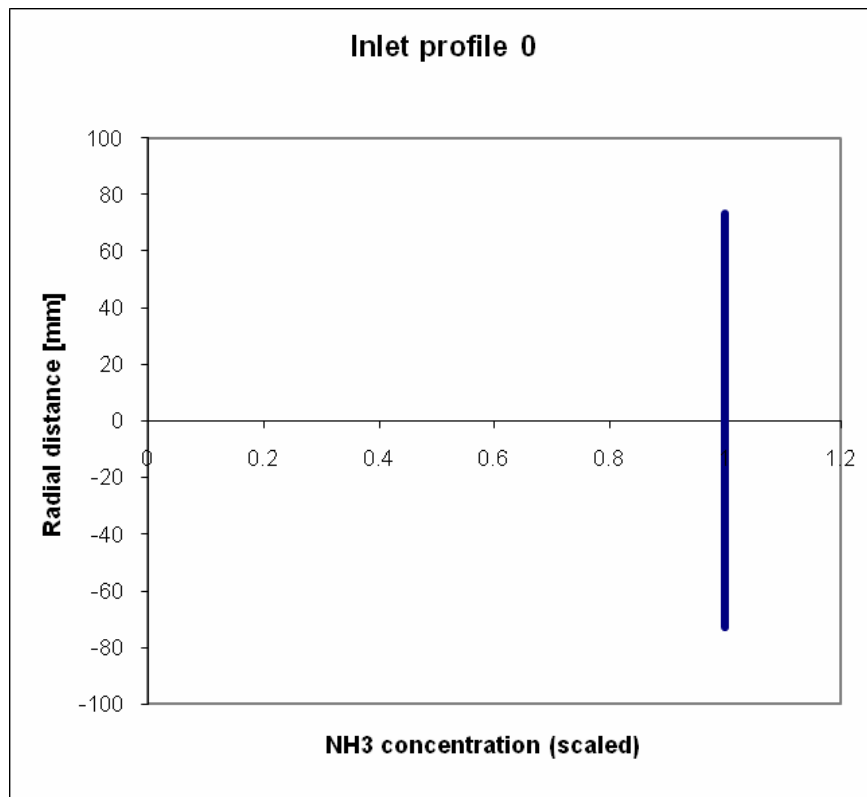
# Exhaust system layout



# SCR catalyst simulation NEDC NO<sub>x</sub> predictions



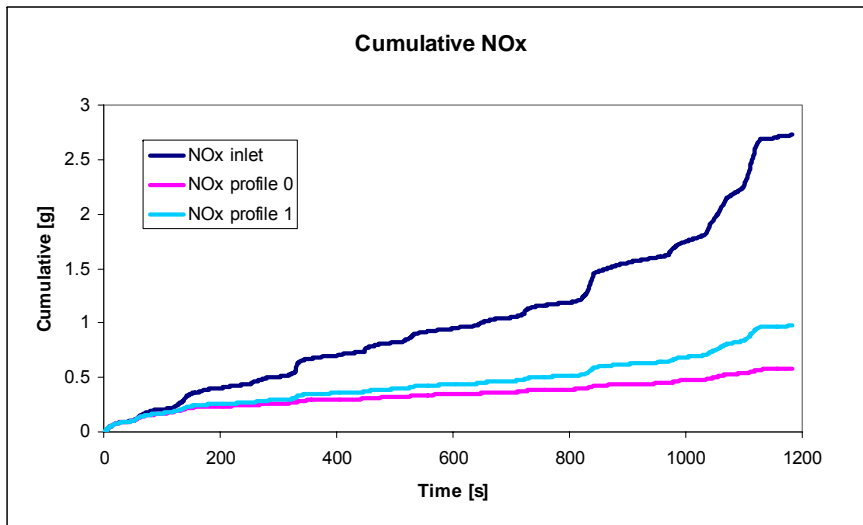
# Effect of NH<sub>3</sub> inlet profile Simulation study



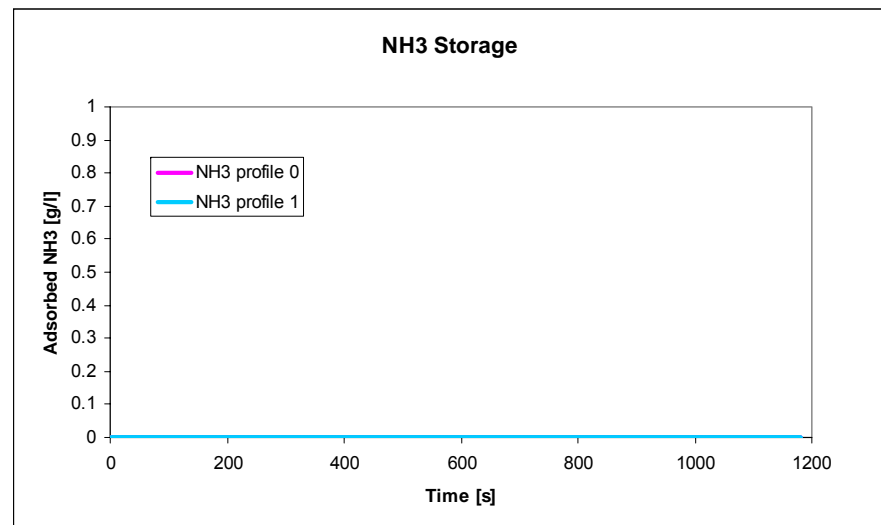
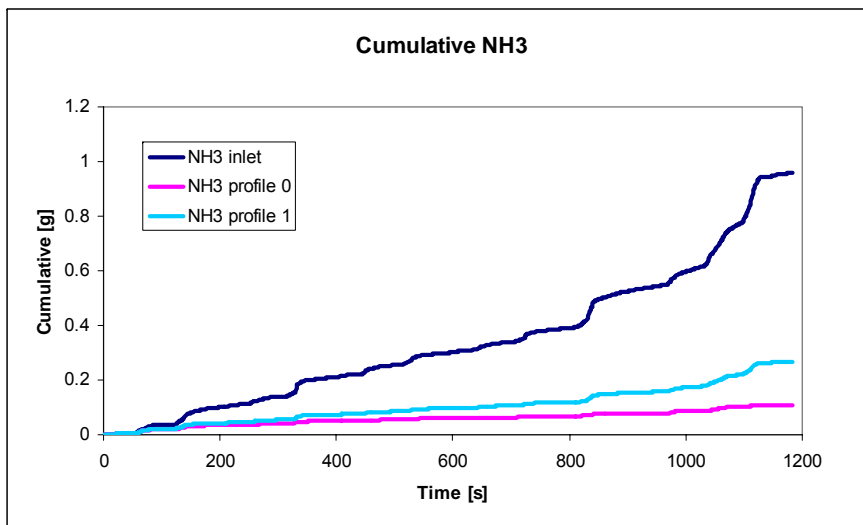
Simplifying assumptions:  
NH<sub>3</sub>/NO<sub>x</sub>=1, only when T<sub>in</sub>>190 °C  
*Uniform inlet flow/NO<sub>x</sub> distribution*



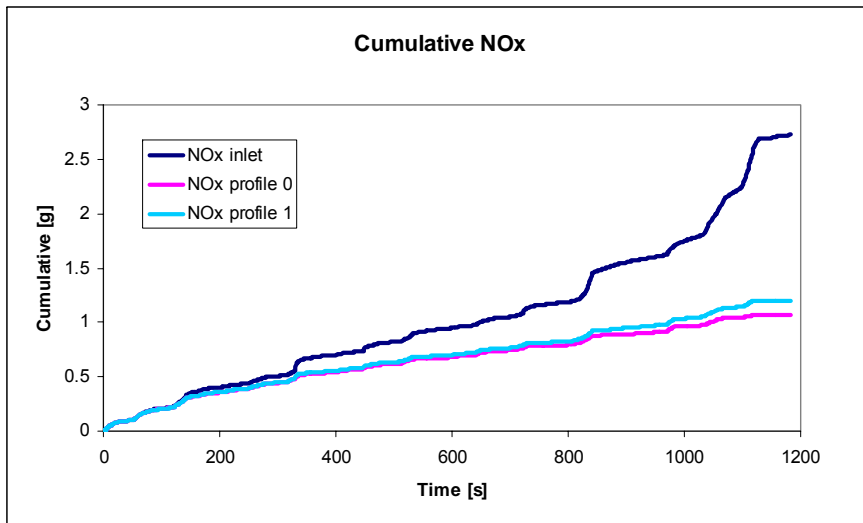
# Assumption: zero NH<sub>3</sub> storage capacity



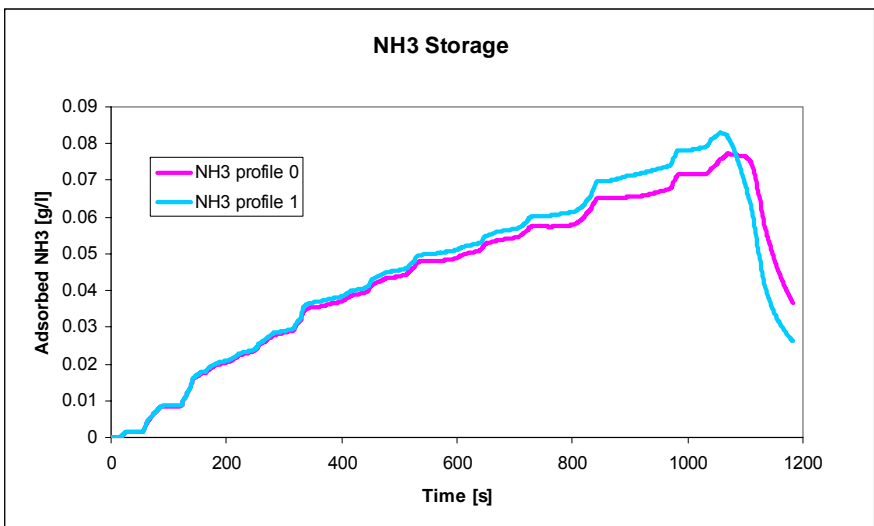
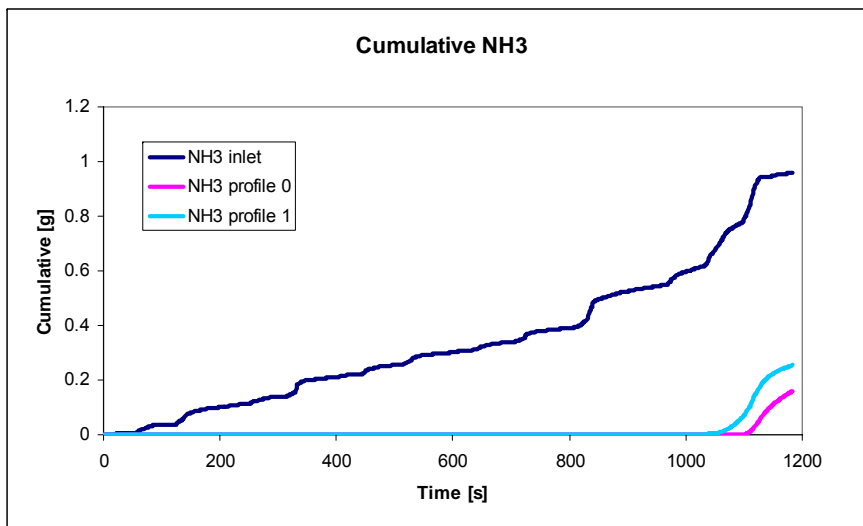
As expected, the non-uniform NH<sub>3</sub> distribution is strongly reflected in the SCR de-NOx performance and NH<sub>3</sub> slip



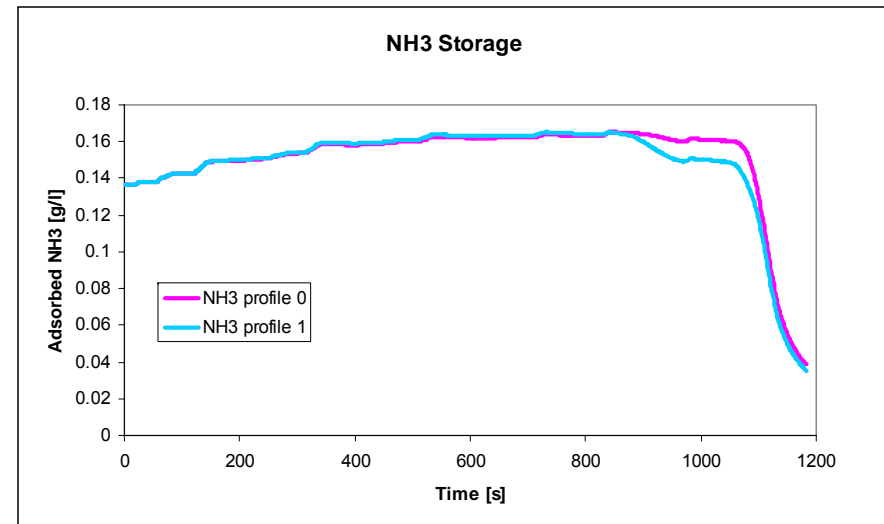
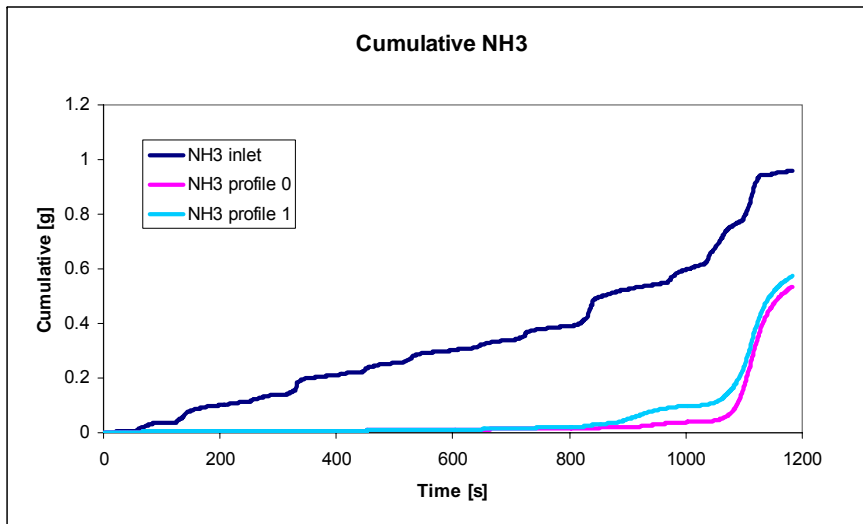
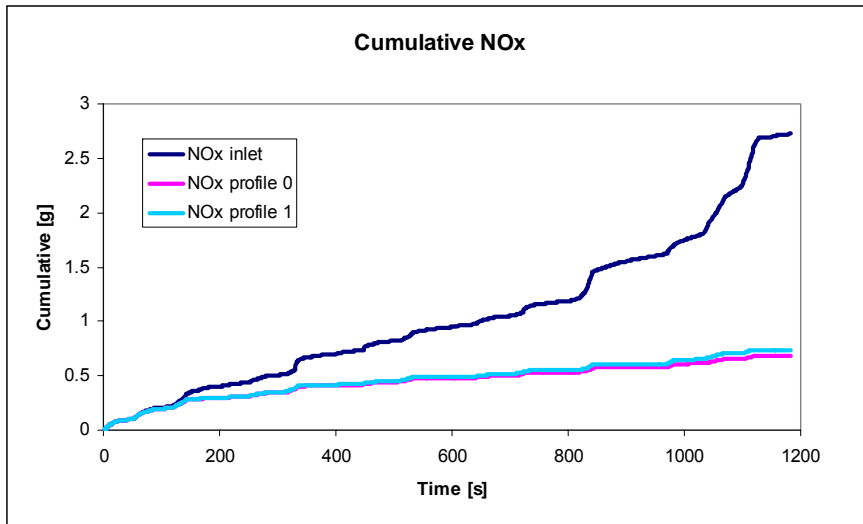
# Assumption: zeolite-based with $\text{NH}_3$ storage capacity, *no pre-adsorbed $\text{NH}_3$*



The  $\text{NH}_3$  adsorption capacity partially “relieves” the detrimental effects of non-uniform distribution



# Assumption: zeolite-based with $\text{NH}_3$ storage capacity, with pre-adsorbed $\text{NH}_3$






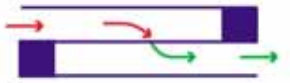




# Complete exhaust line simulation





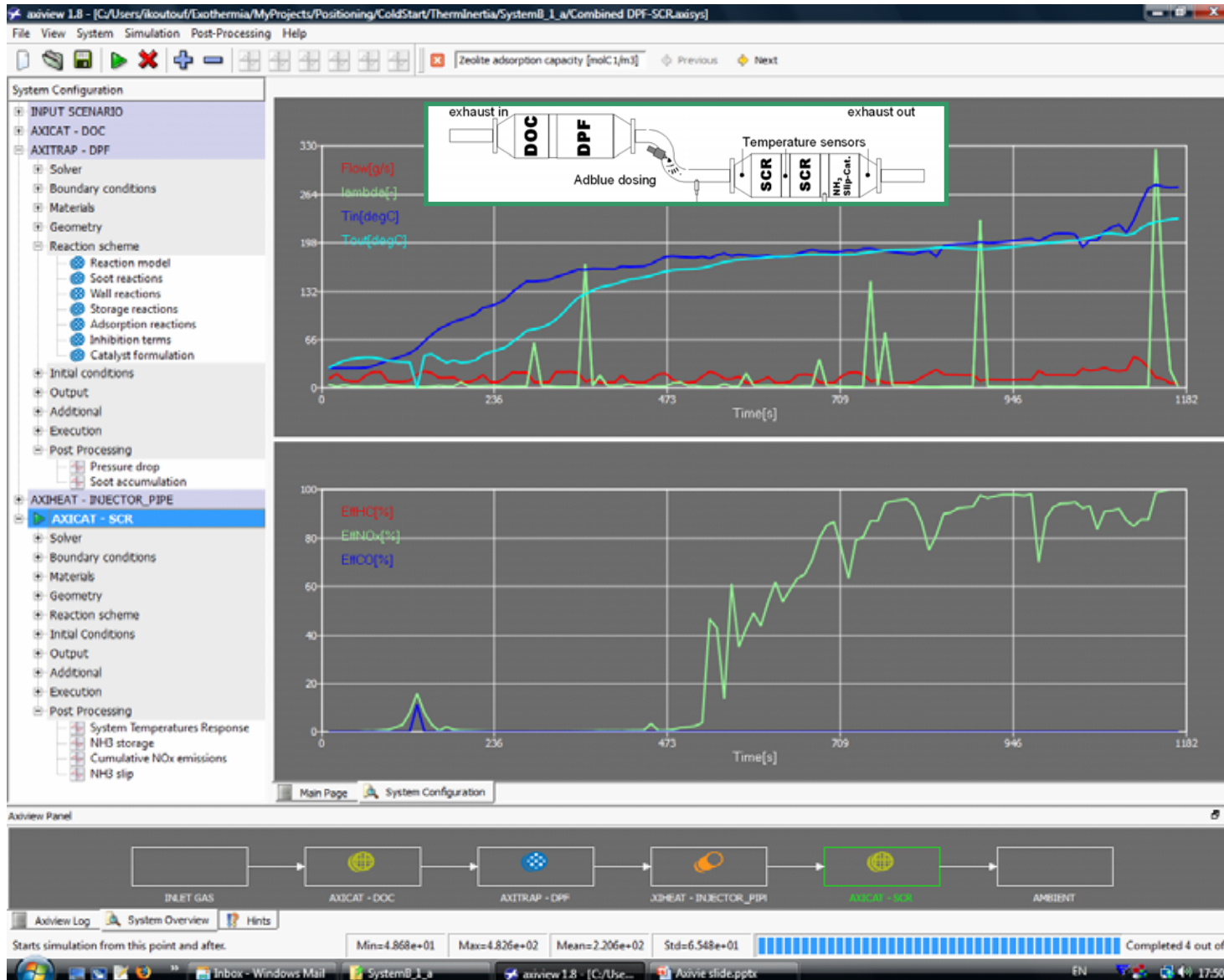
# Simulation modules



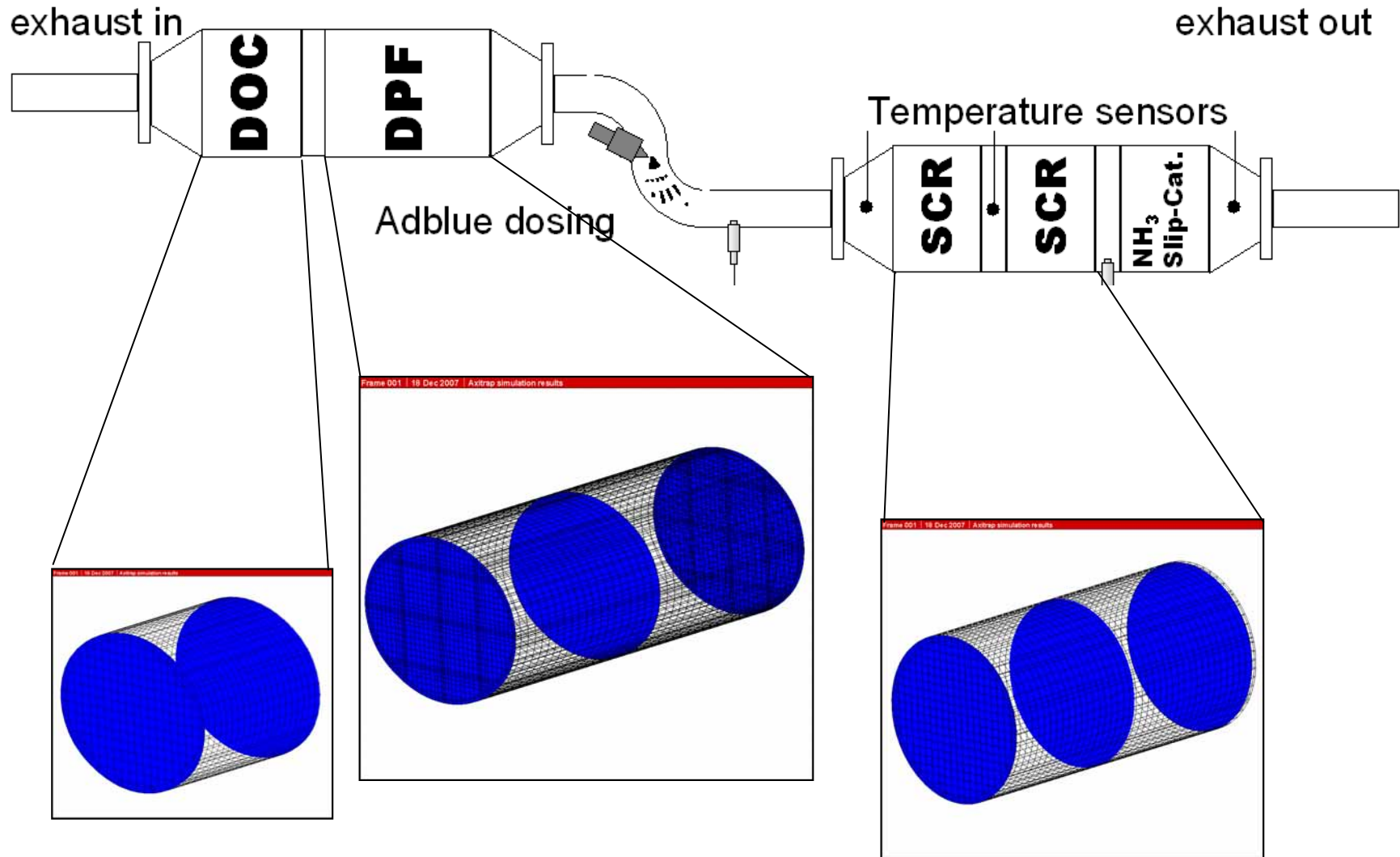
axisuite						
software module	functionality / reactor type	3-way catalyst	diesel oxidation catalyst	lean NO <sub>x</sub> trap	selective catalytic reduction	diesel particulate filter
	 flow-through	✓	✓	✓	✓	n/a
	 wall-flow	n/a	✓	✓	✓	✓
	 deep-bed	n/a	✓	✓	✓	✓
	 exhaust pipe	single-wall	double-wall	insulating material	flanges	reacting flow



# System simulation



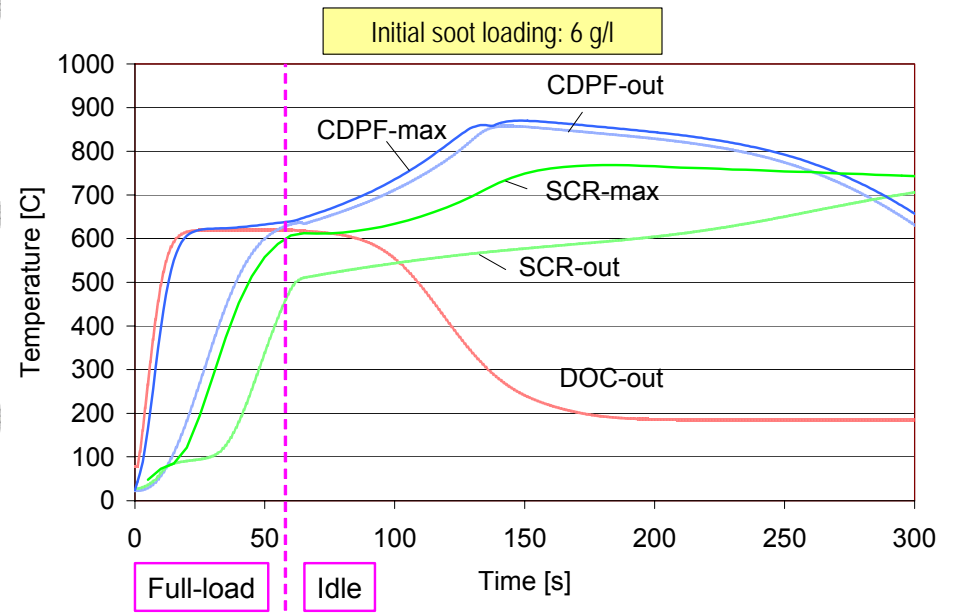
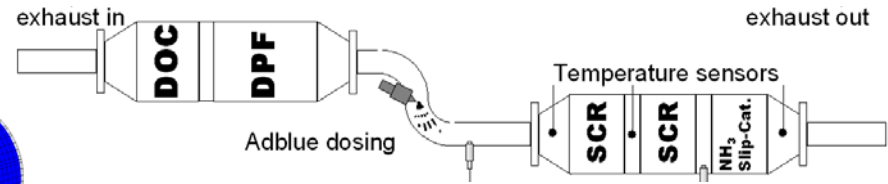
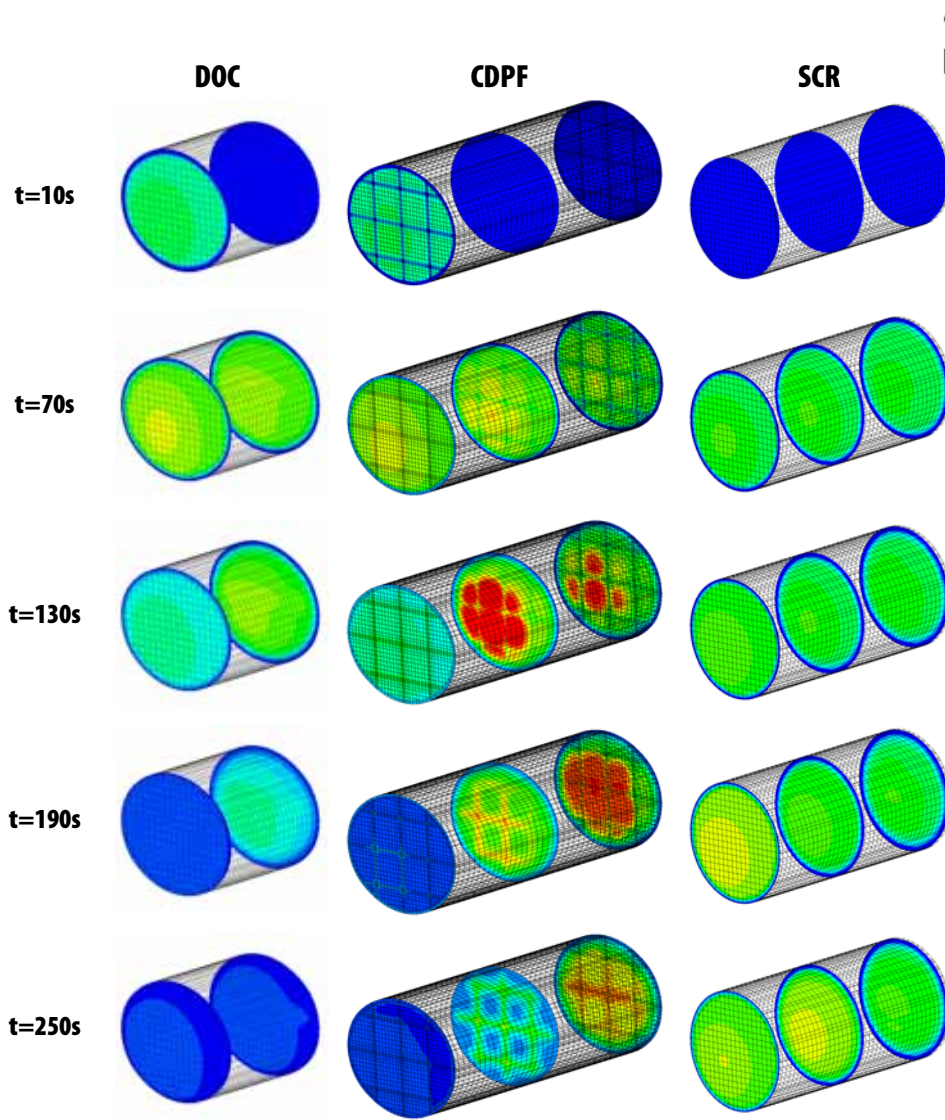
# Complete system simulation: Soot limit with respect to SCR thermal loading



Koltsakis et al., FAD Conference-2007 (LAT-IAV GmbH-Exothermia)



# 3-d system temperature simulation "Worst-case" DPF regeneration case



Test data for model input from IAV engine bench (SAE 2007-01-1127)

Koltsakis et al., FAD Conference-2007 (LAT-IAV GmbH-Exothermia)

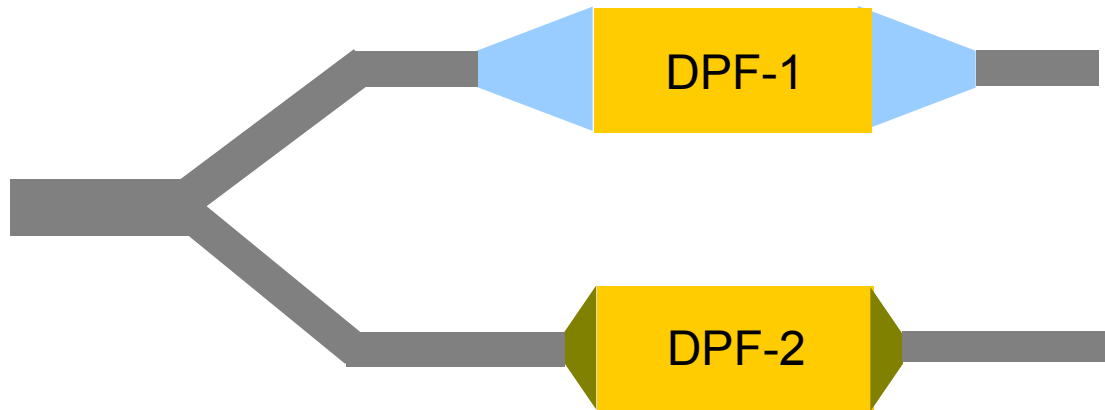






# Illustrative example: 2 branches

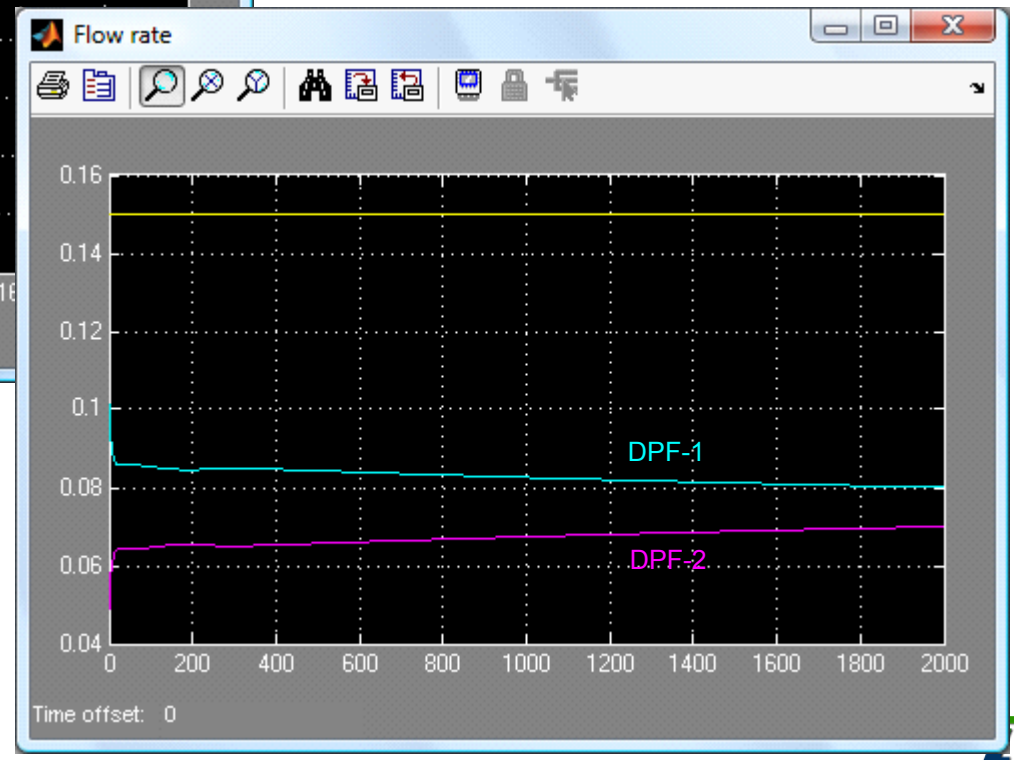
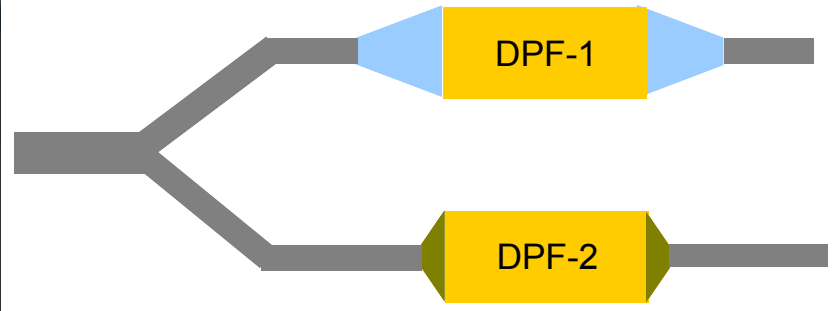
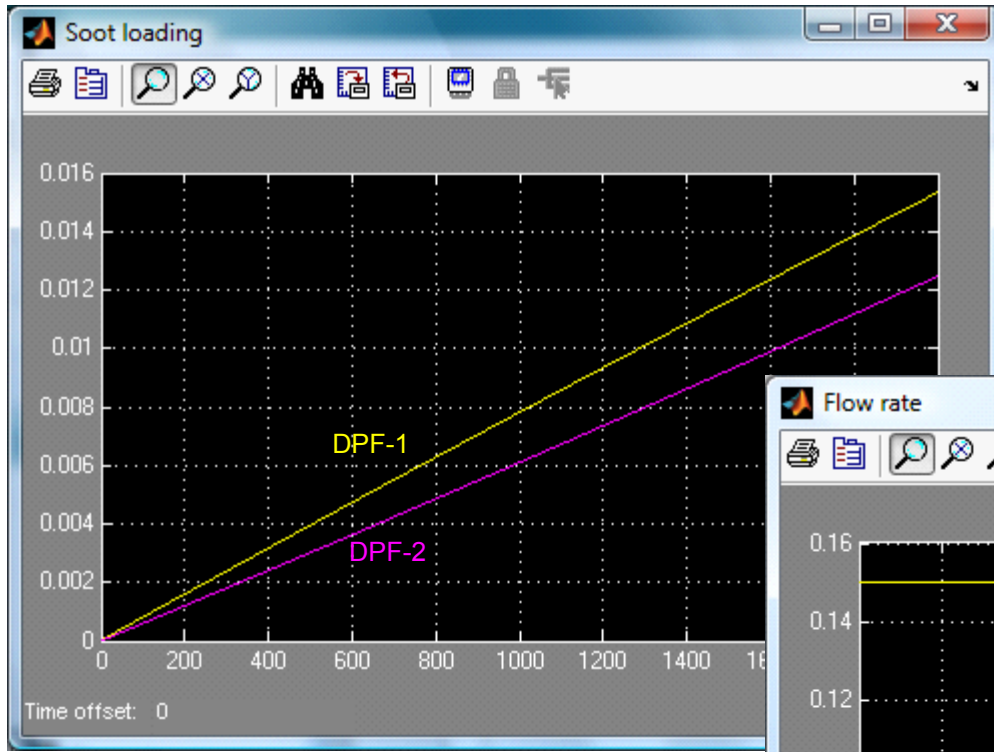
## Identical DPFs, different flow conditions



- ⚡ As a simple illustration case, we consider two DPFs with different cones. DPF-1 cone ensures uniform flow. DPF-2 cones result in significant maldistribution.
- ⚡ How will the flow and soot be distributed during loading?
- ⚡ Will there be any differences during regeneration?

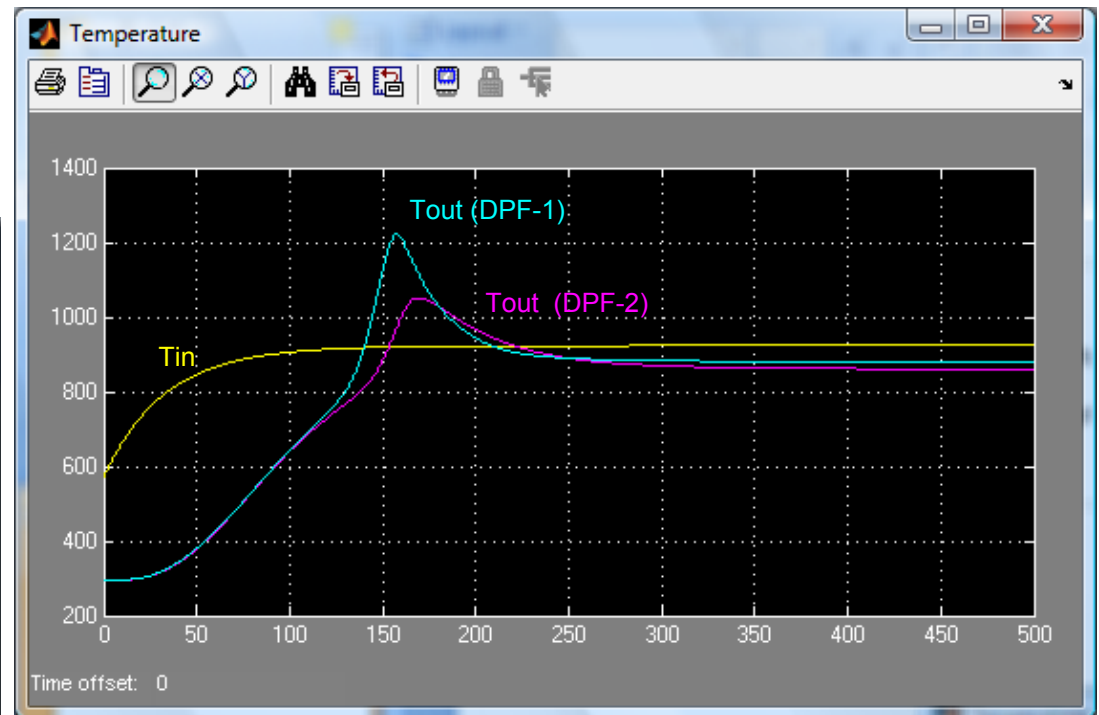
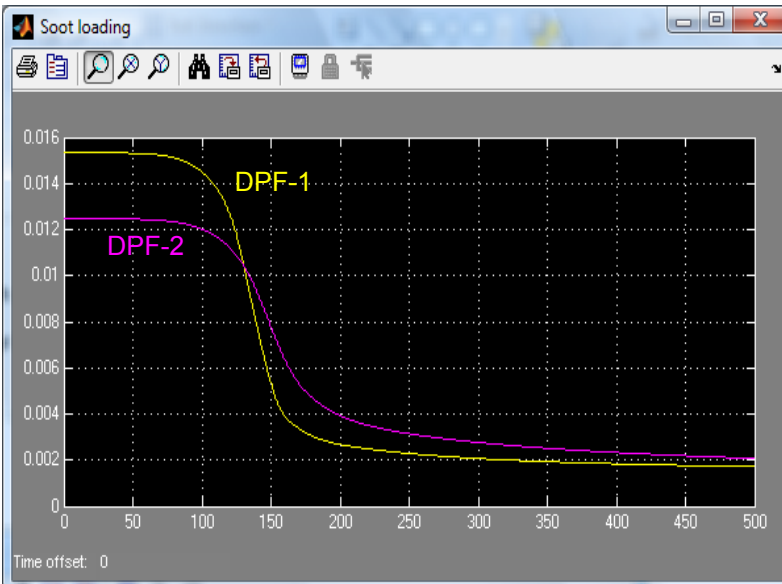
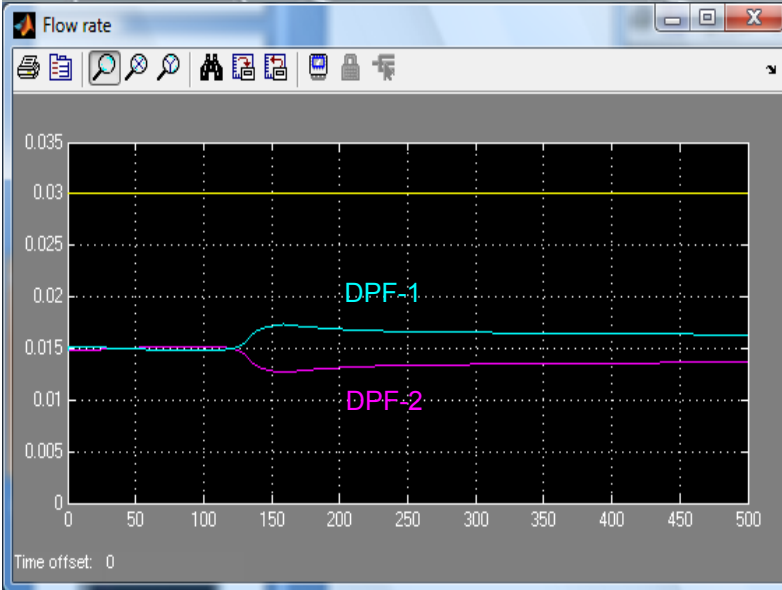
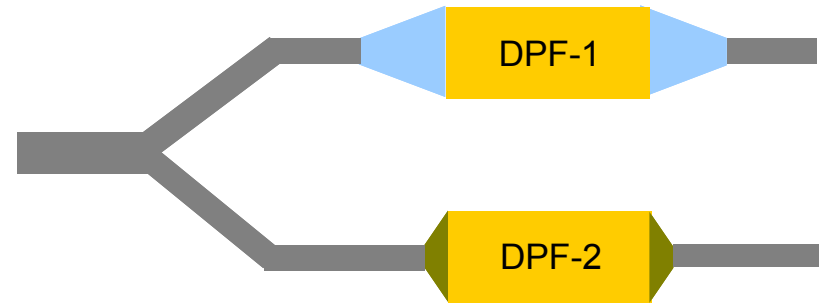


# Flow division and soot accumulation during loading mode





# Parallel filters Regeneration simulation



- ⚡ Depending on the application the detail of modeling – number of model dimensions has to be correctly identified.
- ⚡ For the case of DPF modeling
  - intra-wall dimension is important for filtration/pressure drop and catalyzed reactions modeling
  - 2-d and 3-d DPF discretization is necessary for regeneration modeling
- ⚡ Flow-through catalyst modeling
  - 2-d and 3-d modeling is necessary to account for flow/heat maldistribution
  - For SCR applications, multi-dimensional modeling is crucial for  $\text{NH}_3$  calculations
- ⚡ Parallel systems should be modelled concurrently, to account for the interactions.

# Thank you very much for your attention!

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[www.exothermia.com](http://www.exothermia.com)

