



LABORATORY OF APPLIED THERMODYNAMICS
ARISTOTLE UNIVERSITY THESSALONIKI

**10th CLEERS
Workshop
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4-way Catalyst Modeling in Wall- Flow and Deep-bed Substrates

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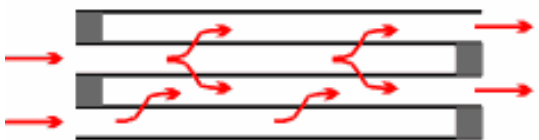
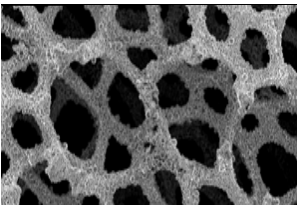
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Introduction

4-way catalysis

- The term “3-way” catalysis first introduced for closed-loop control stoichiometric engines (CO, HC, NO_x)
- Until recently, “2-way” catalysis was adequate for lean burn engines (CO, HC)
- Nowadays and in the near future
 - ◆ Most diesel engines will be equipped with “4-way” systems
 - ◆ Lean burn gasoline engines currently employing “3-way” catalysis. PM aftertreatment may also arise.
- “4-way” catalysis may involve
 - ◆ Multiple reactors (e.g. DOC+DPF+SCR/LNT)
 - ◆ Single reactor (e.g. DPNR)

Reactor concepts – application areas

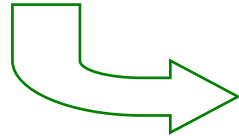
	DOC	LNT	SCR	DPF
<p>Flow-through honeycomb, incl. "turbulent substrates"</p> 	Yes	Yes	Yes	No ~30% efficiency with "turbulent" substrates
<p>Wall-flow honeycomb</p> 	Yes	Yes	?	Yes
<p>"Deep-bed" (e.g. fiber, foam)</p> 	Yes At development stage	?	?	Yes ~90% efficiency with metal foams

Content of presentation

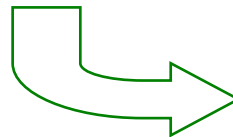
Development and application of modeling tools for
System design optimization
Engine/exhaust system calibration

For each possible system (chemistry/reactor concept combination)

Governing Equations



Parameter Calibration



Experimental Validation

Integrated exhaust line simulation

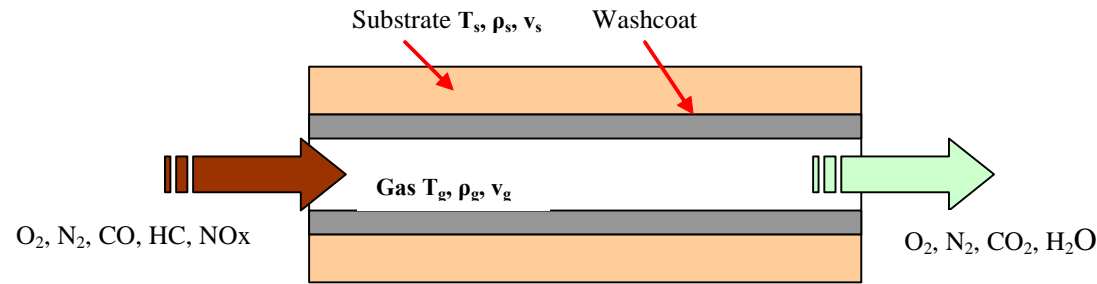


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Flow-through catalyst

Model equations

Basic 1-D model equations



Gas energy balance

$$\rho_g v_g \frac{\partial T_g}{\partial x} = -h \cdot \left(\frac{S}{\varepsilon} \right) \cdot (T_g - T_s)$$

Gas species balance

$$\frac{\partial (v_g c_g)}{\partial x} = -k_j \cdot \left(\frac{S}{\varepsilon} \right) \cdot (c_{g,j} - c_{s,j})$$

Transient energy balance

$$\underbrace{\rho_s C_{p,s}}_{\text{Solid heat capacity}} \frac{\partial T_s}{\partial t} = \underbrace{\lambda_s}_{\text{Conduction}} \frac{\partial^2 T_s}{\partial x^2} + \underbrace{h \left(\frac{S}{1-\varepsilon} \right)}_{\text{Convection}} (T_g - T_s) - \underbrace{\frac{1}{1-\varepsilon} \sum_{k=1}^{n_k} \Delta H_k R_k}_{\text{Reaction heat}}$$

Solid heat capacity

Conduction

Convection

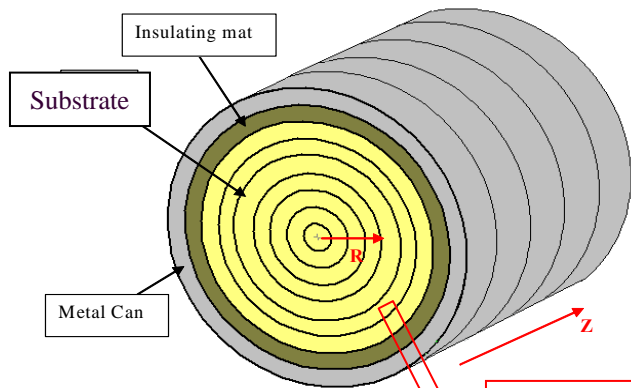
Reaction heat

$$\frac{\rho_g}{M_g} k_j \left(\frac{S}{\varepsilon} \right) (c_{g,j} - c_{s,j}) = R_j$$

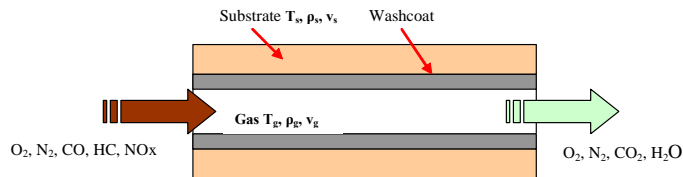
Mass-transfer rate = reaction rate

2-D axi-symmetric modeling

Basic concept



Simulation of discrete "representative" channels



Derivation of heat source terms (convection, exothermy)

Energy balance

$$\rho_s \cdot C_{p,s} \frac{\partial T_s}{\partial t} = \lambda_{s,z} \frac{\partial^2 T_s}{\partial z^2} + \lambda_{s,r} \frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial T_s}{\partial r} \right) + S$$

Heat capacity

Axial heat conduction

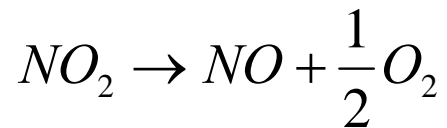
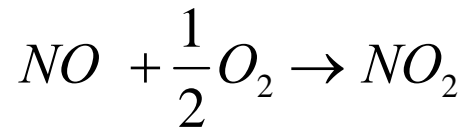
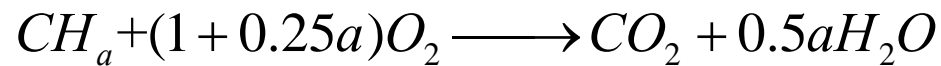
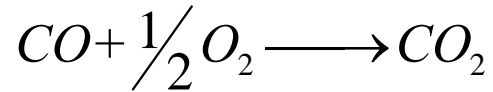
Radial heat conduction



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DOC modeling

Basic oxidation reactions on Precious Metals NO-NO₂ chemical equilibrium



L-H reaction rates with inhibition terms

$$R_1 = \frac{A_1 \cdot e^{-E_1/RT} \cdot c_{CO} \cdot c_{O_2}}{G_2}$$

$$R_2 = \frac{A_1 \cdot e^{-E_1/RT} \cdot c_{CH} \cdot c_{O_2}}{G_2}$$

$$R_5 = \frac{A_5 \cdot e^{-E_5/RT} \cdot c_{NO} \cdot c_{O_2} \cdot Eq_5}{G_5}$$

$$R_6 = \frac{A_6 \cdot e^{-E_6/RT} \cdot c_{NO} \cdot c_{O_2} \cdot Eq_6}{G_5}$$

NO/NO₂ thermodynamics are taken into account by the terms Eq_i

$$Eq_i = 1 - K_p(T) \cdot \frac{\prod c_{s,prod}^n}{\prod c_{s,react}^m}$$

Chemical equilibrium constant
(function of temperature)

Negative value of a parameter Eq_i suggests that the reaction is not thermodynamic possible and the reaction rate in the model is zeroed.

Adsorption – desorption modeling

➤ Competitive HC, H₂O, NH₃ adsorption on zeolite

- ◆ $H_2O \rightleftharpoons (H_2O)_{ads}$
- ◆ $C_xH_y \rightleftharpoons (C_xH_y)_{ads}$ (toluene)
- ◆ $C_xH_y \rightleftharpoons (C_xH_y)_{ads}$ (decane)
- ◆ $NH_3 \rightleftharpoons (NH_3)_{ads}$

Adsorption model Dubinin-Radushkevich isotherm

- The equation of the DR isotherm gives the adsorbed mass as function of temperature and partial pressure.

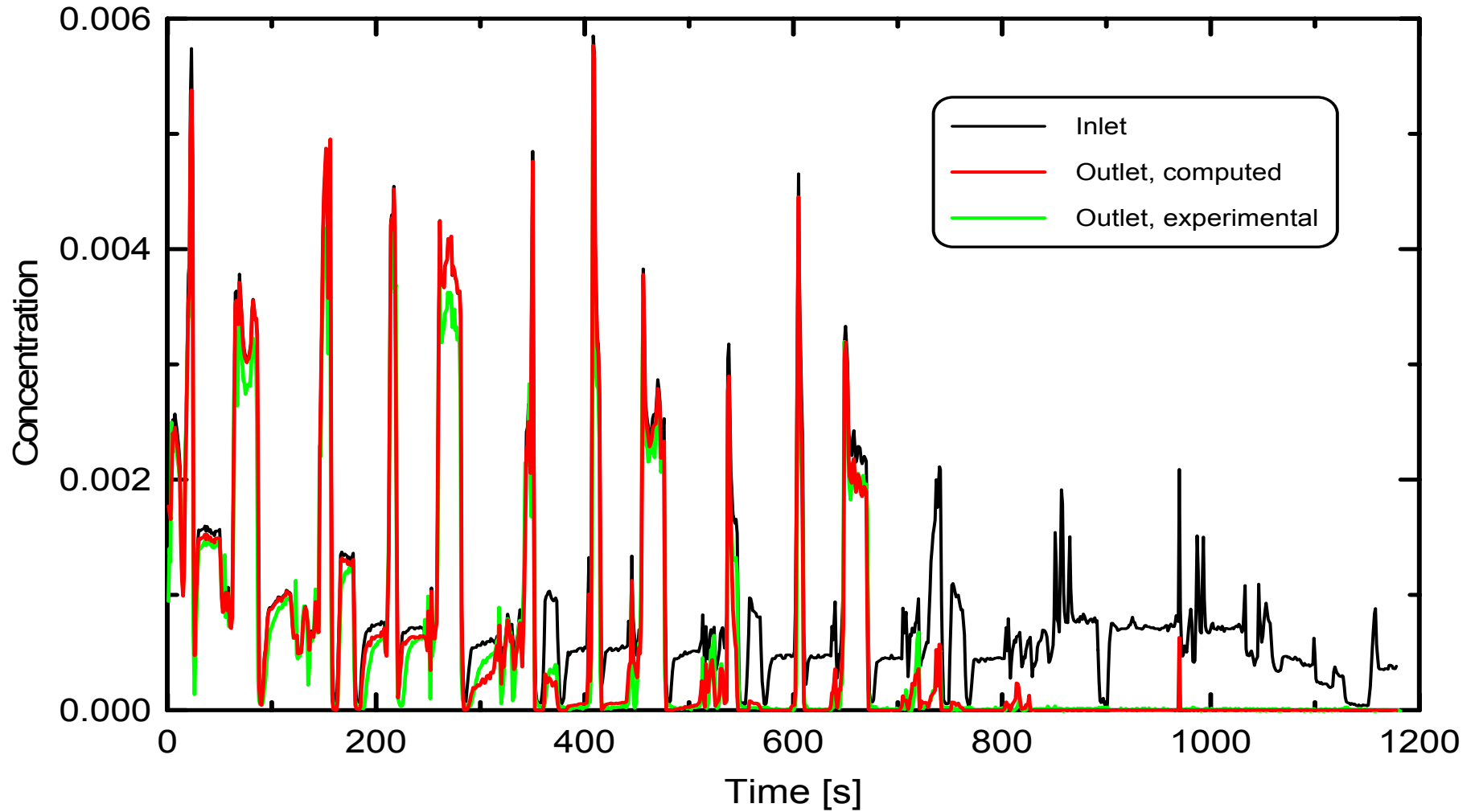
$$\ln x_{eq} = \ln(W_0 \rho) - D \left[\ln \left(\frac{p_0}{p} \right) \right]^2 \quad D = A \left(\frac{RT}{\beta} \right)^2$$

- A linear «driving force» is assumed to calculate the rates towards equilibrium.

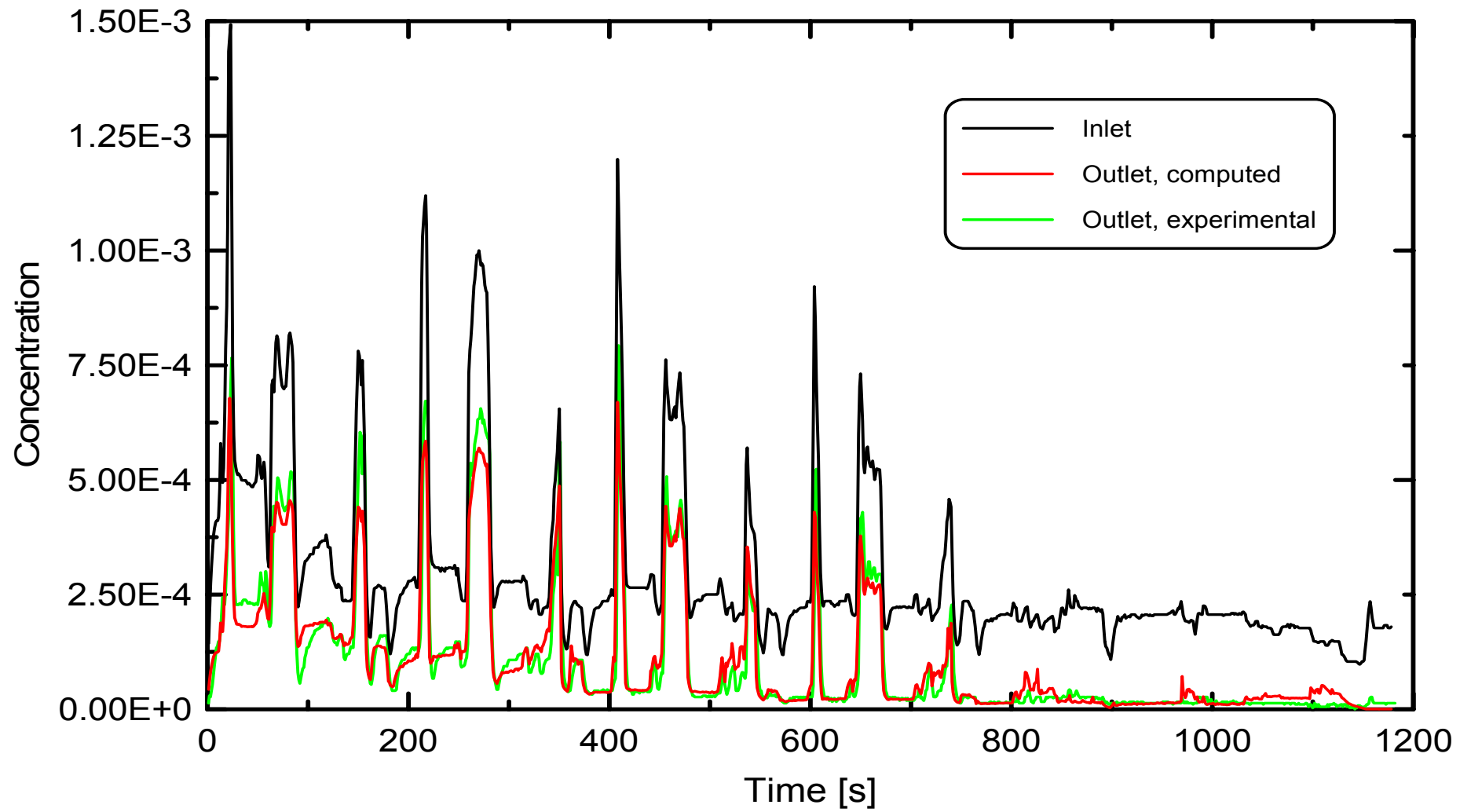
$$R = \frac{\partial x}{\partial t} = k \cdot (x_{eq} - x)$$

- Adjustable parameters:
 - ◆ W_0 (micropore volume)
 - ◆ A (micropore size distribution)
 - ◆ β (affinity parameter)
 - ◆ k (Arrhenius-type parameter)

CO prediction in transient driving cycle instantaneous emissions

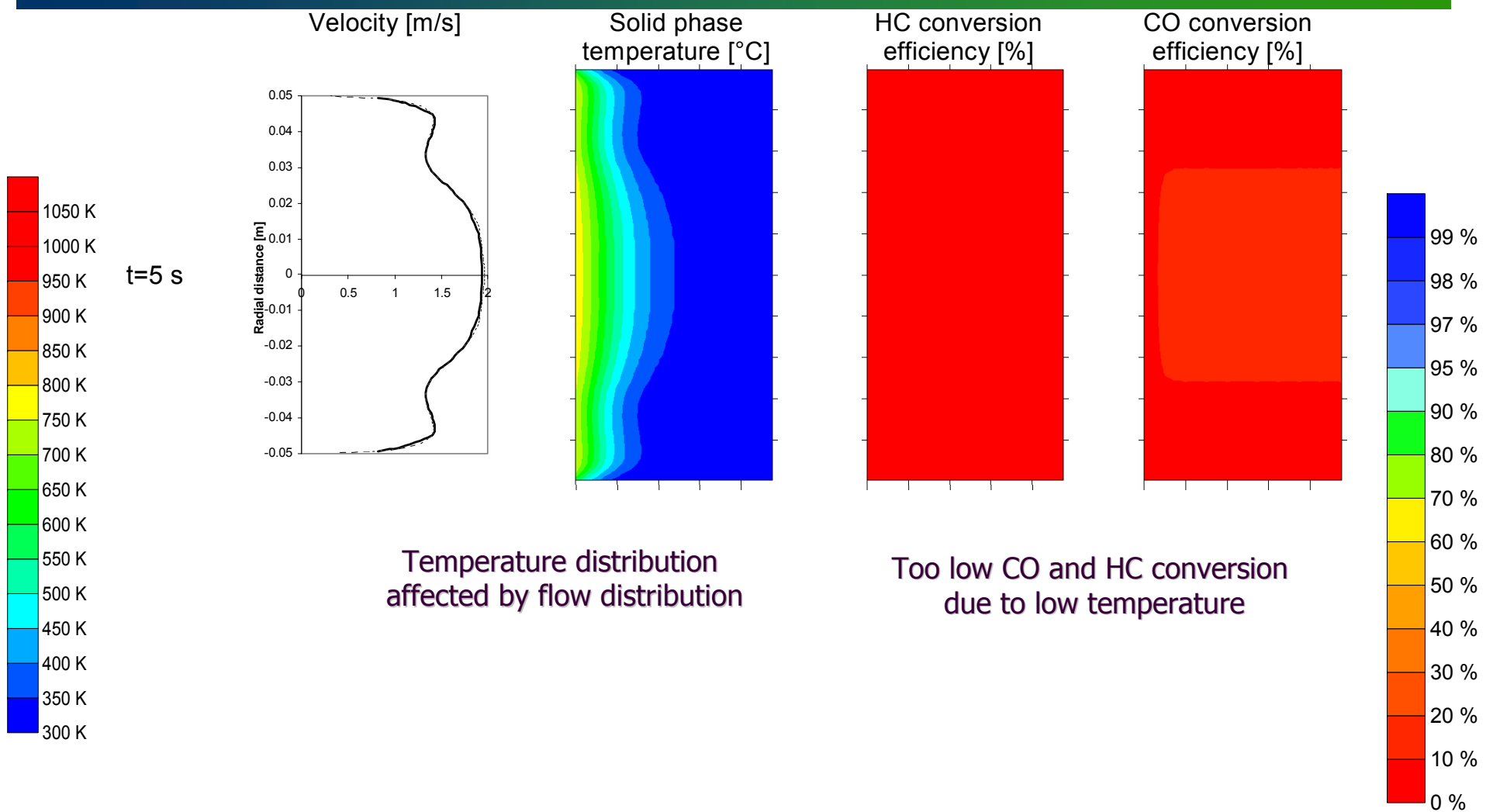


HC prediction in transient driving cycle instantaneous emissions

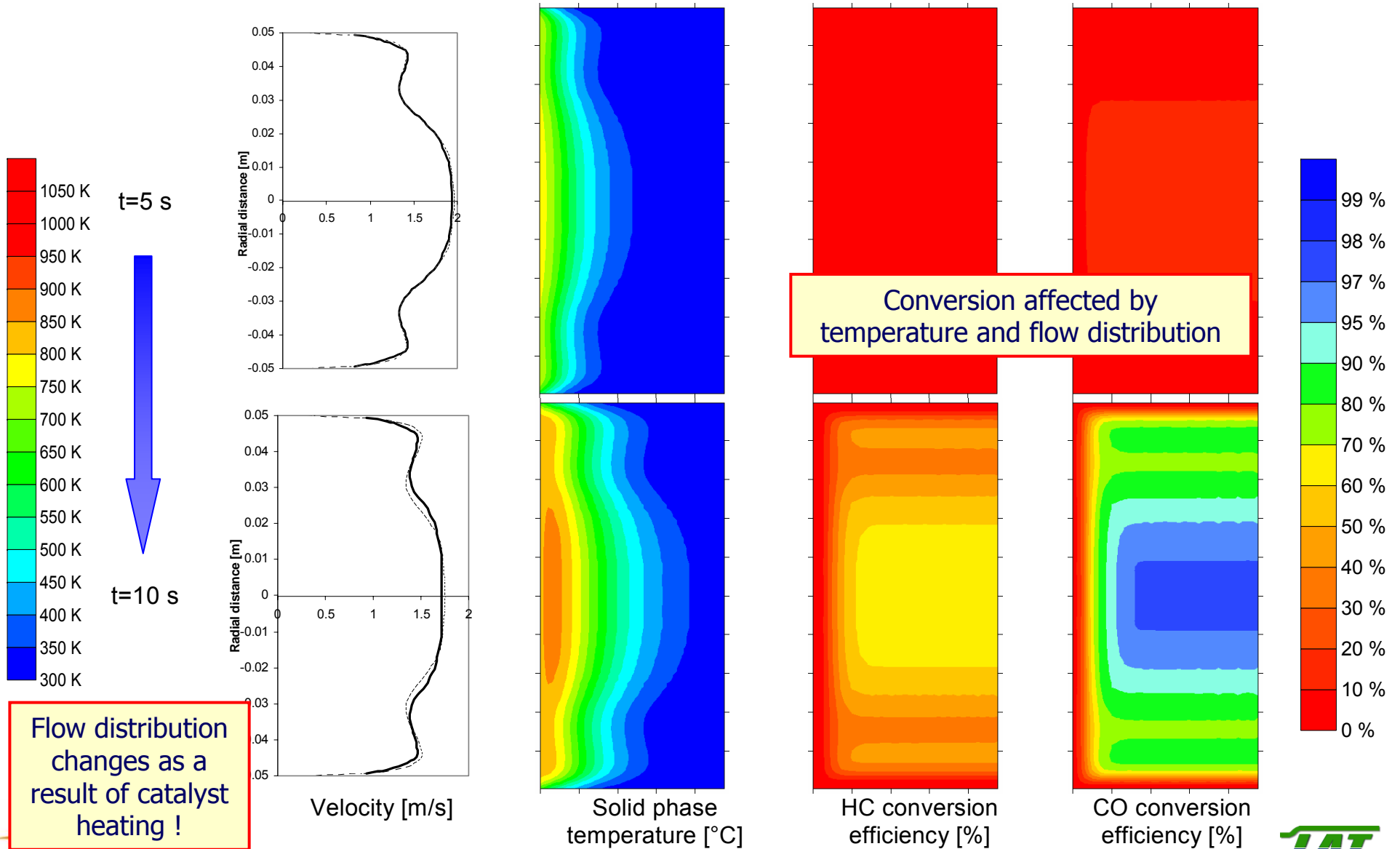


2-d simulation example

Catalyst warm-up behavior



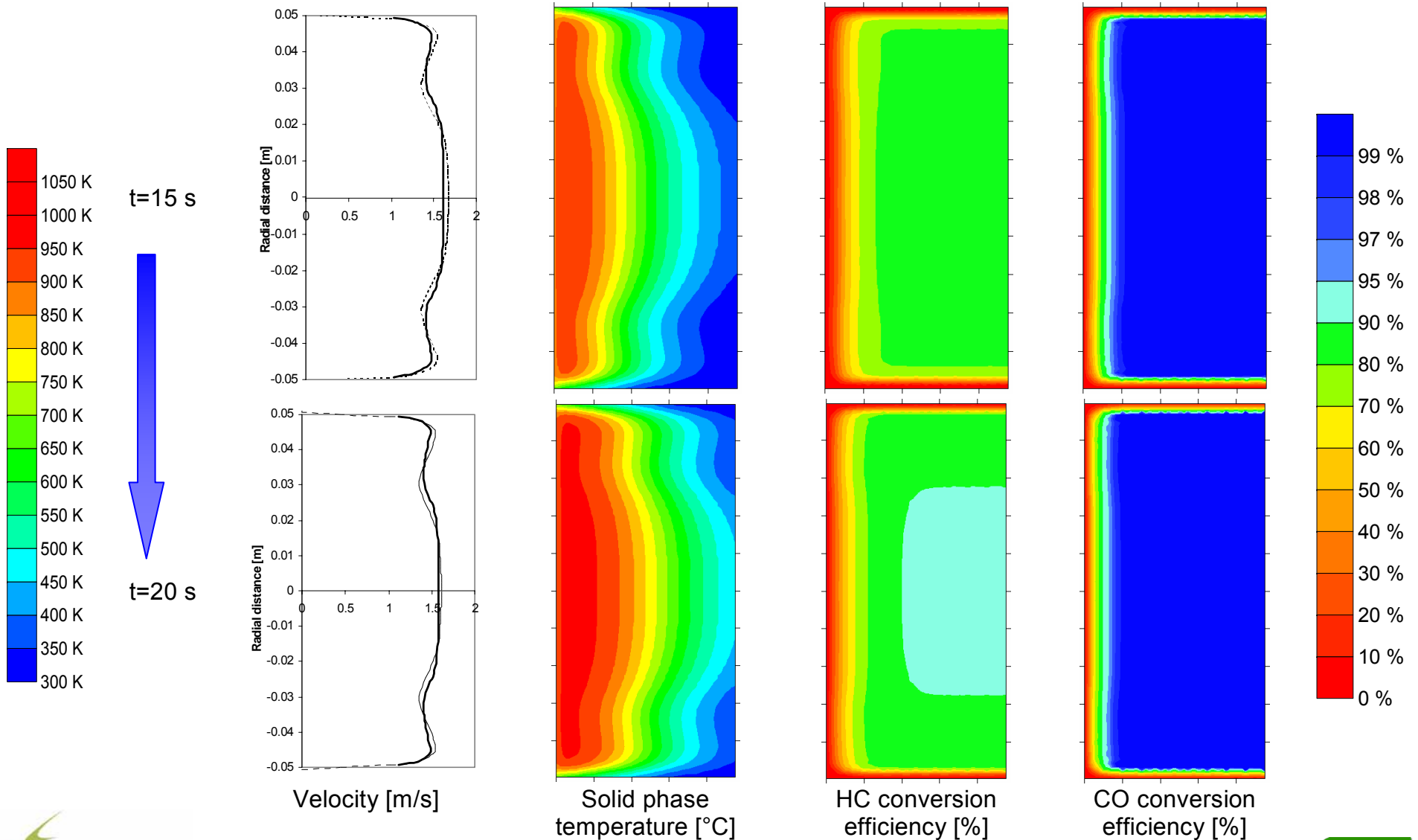
2-d simulation example Catalyst warm-up behavior



Flow distribution changes as a result of catalyst heating !

2-d simulation example

Catalyst warm-up behavior



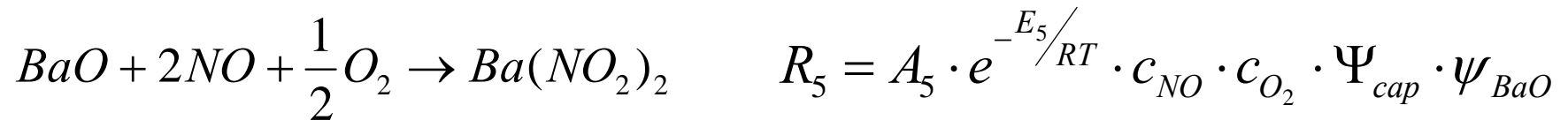
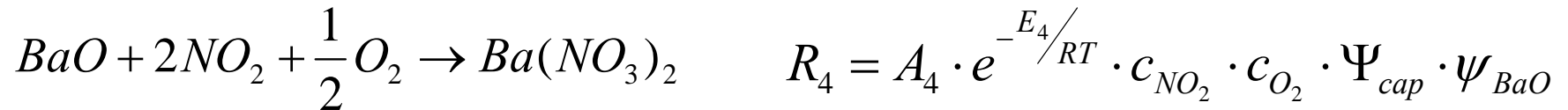


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LNT modeling

NO_x Storage reactions

NO, NO₂ storage



Nitrate and Nitrite decompositions

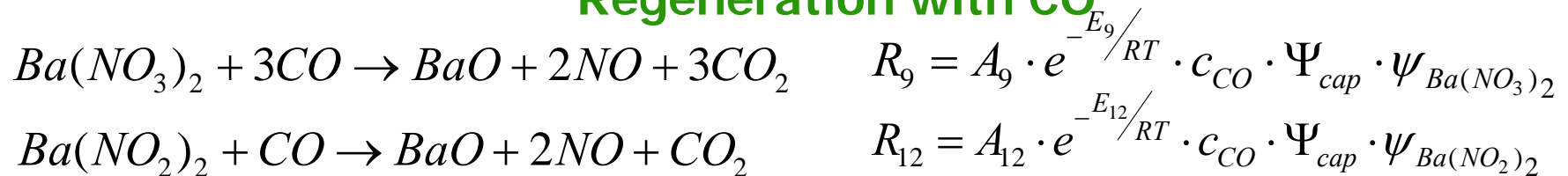


Nitrite to nitrate

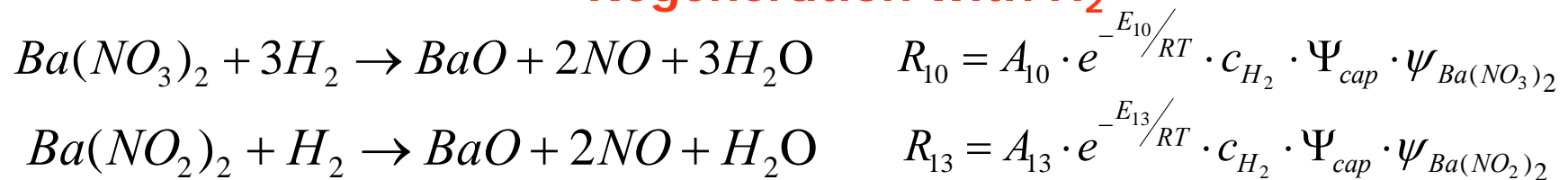


LNT Regeneration reactions

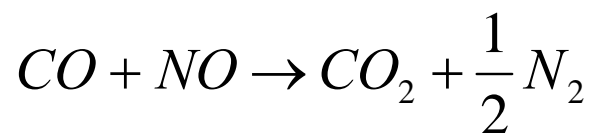
Regeneration with CO



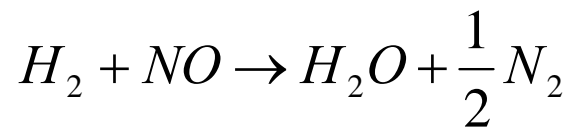
Regeneration with H₂



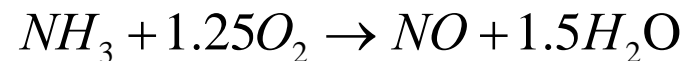
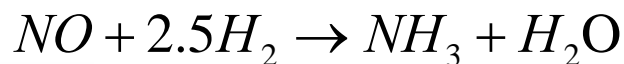
Reduction of released NO – NH₃ production/oxidation



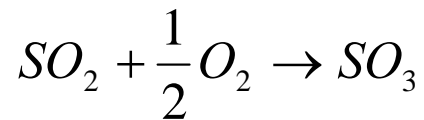
$$R_{11} = \frac{A_{11} \cdot e^{-E_{11}/RT} \cdot c_{CO} \cdot c_{NO}}{G_6}$$



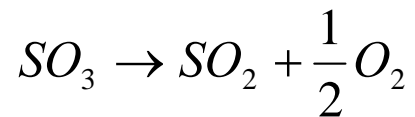
$$R_{14} = \frac{A_{14} \cdot e^{-E_{14}/RT} \cdot c_{H_2} \cdot c_{NO}}{G_6}$$



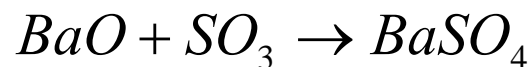
Sulfation/desulfation model



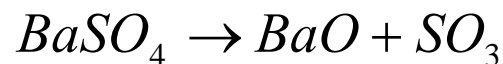
$$R = (A \cdot e^{-E/RT} \cdot c_{SO_2} \cdot c_{O_2} \cdot Eq) / G_1$$



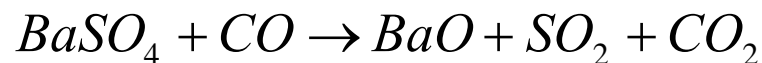
$$R = (A \cdot e^{-E/RT} \cdot c_{SO_3} \cdot Eq) / G_1$$



$$R = A \cdot e^{-E/RT} \cdot c_{SO_3} \cdot \Psi_{cap} \cdot \psi_{BaO} \cdot Eq$$



$$R = A \cdot e^{-E/RT} \cdot \Psi_{cap} \cdot \psi_{BaSO_4} \cdot Eq$$



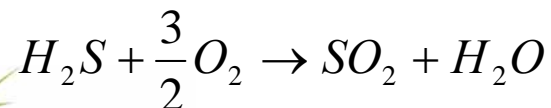
$$R = A \cdot e^{-E/RT} \cdot c_{CO} \cdot \Psi_{cap} \cdot \psi_{BaSO_4} \cdot Eq$$



$$R = A \cdot e^{-E/RT} \cdot c_{H_2} \cdot \Psi_{cap} \cdot \psi_{BaSO_4} \cdot Eq$$



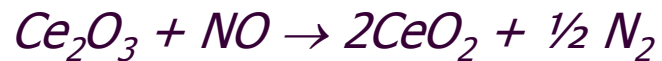
$$R = A \cdot e^{-E/RT} \cdot c_{H_2} \cdot \Psi_{cap} \cdot \psi_{BaSO_4} \cdot Eq$$



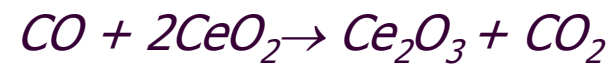
$$R = (A \cdot e^{-E/RT} \cdot c_{H_2S} \cdot c_{O_2}) / G_1$$

O₂ storage submodel – Ceria based mechanism

O₂ "storage"



O₂ "release"



Ce oxidation state

$$\psi = \frac{2 \times \text{moles CeO}_2}{2 \times \text{moles CeO}_2 + \text{moles Ce}_2\text{O}_3}$$

$$\frac{d\psi}{dt} = -\frac{1}{\Psi_{cap}} (R_{ox} - R_{red})$$

Oxygen storage/release phenomena strongly affect reductants availability and NO release during regeneration

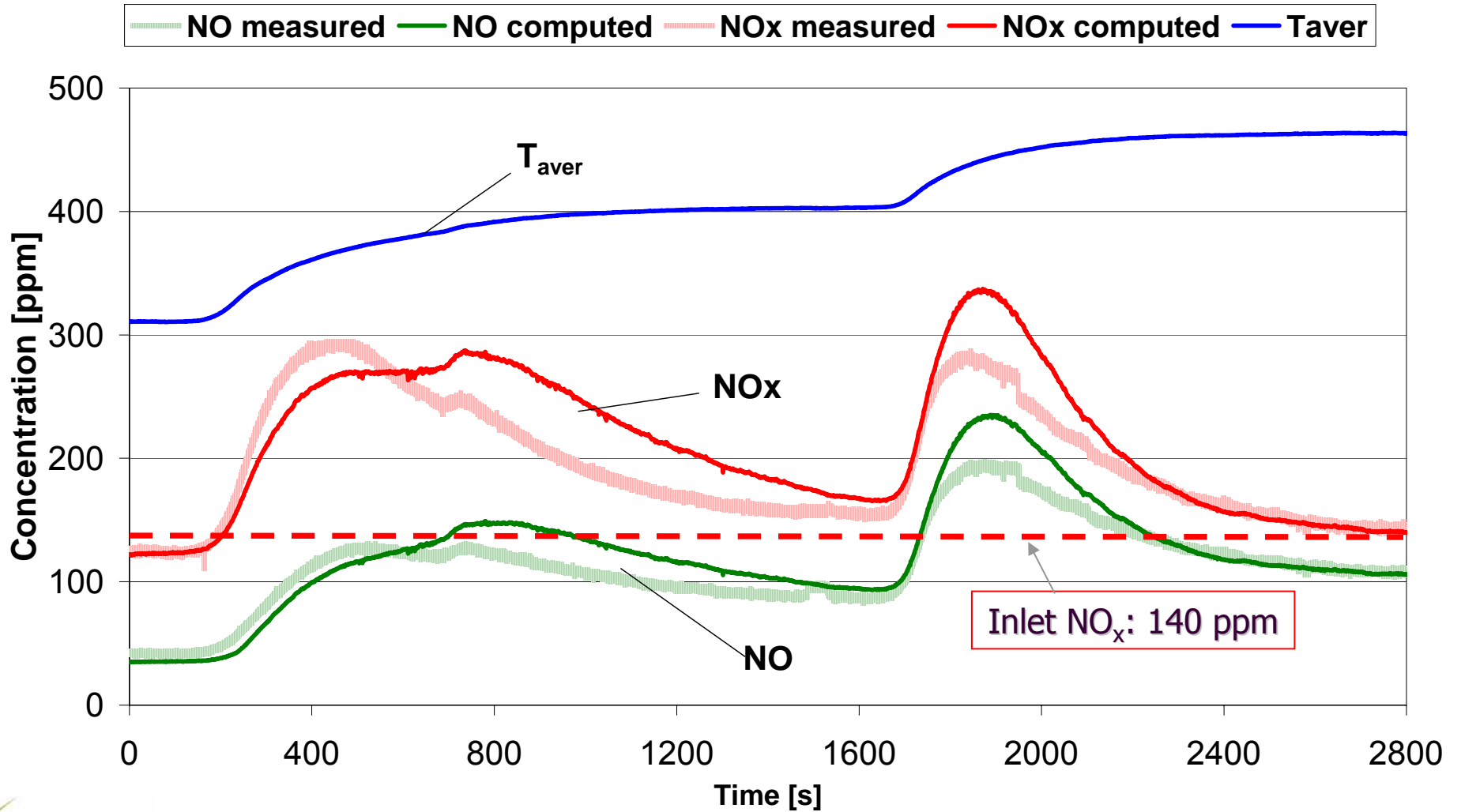
LNT model parameter calibration

Tube reactor placed in an electrically heated tube furnace



"Spontaneous" (thermal) NO_x release during temperature increase in lean operation

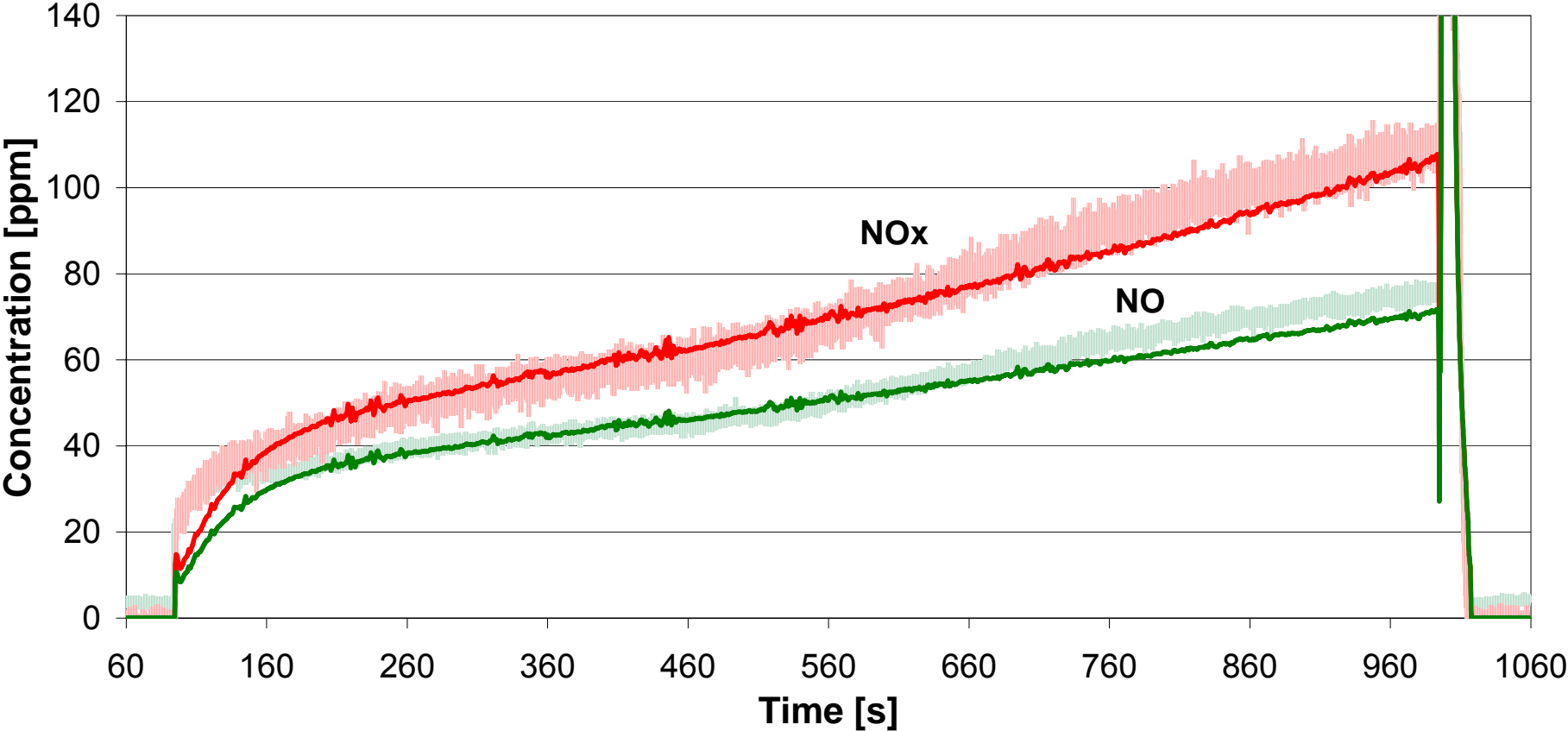
Inlet: NO:67 ppm, NO₂:73 ppm, NO_x:140 ppm, GHSV:88000 [h⁻¹]



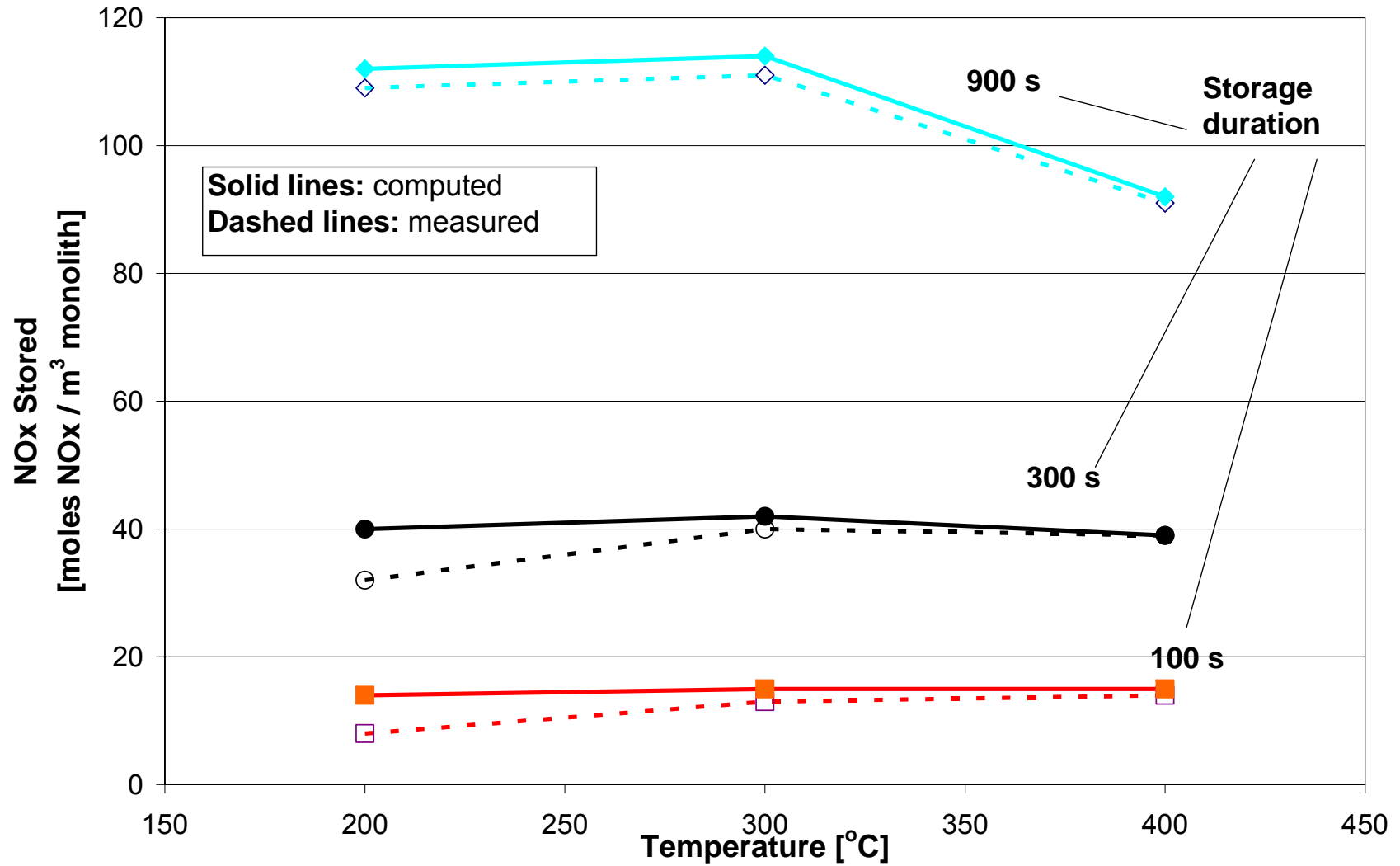
Storage experiment at 400°C with diesel exhaust

Inlet: NO:90 ppm, NO₂:75 ppm, NO_x:165 ppm

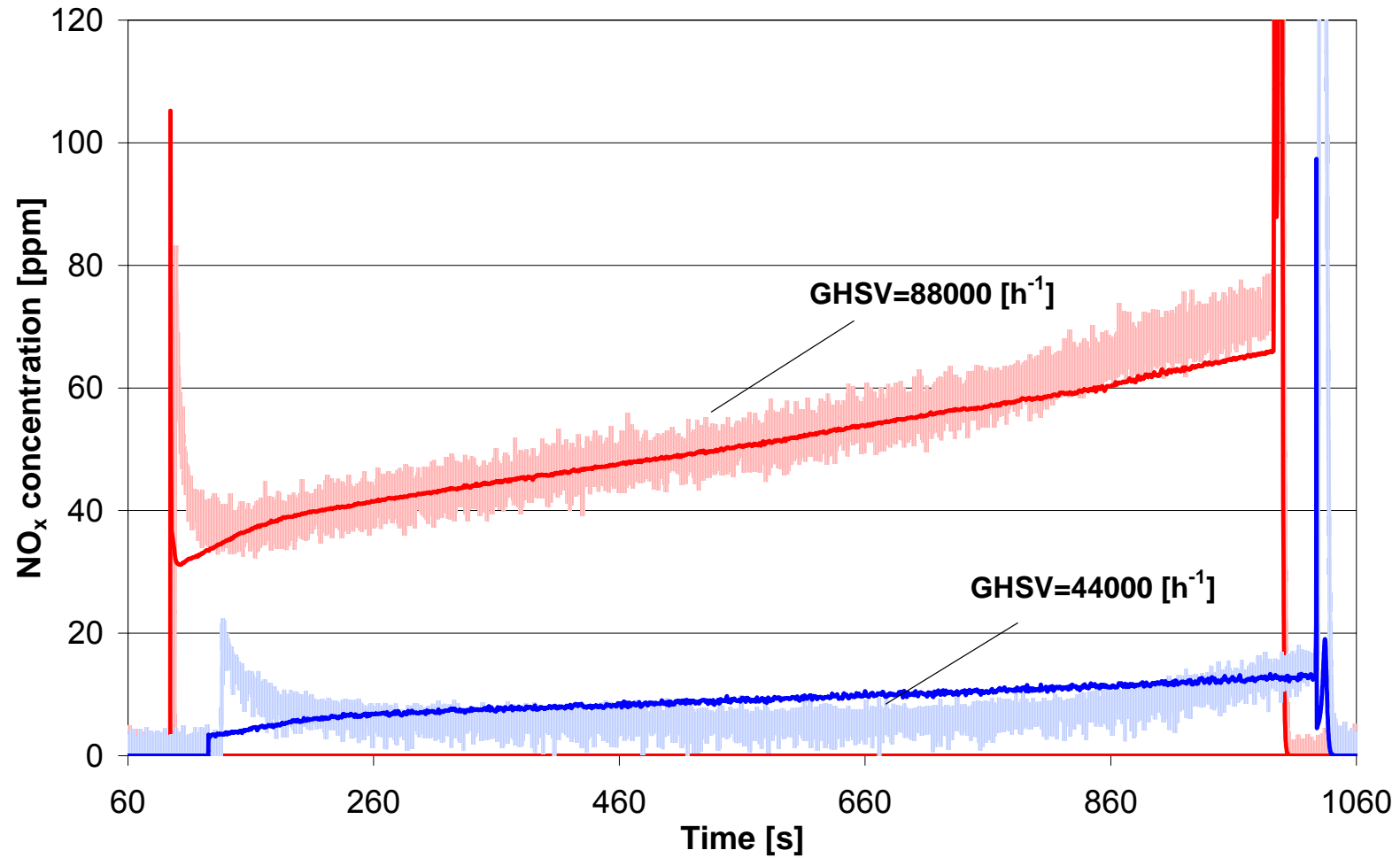
NO measured NO_x measured NO_x computed NO computed



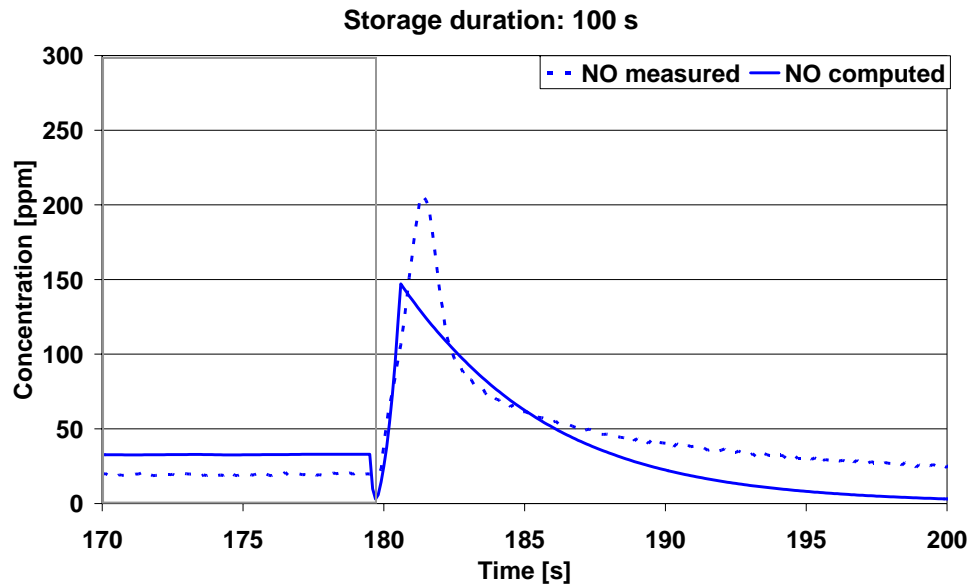
Stored NO_x at different temperatures



Model validation at different flow rate at 300°C

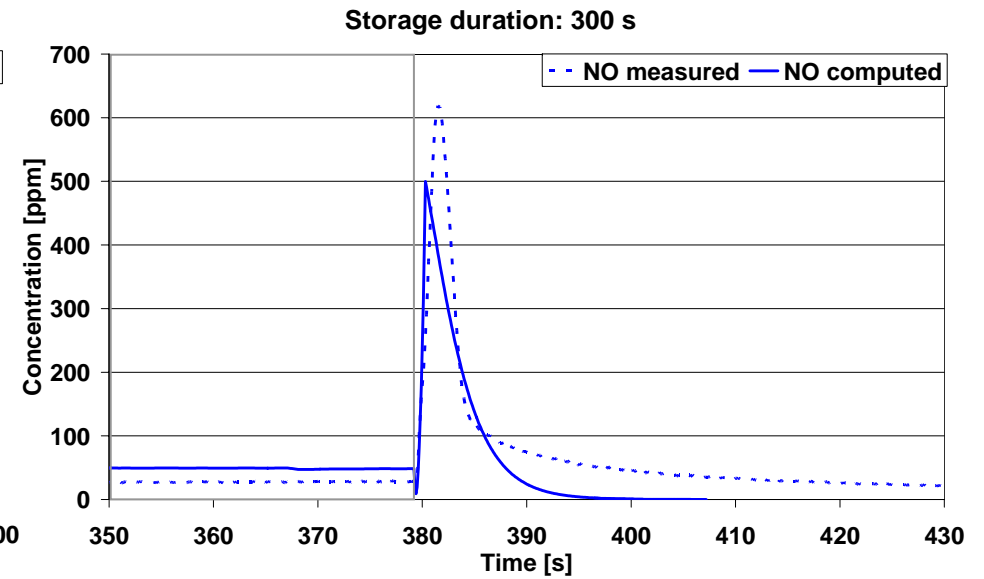
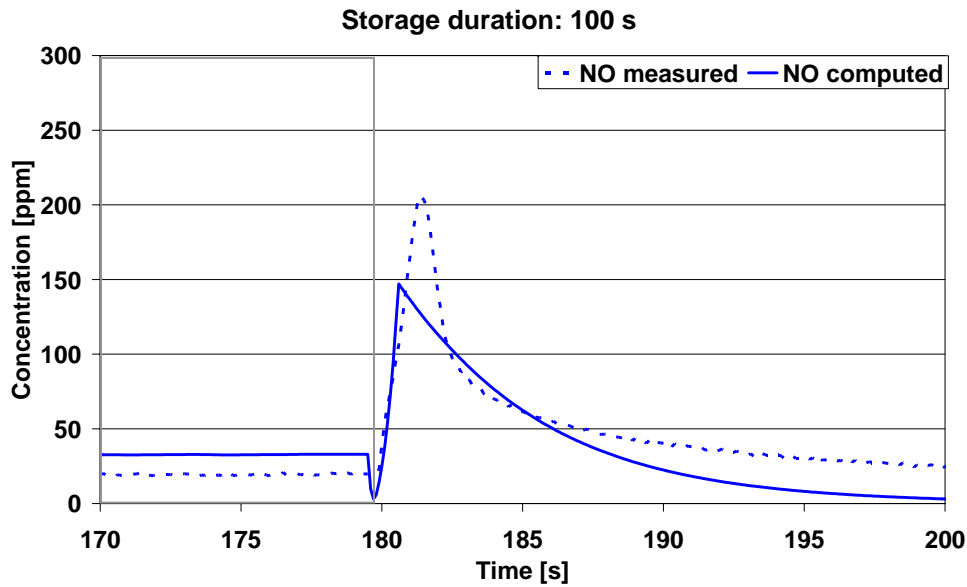


NO emissions during regeneration at 200°C



**During regeneration NO_2 is negligible
(not favored thermodynamically)**

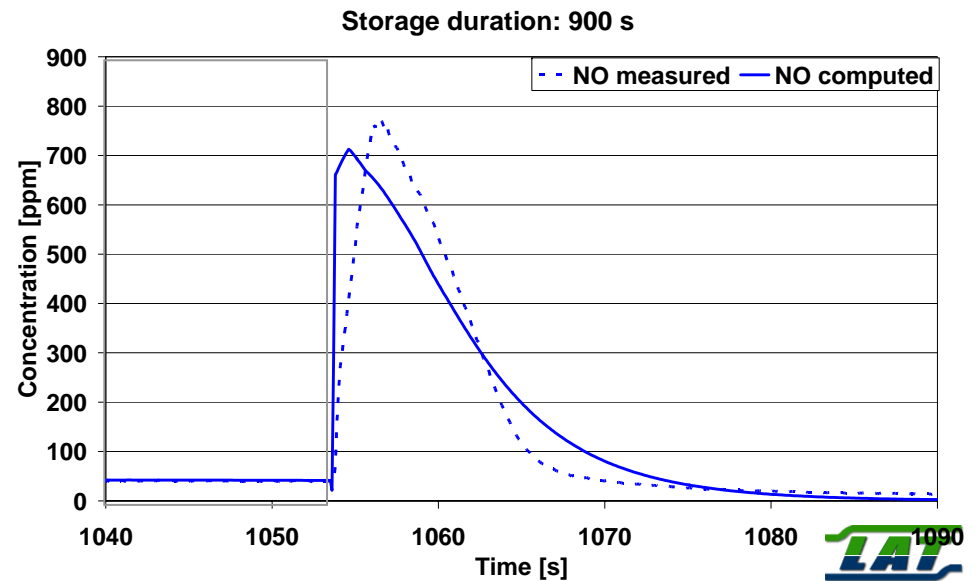
NO emissions during regeneration at 200°C



During regeneration NO_2 is negligible
(not favored thermodynamically)

Note the different peak NO levels

NO release duration: 5 - 10 s



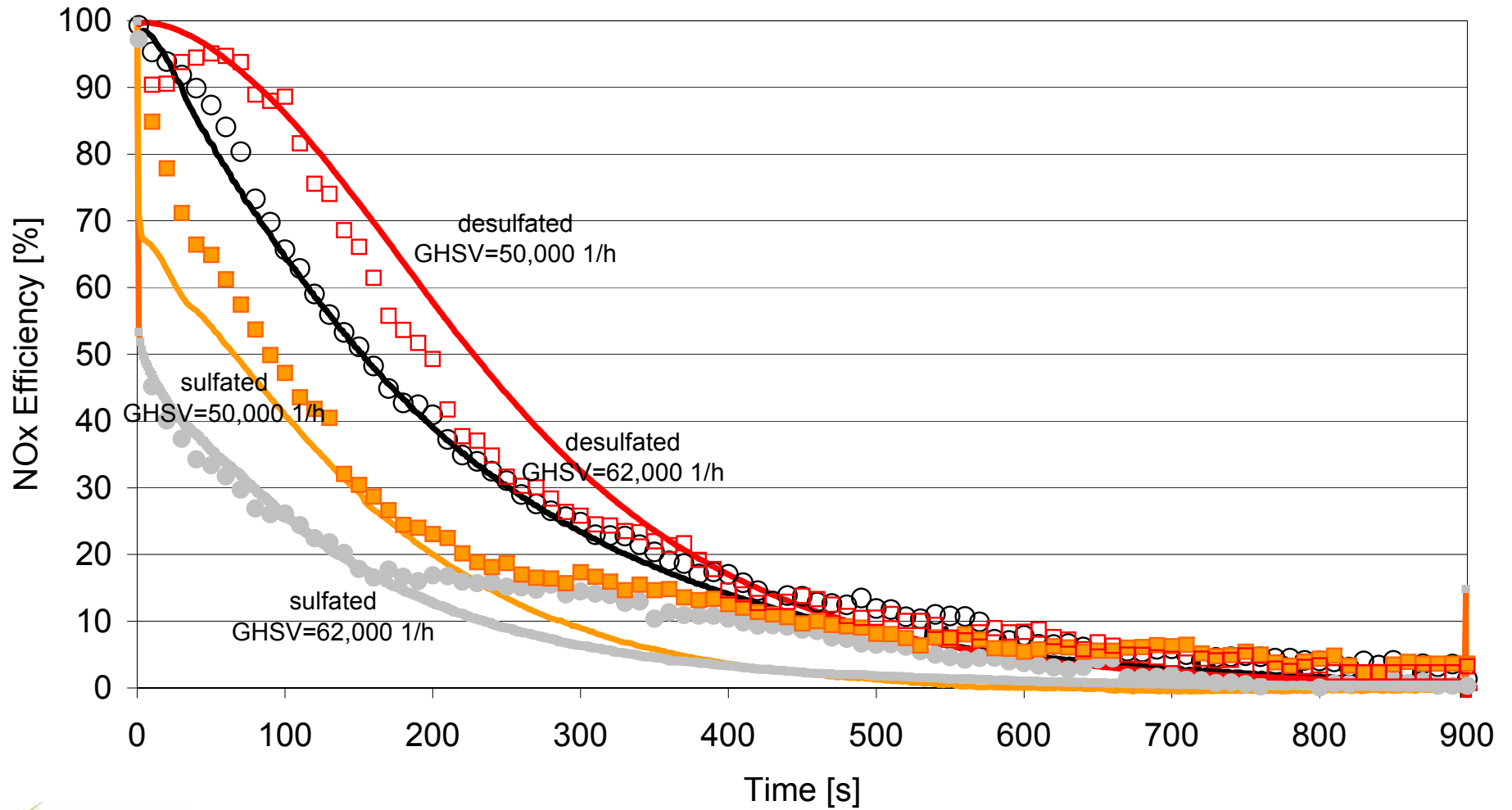


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Sulfur effects

Sulfation model validation at two different space velocities

Marks: measurement, Lines: computed





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SCR catalyst modeling

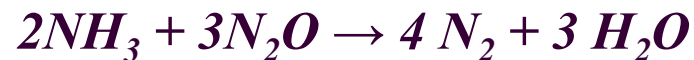
Main SCR reactions

➤ Reaction scheme:

◆ SCR reactions



◆ Alternatively, "direct $\text{NH}_3 + \text{NO}_2$ " reaction is split in 2 reactions:



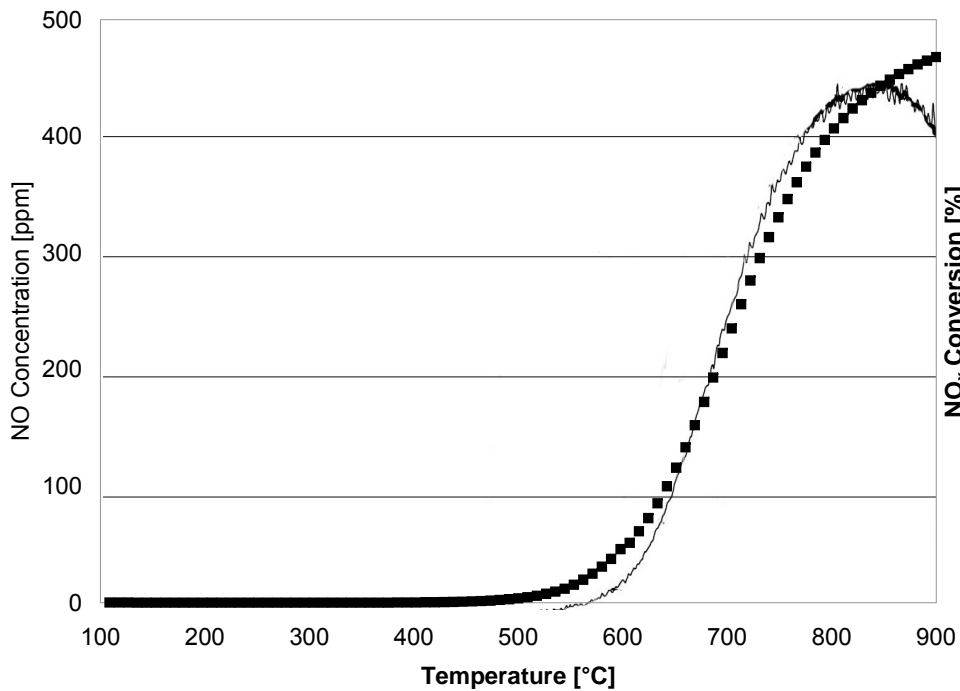
◆ NH_3 oxidation reaction



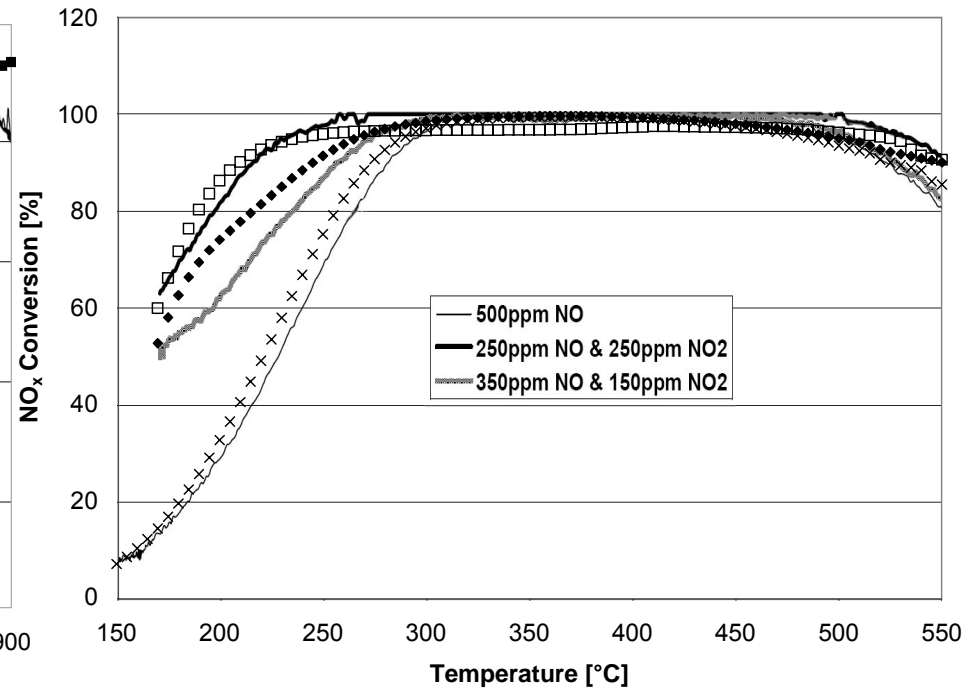
SCR

Parameter calibration example

NH₃ oxidation



Effect of NO/NO₂ ratio

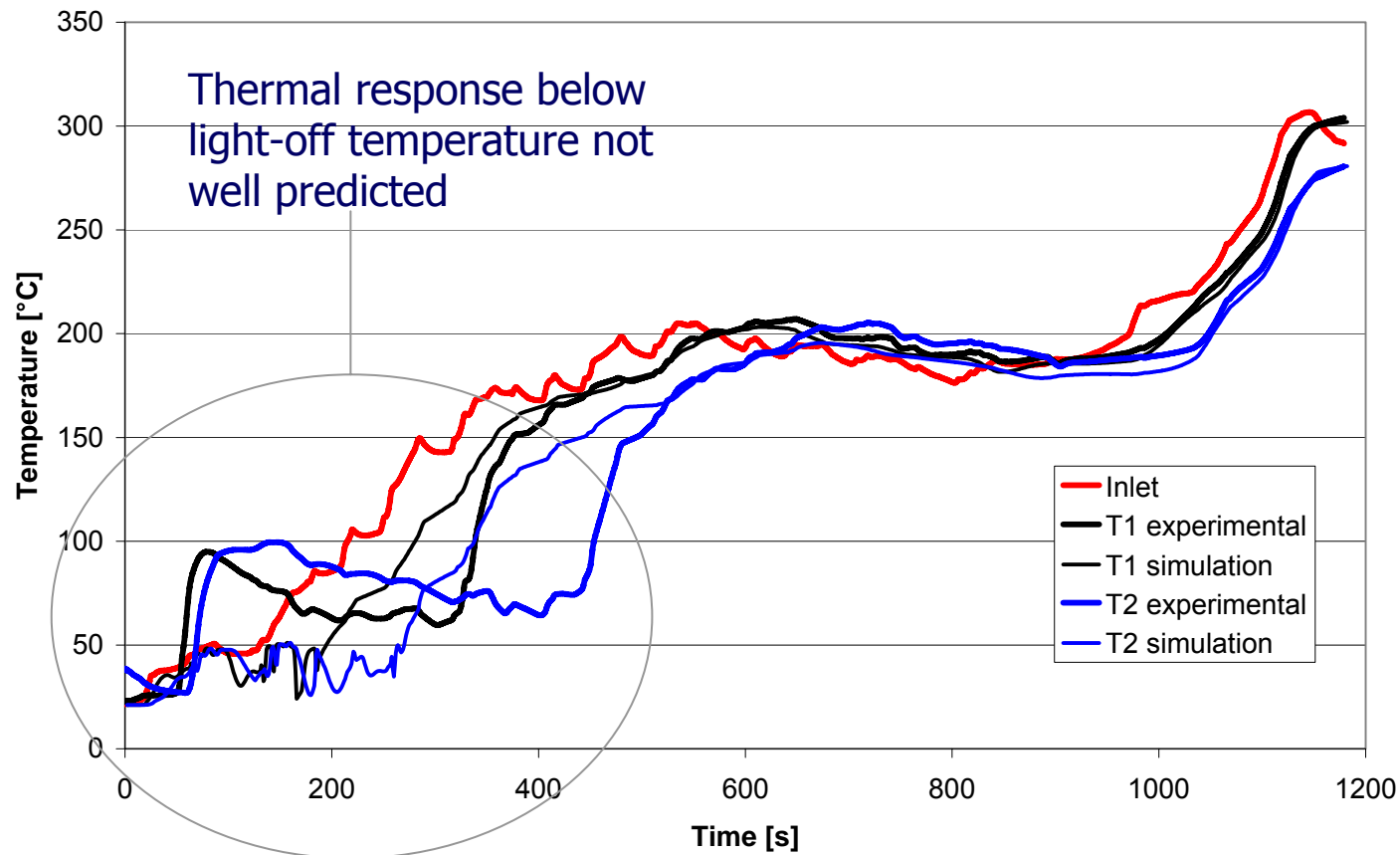


Lines: Experimental, symbols: simulation.

Experimental Data Source: Winkler et al., Modeling of SCR DeNO_x Catalyst – Looking at the Impact of Substrate Attributes, SAE Paper 2003-01-0845

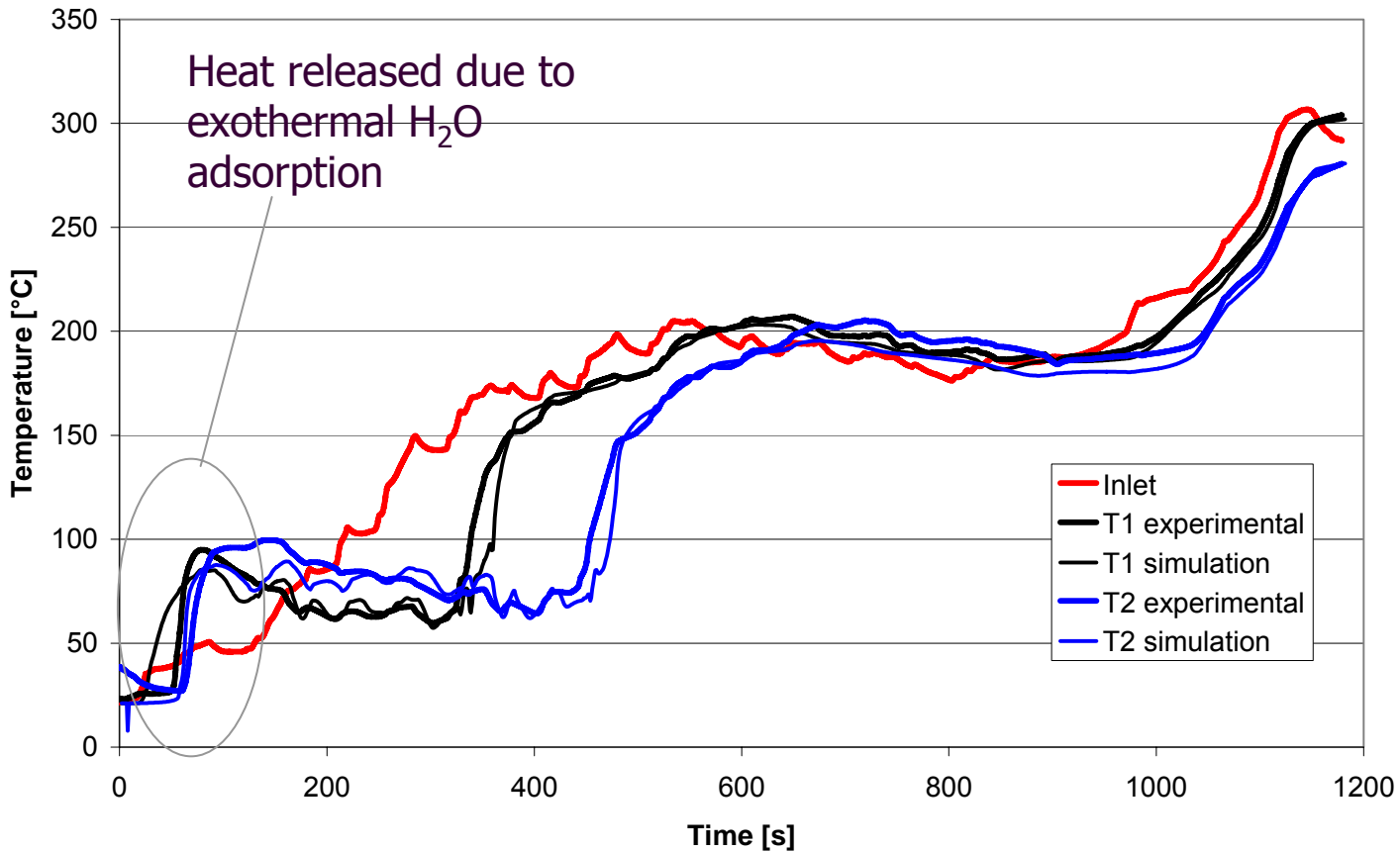
Experimental validation SCR simulation in transient cycle

- ◆ Water adsorption **neglected!**



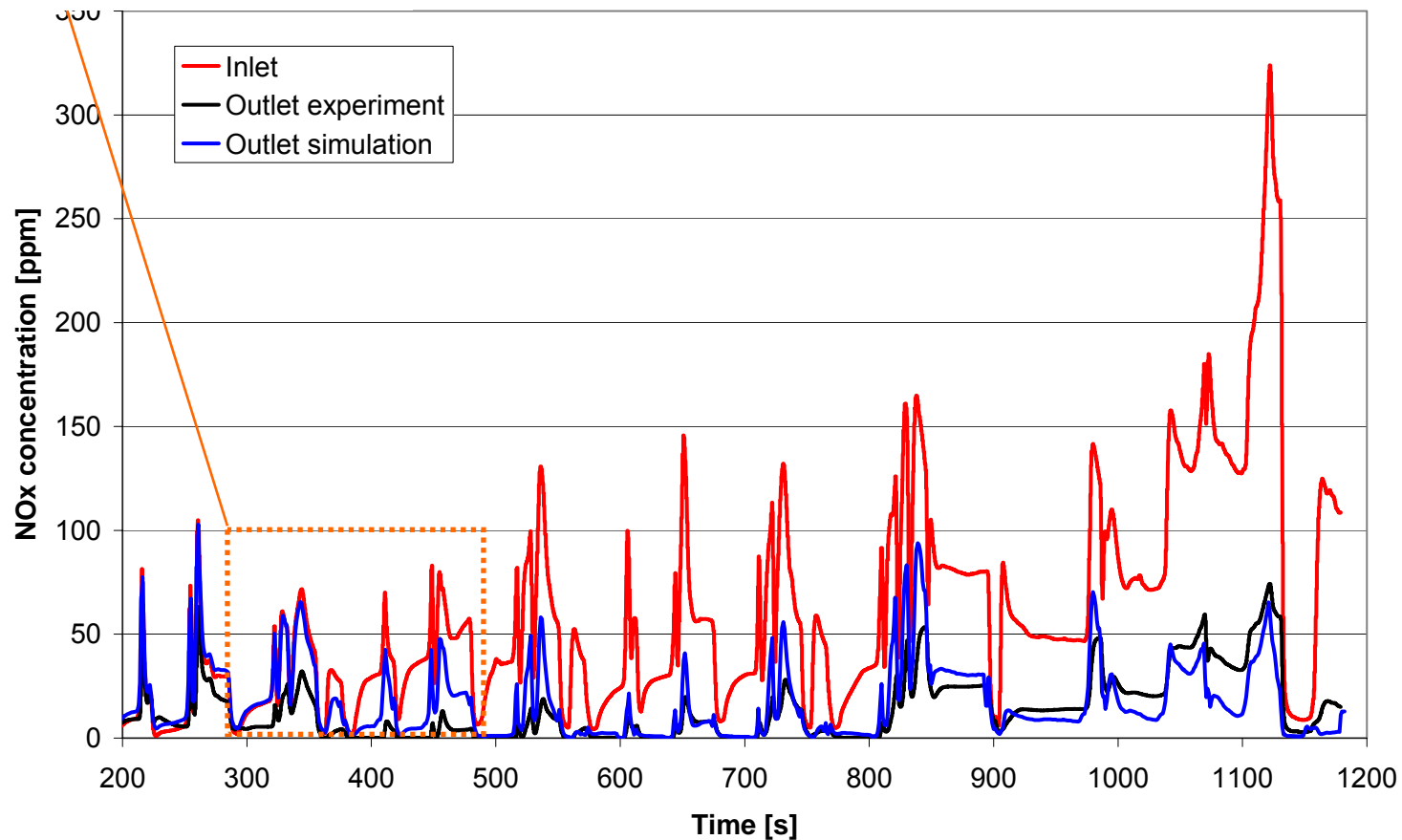
Experimental validation SCR simulation in transient cycle

Water adsorption **included!**



Experimental validation SCR simulation in transient cycle

NOx conversion measured and simulated, as a result of SCR reaction with previously adsorbed ammonia



Experiments conducted at an engine test bench of IAV GmbH



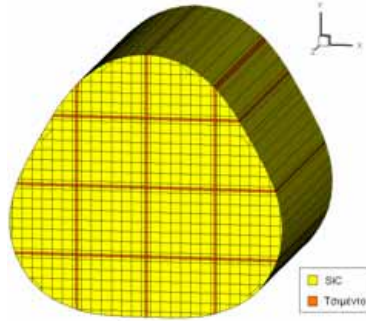
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Wall-flow reactor modeling

Wall-flow Reactor Modeling Modeling levels

Filter scale

- 3D heat transfer
- Inlet flow distribution
- Diffuser effects
- Soot non-uniformities

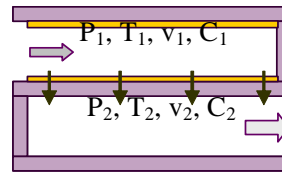


Equations

- Solid energy balance
- Mass balance
- Diffuser pressure drop

Channel scale

- Heat convection
- Wall velocity profile
- Mass convection

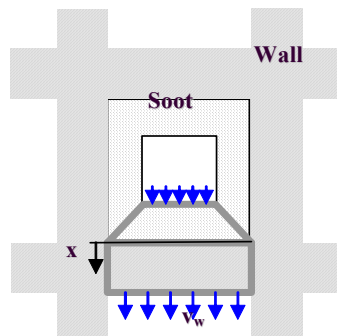


Equations

- Gas energy balance
- Mass balance
- Momentum balance
- Species balance

Wall scale

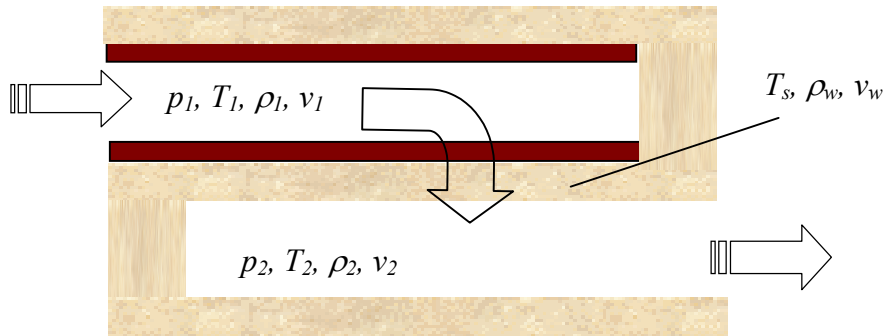
- Intra-layer reaction
- Intra-layer diffusion
- Intra-layer velocity and density variation



Equations

- Species balance
- Soot mass balance
- Soot layer pressure drop

Channel scale (1-d modeling) Equations



Gas phase

Mass

$$\frac{\partial}{\partial z} (d_i^2 \rho_i v_i) = (-1)^i 4 d \rho_w v_w$$

Momentum

$$\frac{\partial p_i}{\partial z} + \frac{\partial}{\partial z} (\rho_i v_i^2) = -\alpha_1 \mu v_i / d_i^2$$

Energy

$$C_{p,g} \rho_1 v_1 \Big|_z \frac{\partial T_1}{\partial z} = h_1 \frac{4}{d_1} (T_s - T_1)$$

$$C_{p,g} \rho_2 v_2 \Big|_z \frac{\partial T_2}{\partial z} = (h_2 + C_{p,g} \rho_w v_w) \frac{4}{d} (T_s - T_2)$$

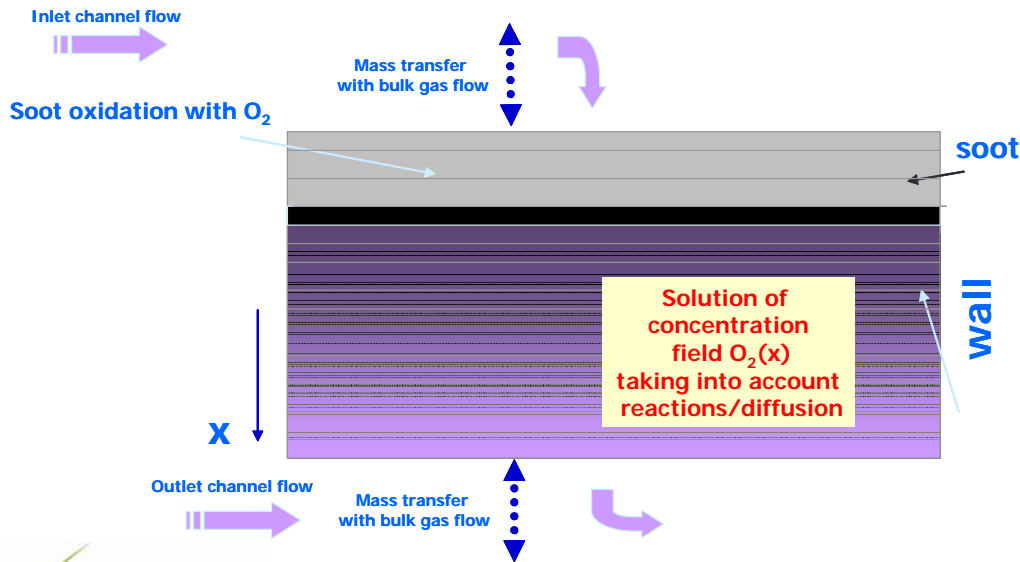
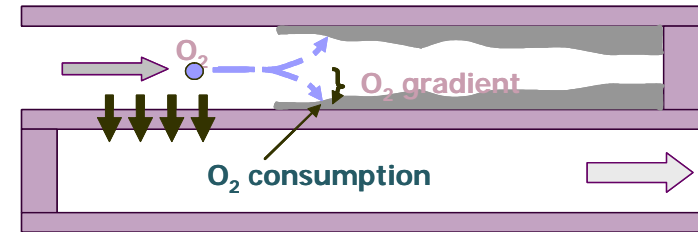
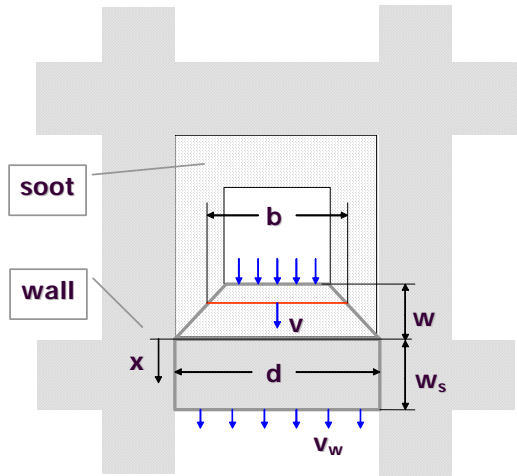
Wall – Energy balance

$$\frac{\partial}{\partial t} (\rho_p C_{p,p} T_w + \rho_s C_{p,s} T_w) = h_1 (T_1 - T_w) + h_2 (T_2 - T_w) + \rho_w v_w C_{p,g} (T_1 - T_w) + H_{react} + H_{cond}$$

Soot – Mass balance

$$\rho_p \frac{dw}{dt} = - \left(\frac{M_c}{M_{O_2}} \right) \rho_w v_w y \frac{1}{a} \left(1 - \exp \left(- \frac{S_p k_1 (T_w) w}{v_w} a \right) \right)$$

Transport-reaction "coupling"



Convective mass transfer in channels

$$\frac{\partial}{\partial z} (v_1 y_{1,j}) = -\frac{1}{df_{-w}^2} v_w y_{1,j} + \frac{1}{df_{-w}} k_{1,j} (y_{1s,j} - y_{1,j})$$

$$\frac{\partial}{\partial z} (v_2 y_{2,j}) = \frac{1}{df_{w_s}^2} v_w y_{2s,j} + \frac{1}{df_{w_s}} k_{2,j} (y_{2s,j} - y_{2,j})$$

Intra-layer reaction-diffusion coupling

$$v_w \frac{\partial y_j}{\partial x} - D_j \frac{\partial}{\partial x} \left(f_x \frac{\partial y_j}{\partial x} \right) = \frac{f_x}{c_m} \sum_k c_{j,k} R_k$$

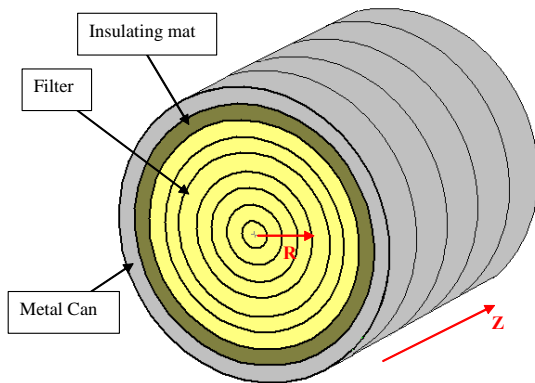
Intra-layer soot mass balance

$$\frac{d\hat{m}_p}{dt} = -\hat{m}_p \sum R'_k + s_F \rho_w v_w \mu_p$$

Intra-layer Δp law

$$\frac{dp}{dx} = \frac{\mu v(x)}{k_p}$$

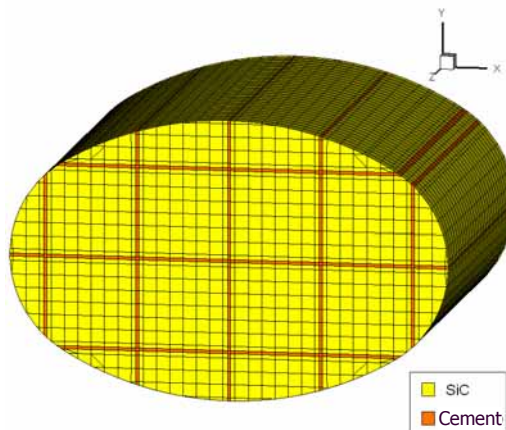
2-d & 3-d extension



2-d Transient Heat Transfer

$$\rho_s \cdot C_{p,s} \frac{\partial T_s}{\partial t} = \lambda_{s,z} \frac{\partial^2 T_s}{\partial z^2} + \lambda_{s,r} \frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial T_s}{\partial r} \right) + S$$

$$S = H_{conv} + H_{wall} + H_{react} + H_{rad}$$



3-d Transient Heat Transfer

$$\rho_s \cdot C_{p,s} \frac{\partial T_s}{\partial t} = \lambda_{s,z} \frac{\partial^2 T_s}{\partial x^2} + \lambda_{s,r} \frac{\partial^2 T_s}{\partial y^2} + \lambda_{s,r} \frac{\partial^2 T_s}{\partial z^2} + S$$

$$S = H_{conv} + H_{wall} + H_{react} + H_{rad}$$



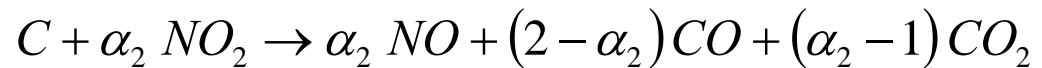
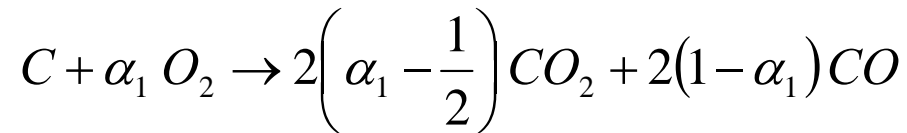
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Wall-flow DOC

Model Reactions

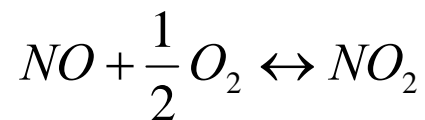
Soot layer

Carbon oxidation

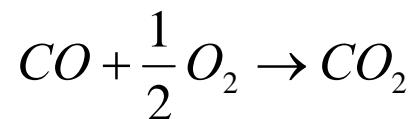


Catalyzed wall: basic reactions for Noble Metals coatings

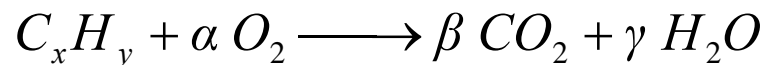
Bi-directional
NO oxidation



CO oxidation



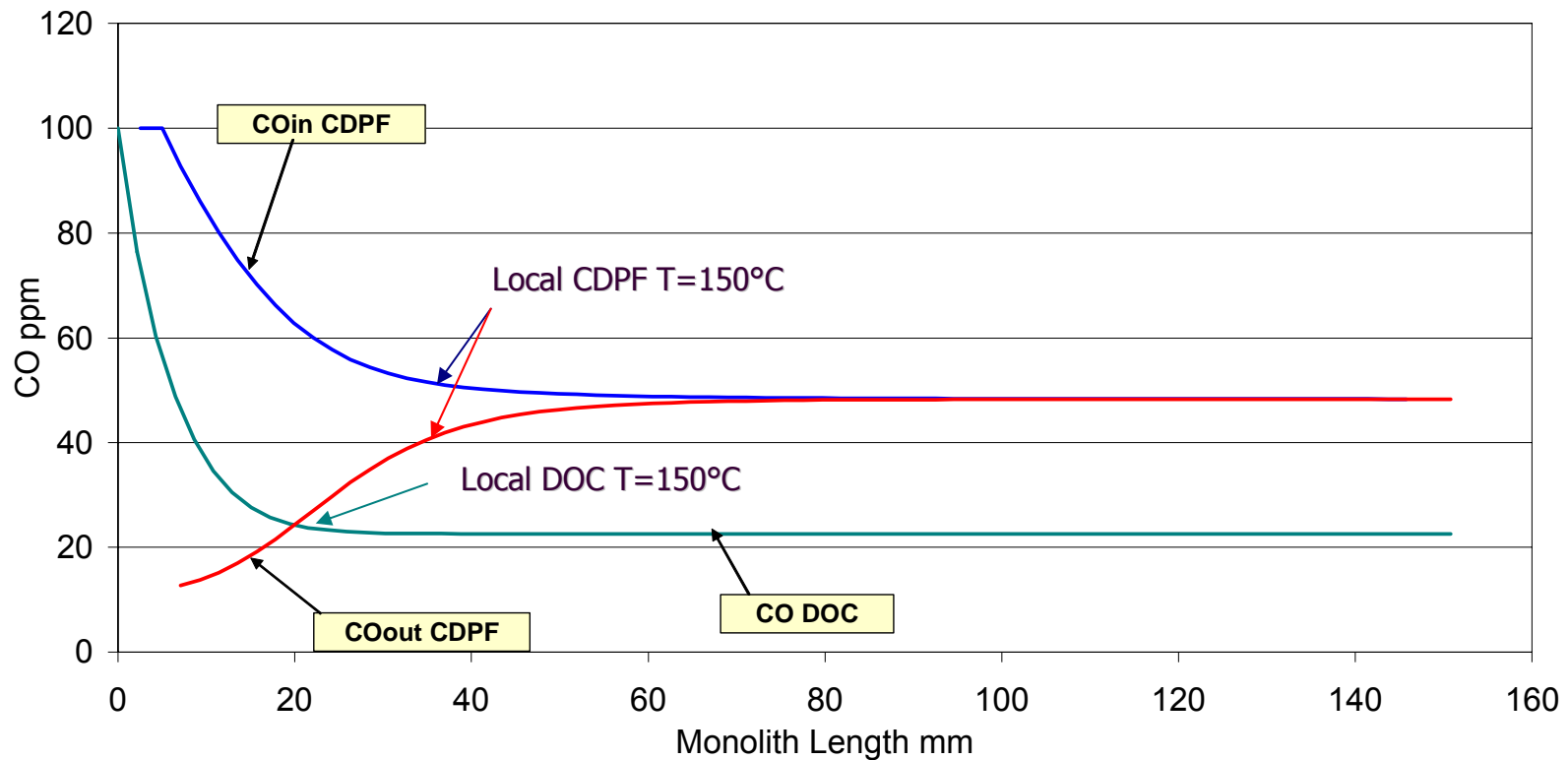
HC oxidation



CO profiles in DOC and CDPF during warm-up

"Active length" ($T > 150^\circ\text{C}$): DOC: 25 mm, CDPF: 35 mm

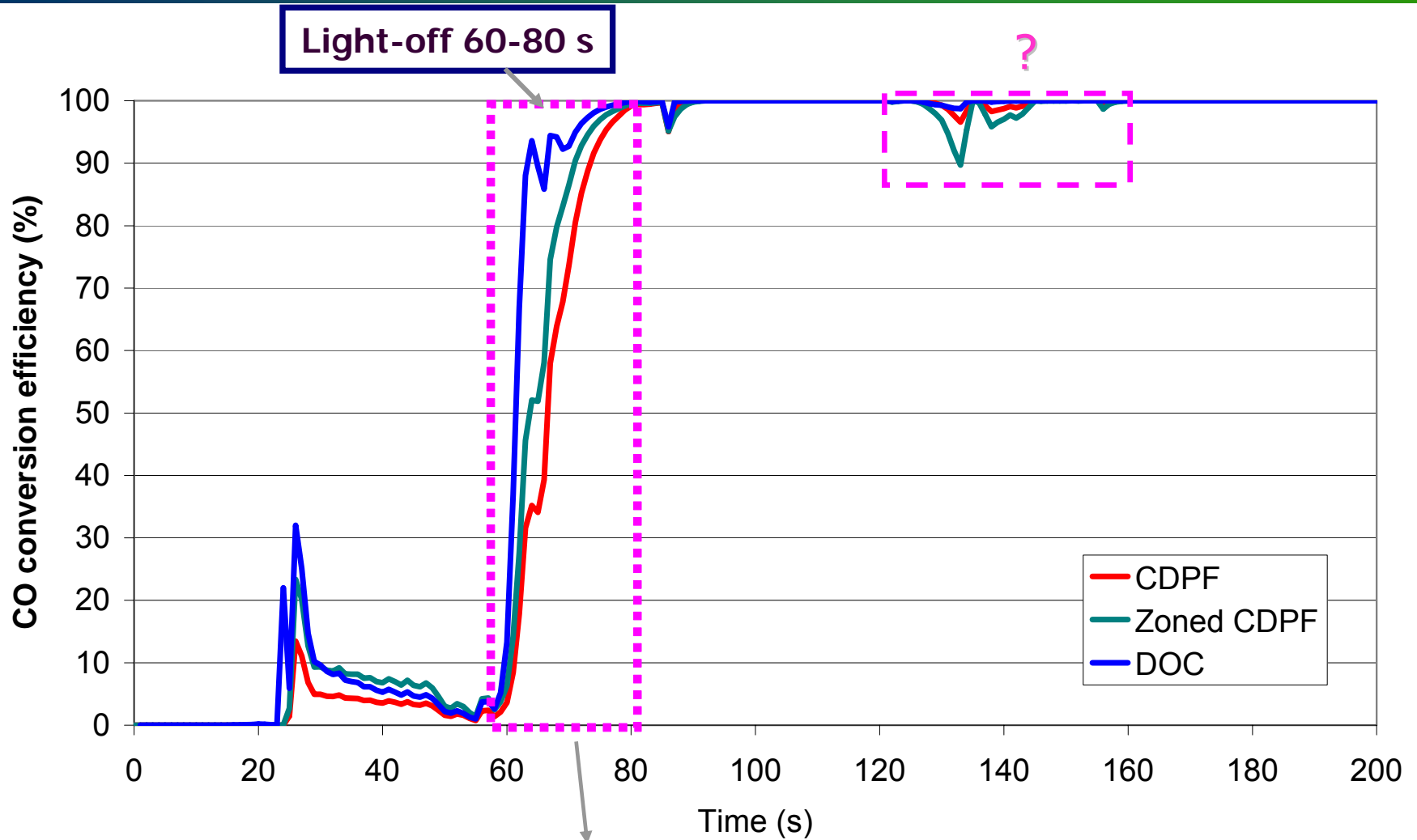
CO profiles $t = 15\text{ s}$



Due to the lower axial gas velocities in the DOC the conversion is higher despite the shorter "active length"

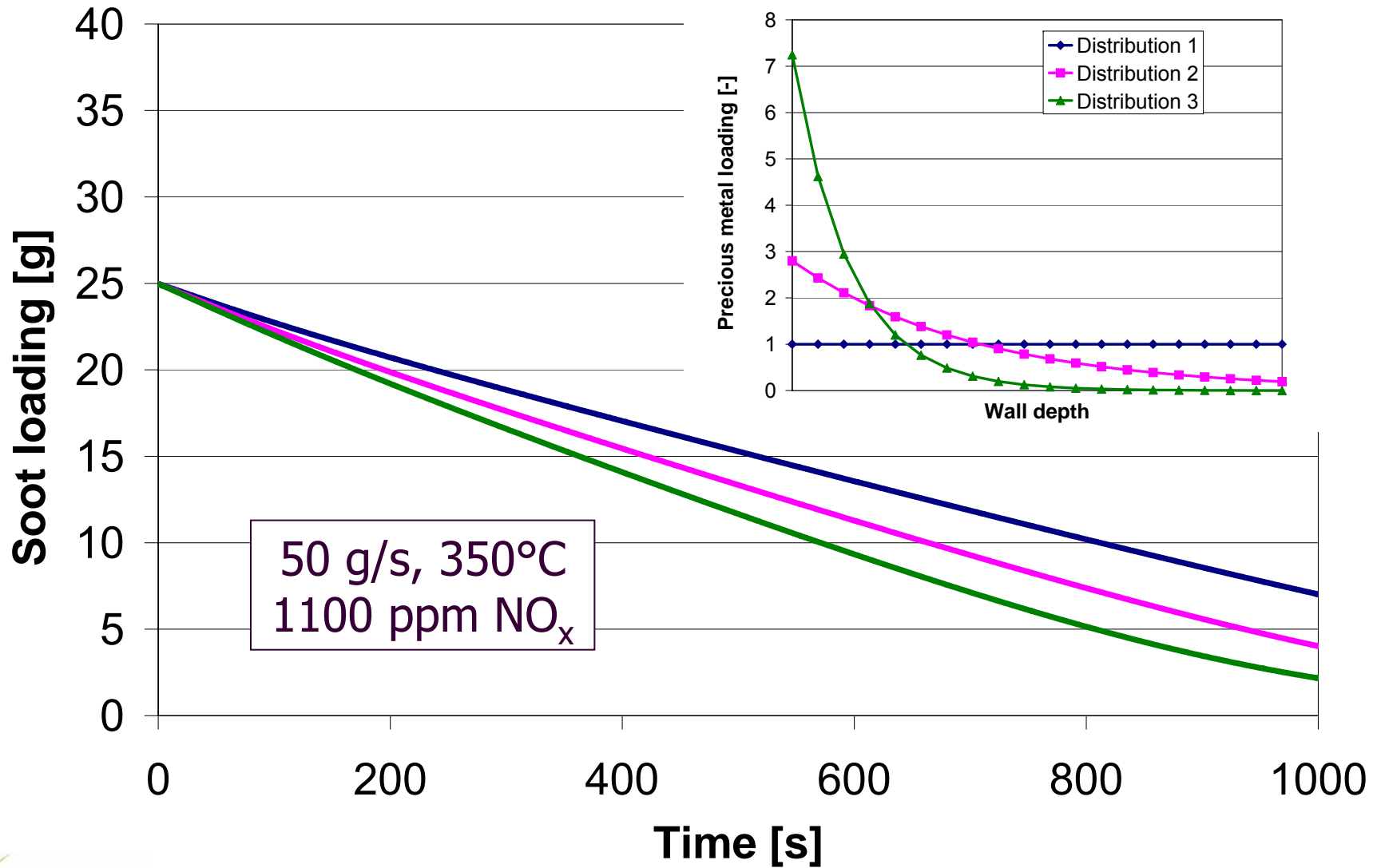
Wall-flow reactor performance in driving cycle

Effect of catalyst zoning



Light-off phase: DOC better than CDPF
zCDPF better than CDPF

Effect of intra-wall catalyst distribution CDPF regeneration rate



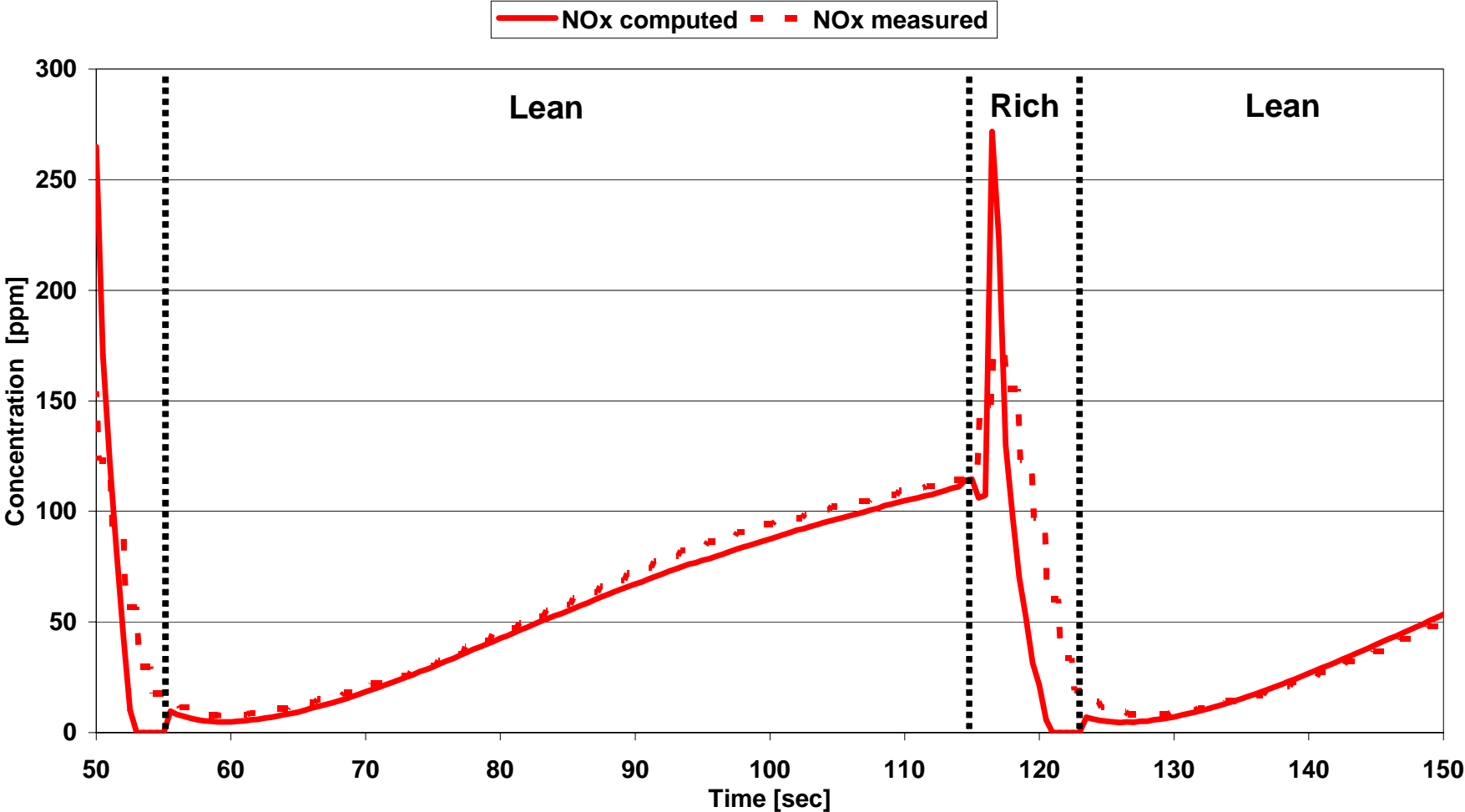


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Wall-flow LNT (DPNR)

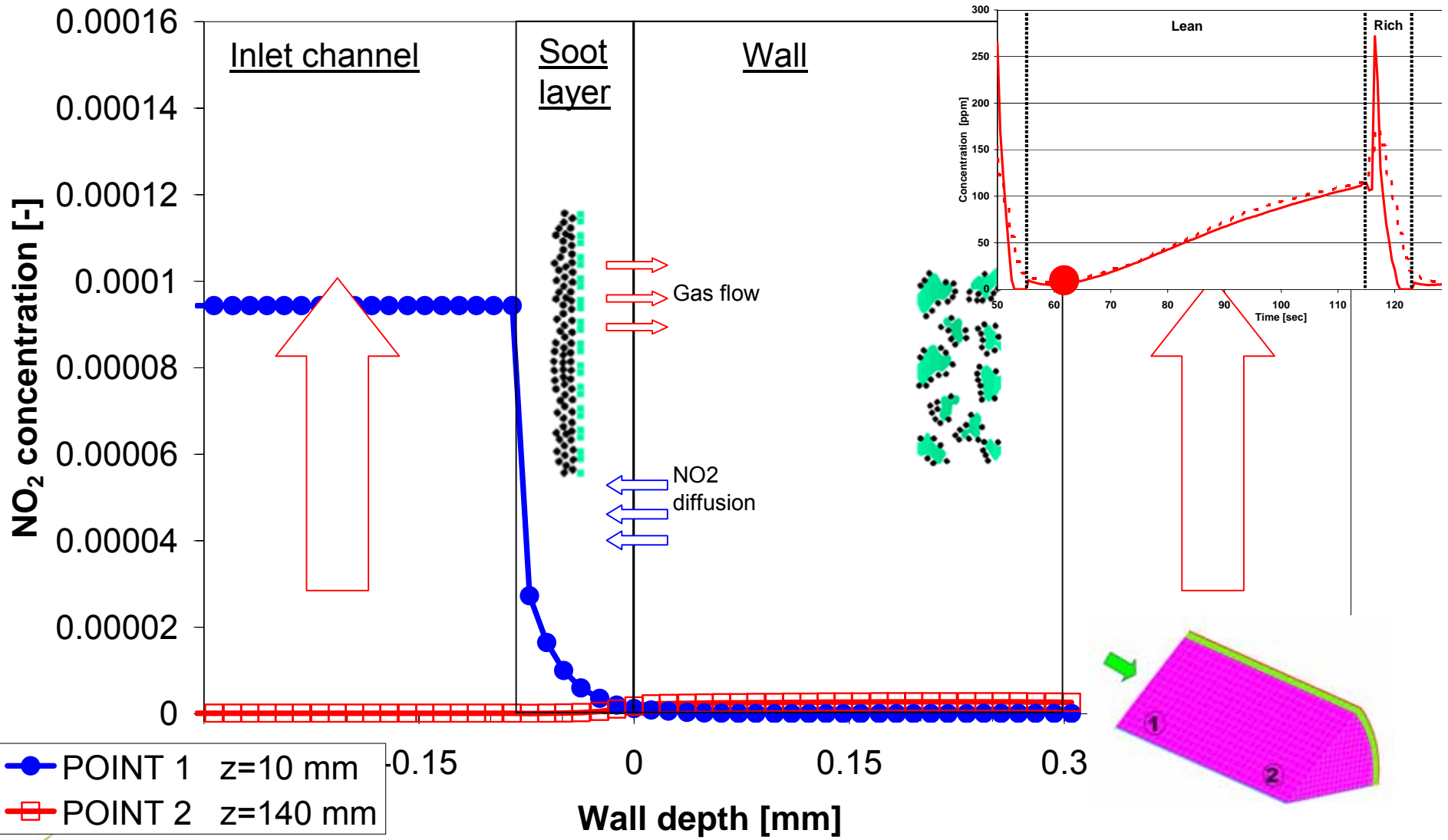
DPNR simulation example

Lean-rich cycle at 350°C



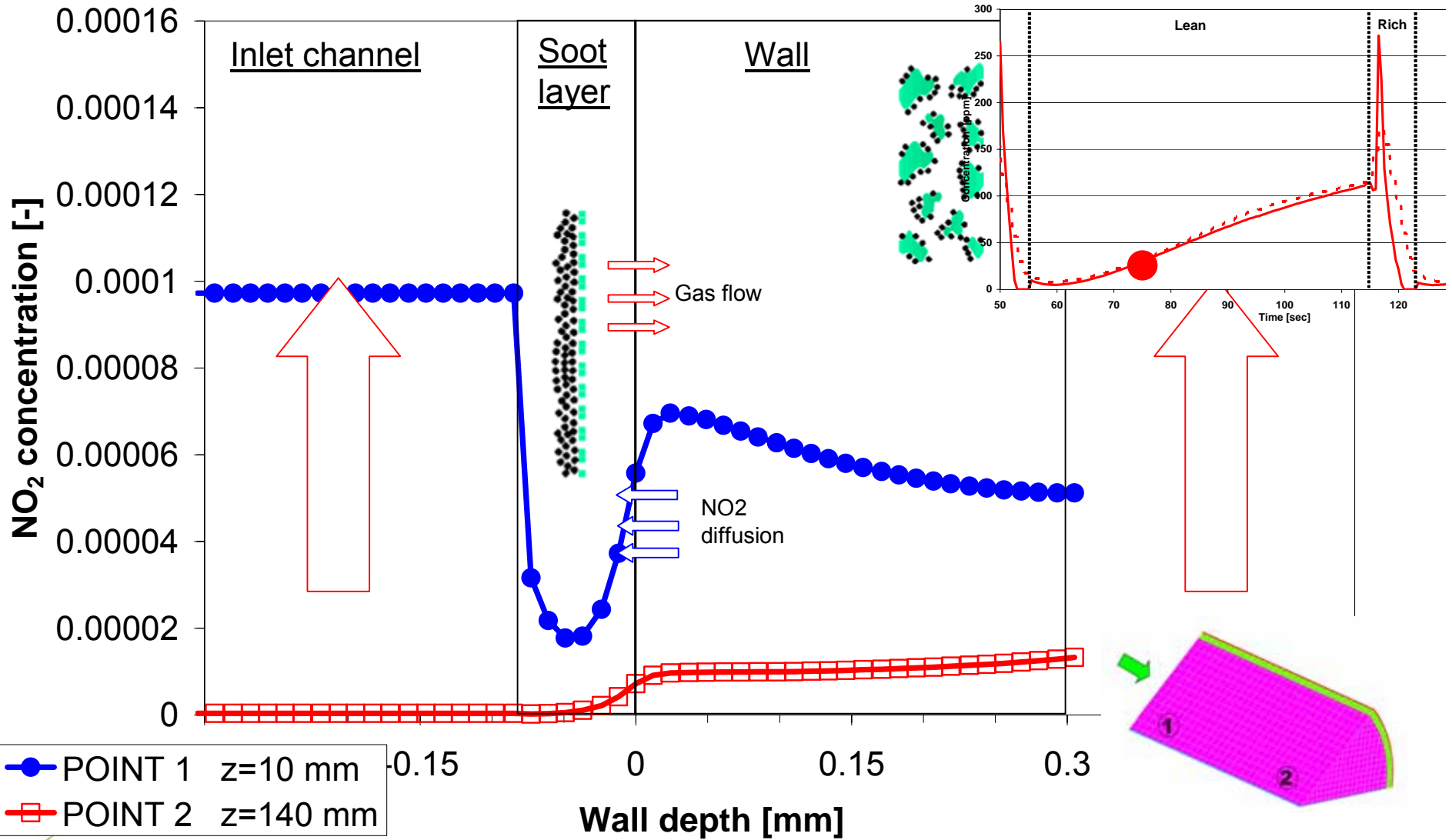
Intra-layer NO₂ profiles

t=60 s



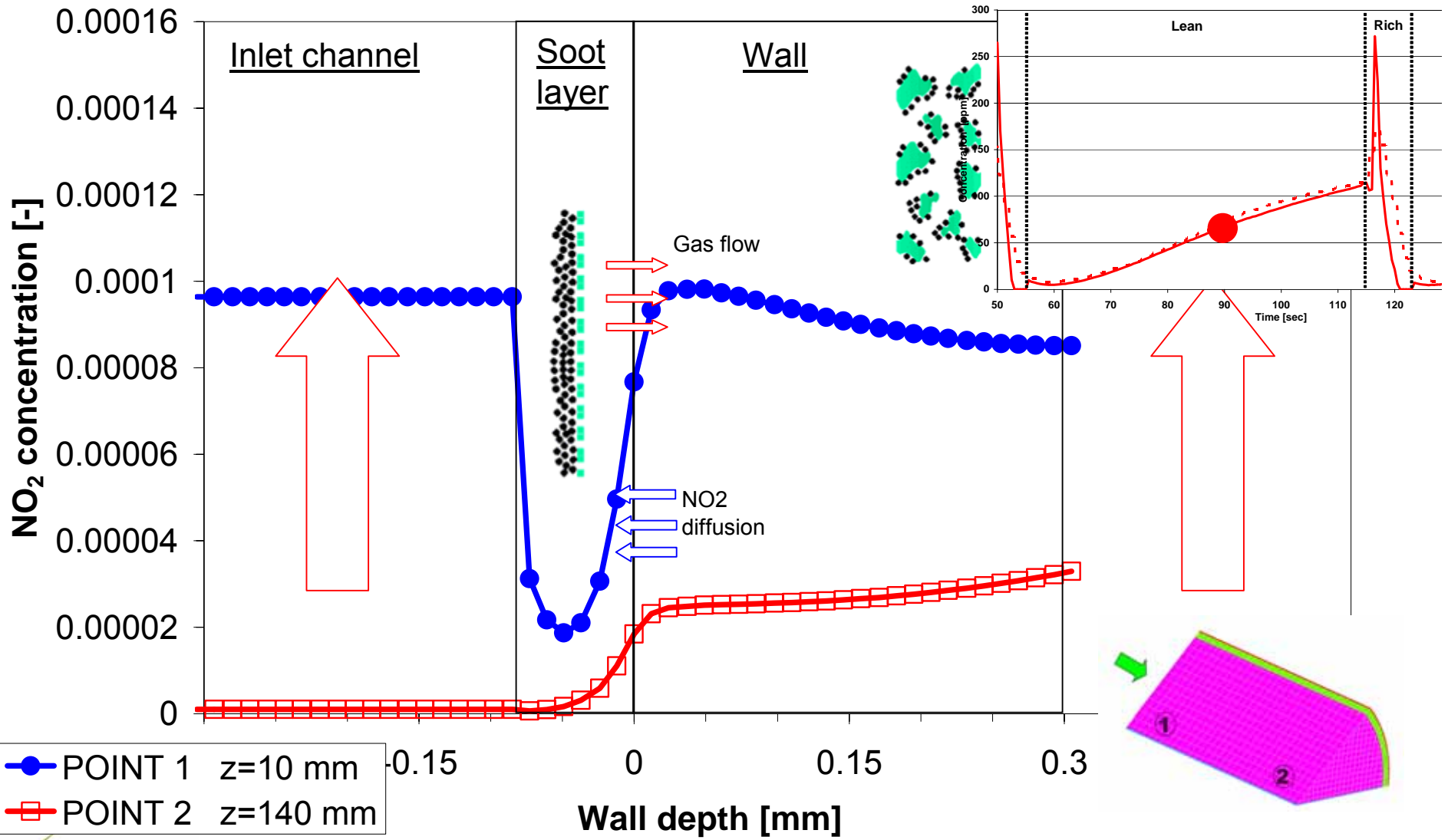
Intra-layer NO₂ profiles

t = 75 s



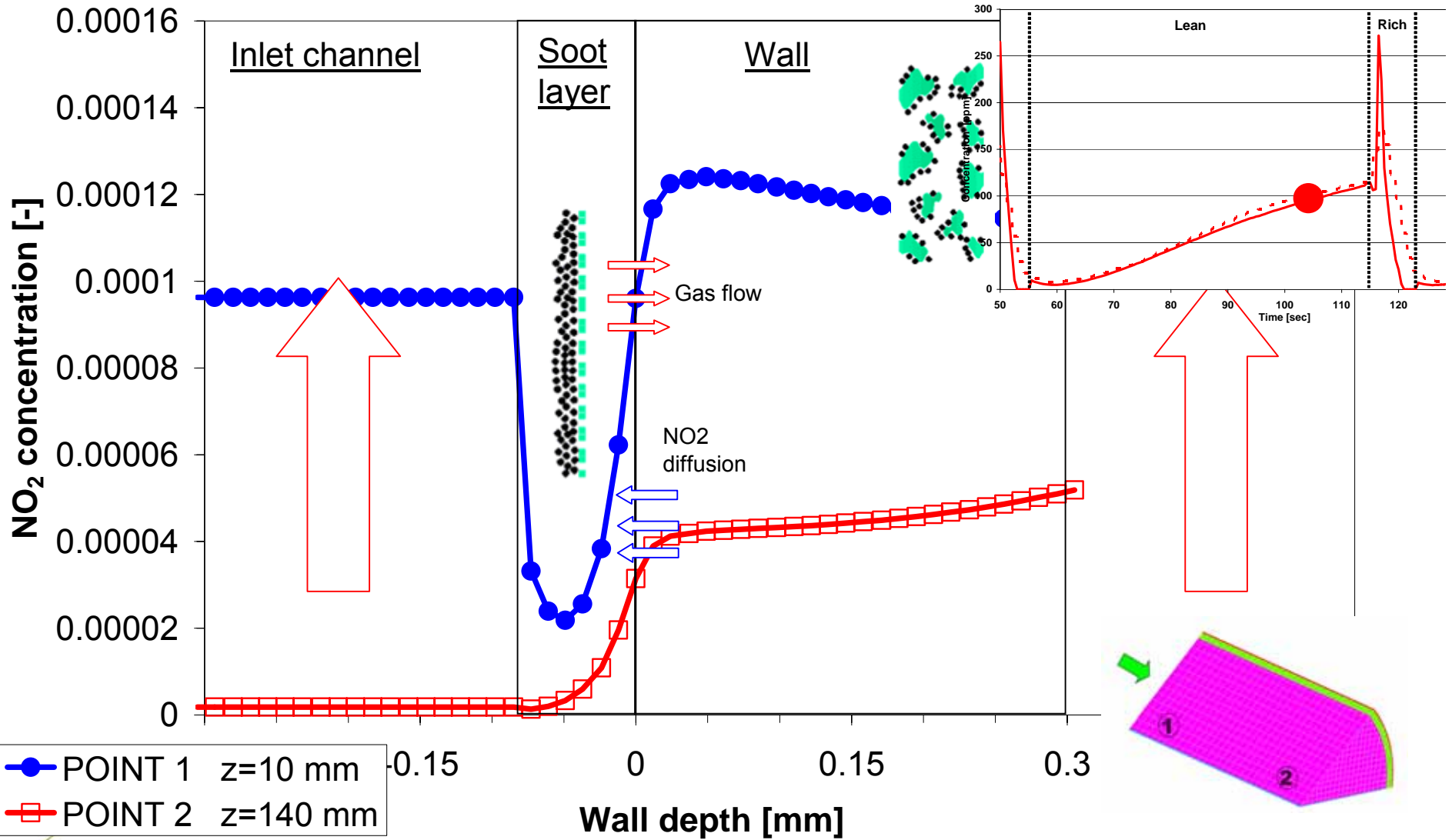
Intra-layer NO₂ profiles

t=90 s



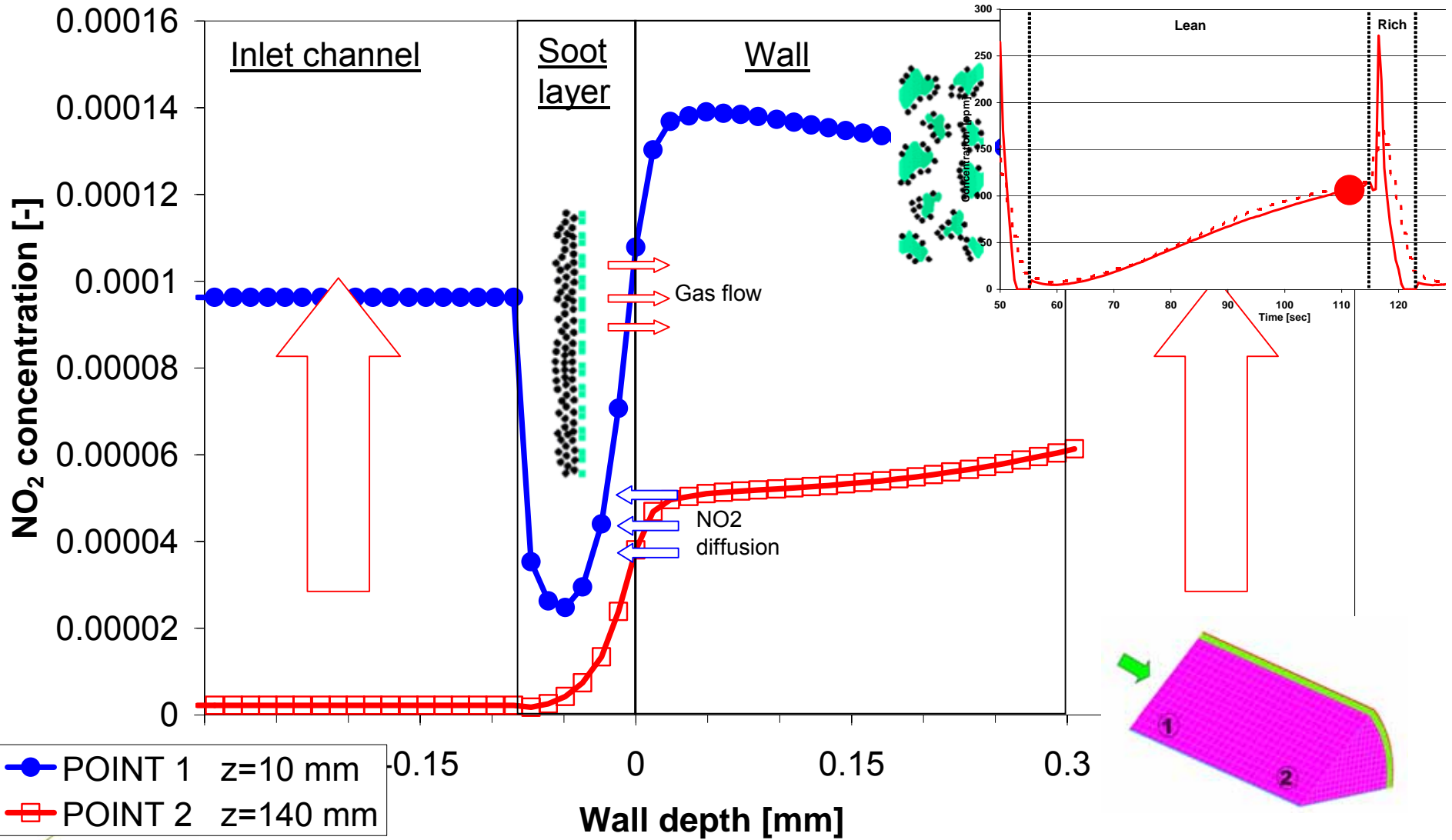
Intra-layer NO₂ profiles

t = 105 s



Intra-layer NO₂ profiles

t=114 s

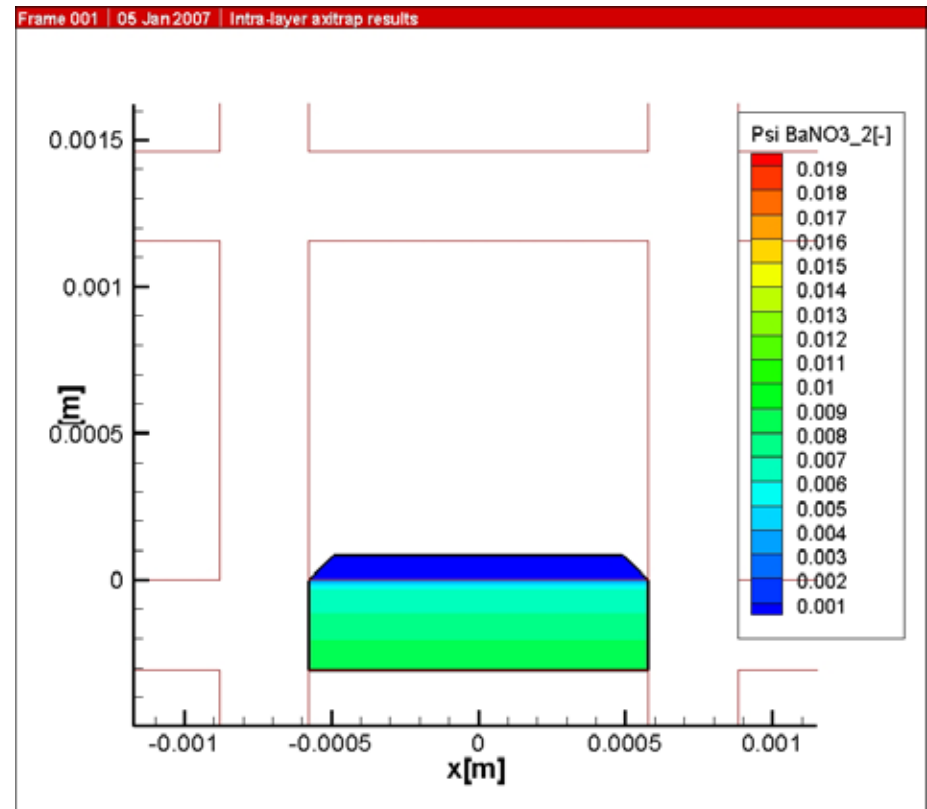
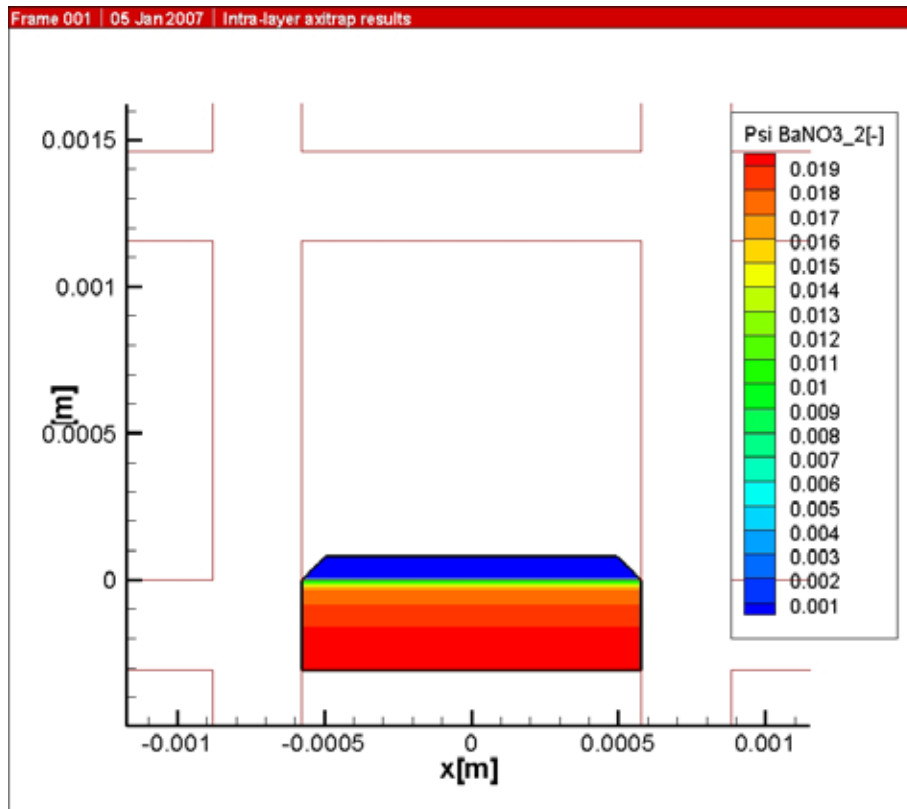


DPNR simulation example

Saturation profiles at the end of storage phase

Near filter entrance

Near filter exit



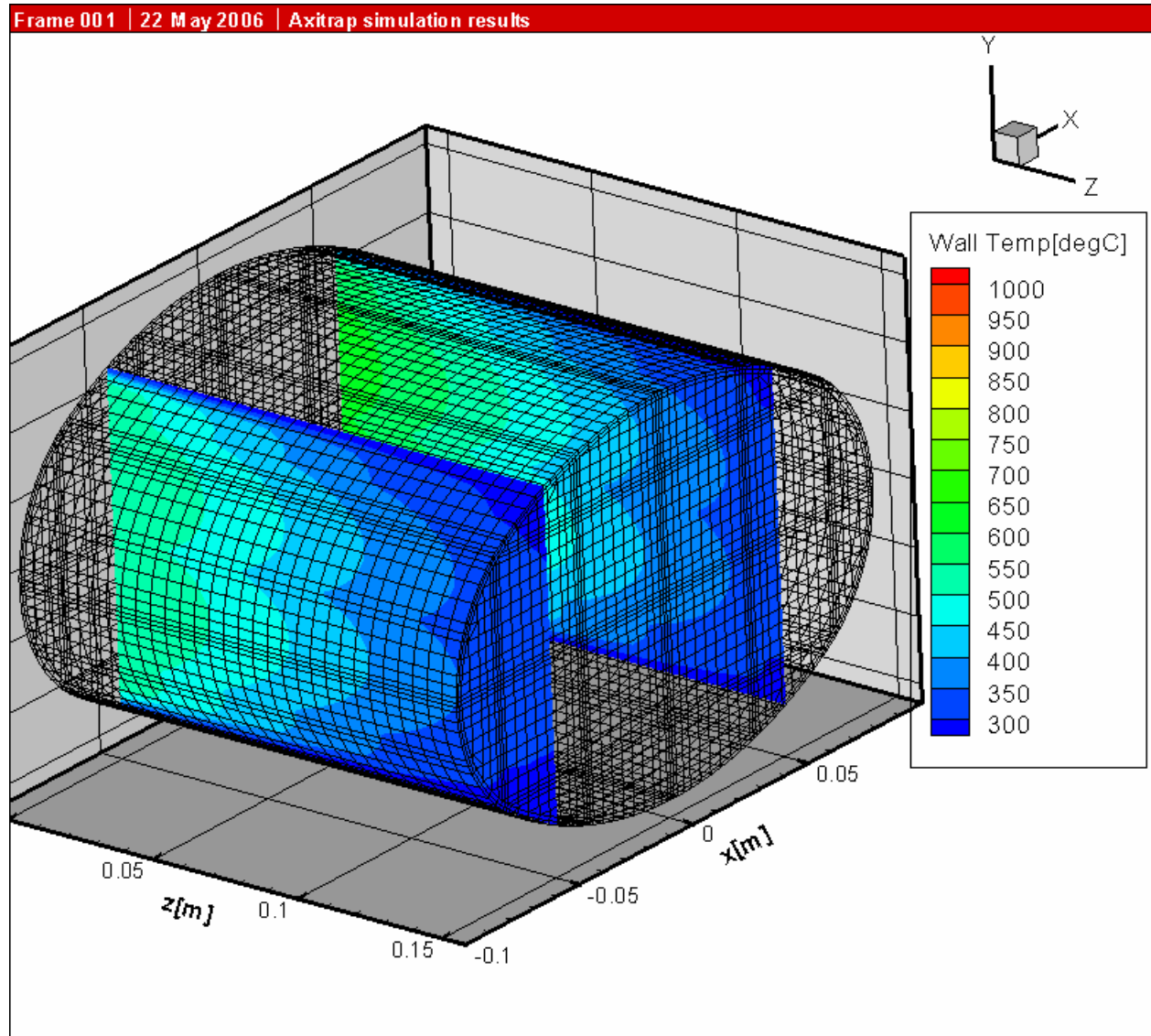


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Catalytic DPF regeneration

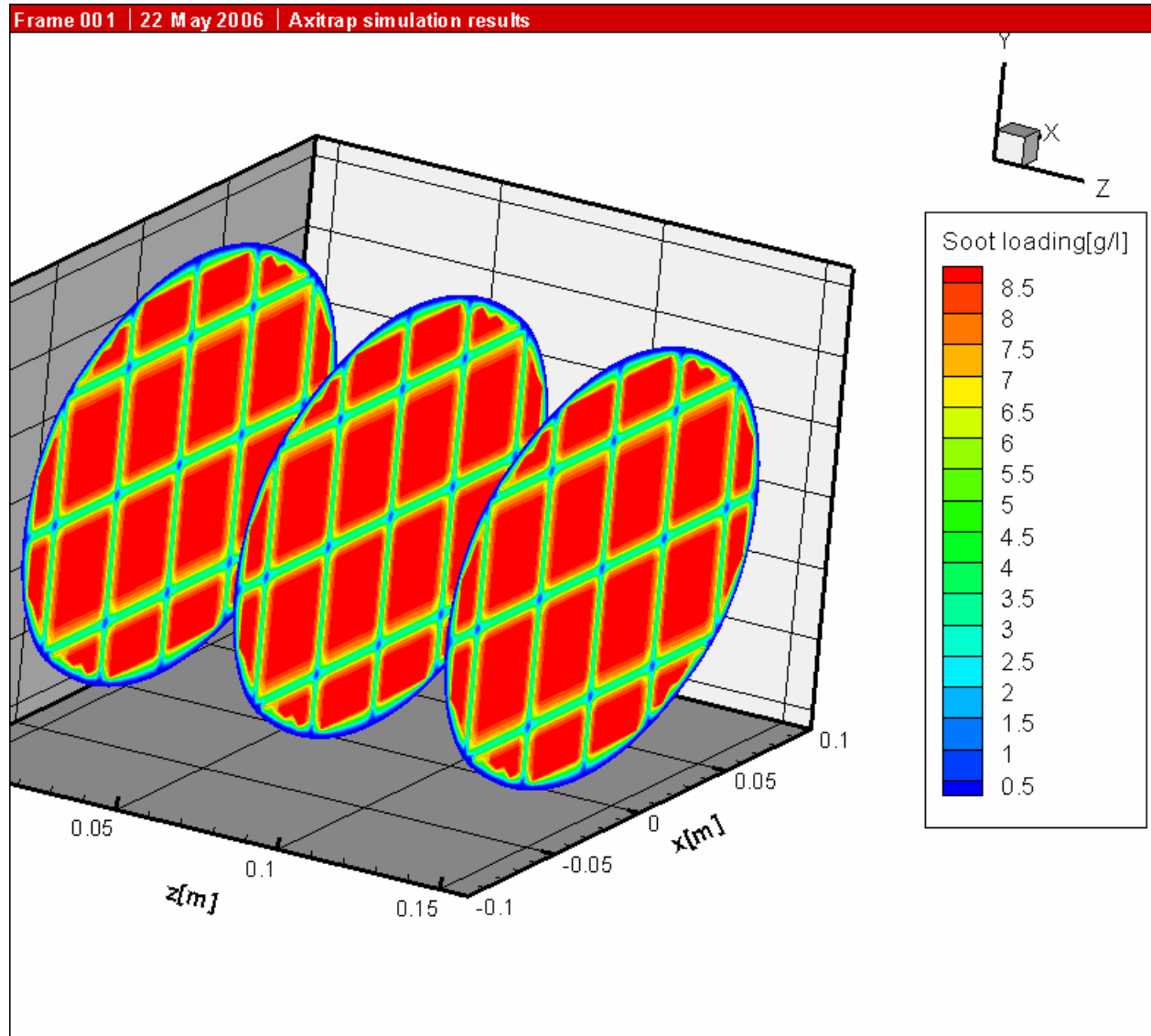
Regeneration simulation example

Filter temperature calculation



Regeneration simulation example

Soot distribution calculation

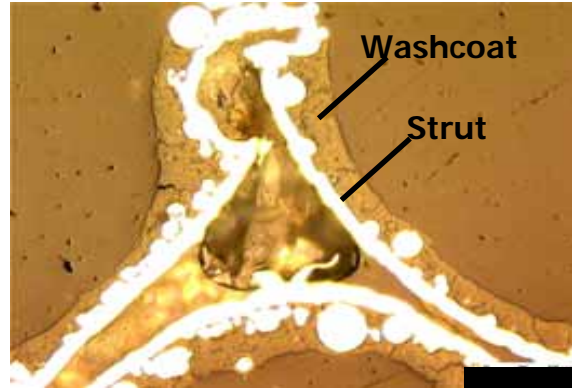
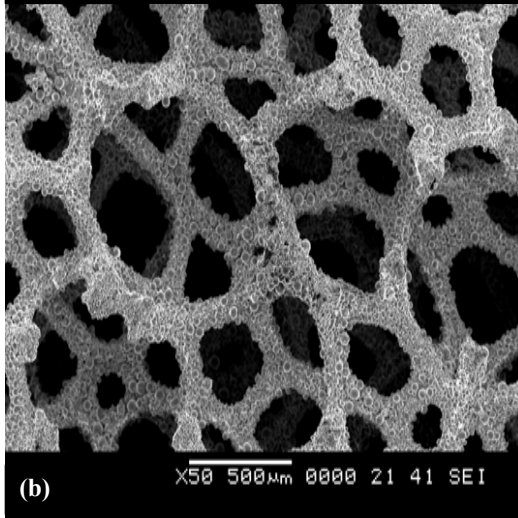
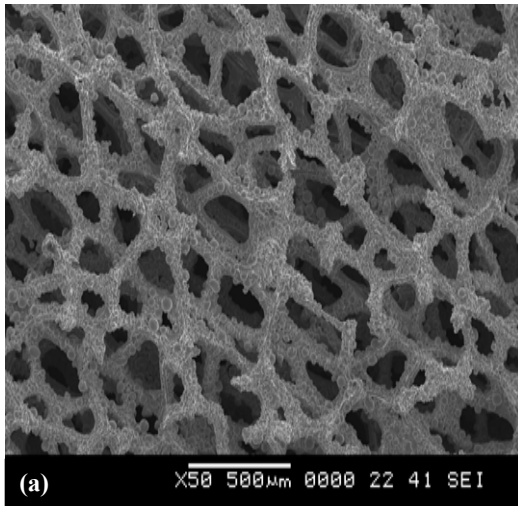




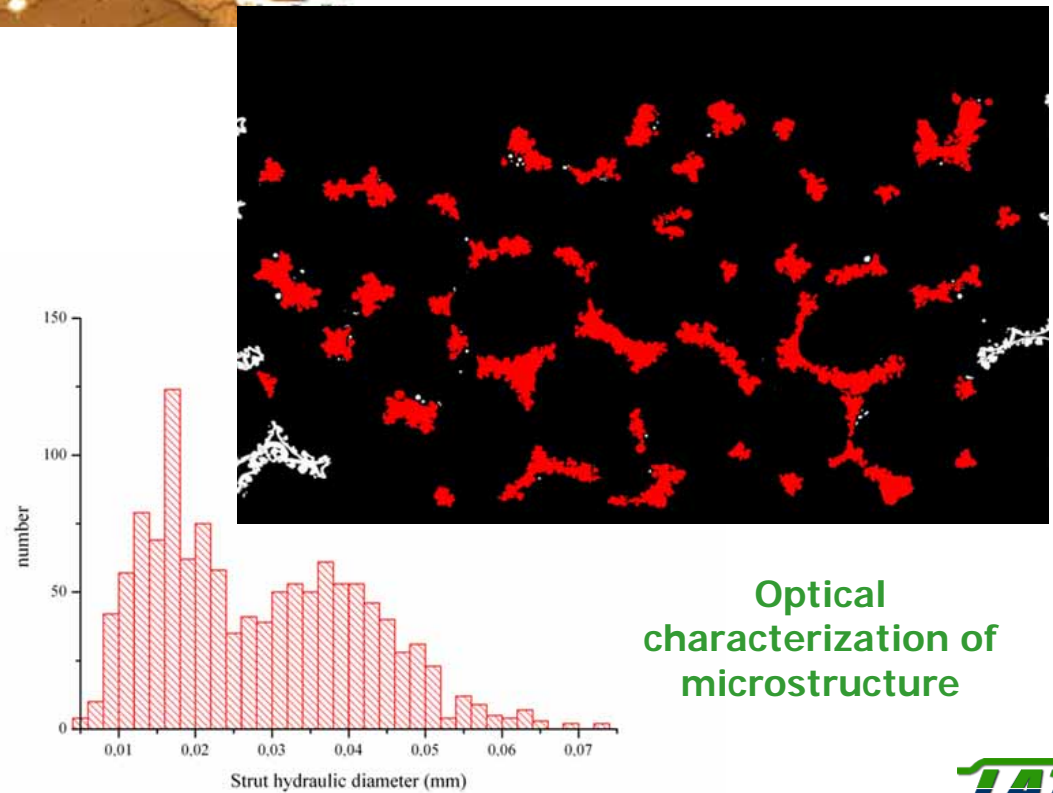
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De-NO_x Modeling on Foam Substrates

Foam morphology characterization (example with INCOFOAM® HighTemp)

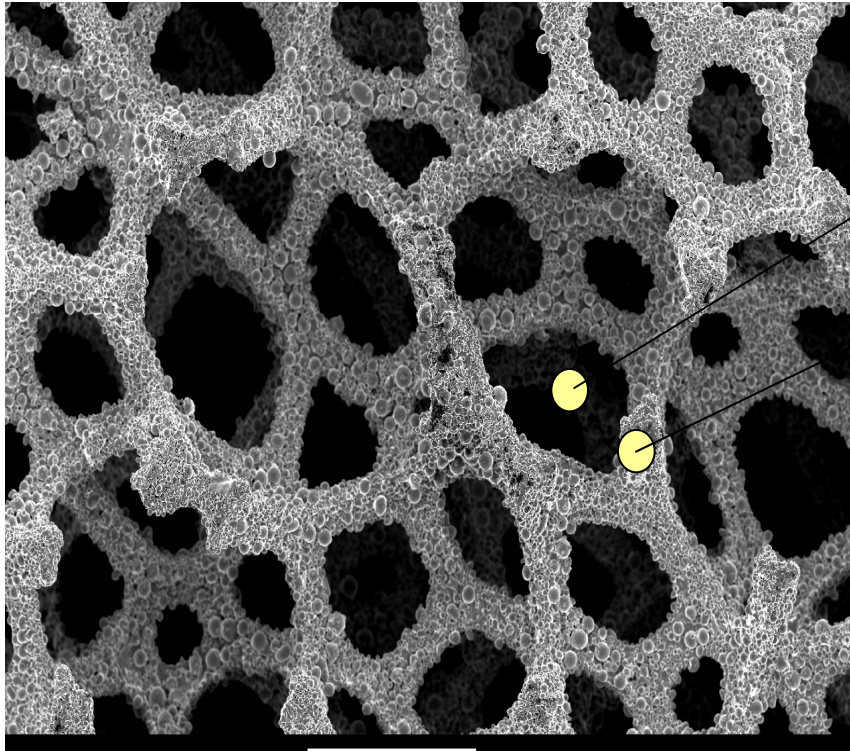


Coated foam
cross-section



Optical
characterization of
microstructure

Definitions



Gas phase concentration: c_g

Surface concentration: c_s

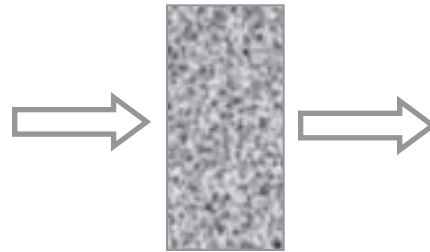
The catalytic reaction rates
are functions of c_s

$$R_1 = \frac{A_1 \cdot e^{-E_1/RT} \cdot c_{CO} \cdot c_{O_2}}{G_2}$$

Inhibition term depending on
surface species concentrations

1-d modeling: Transport/Reaction

Axial flow concept



Gas energy balance

$$\rho_g v_g \frac{\partial T_g}{\partial x} = h \cdot \left(\frac{S}{\varepsilon} \right) \cdot (T_g - T_s)$$

Gas species balance

$$\frac{\partial (v_g c_g)}{\partial x} = k_j \cdot \left(\frac{S}{\varepsilon} \right) \cdot (c_{g,j} - c_{s,j})$$

Transient energy balance

$$\underbrace{\rho_s C_{p,s} \frac{\partial T_s}{\partial t}}_{\text{Solid heat capacity}} = \underbrace{\lambda_s \frac{\partial^2 T_s}{\partial x^2}}_{\text{Conduction}} + \underbrace{h \left(\frac{S}{1-\varepsilon} \right) (T_g - T_s)}_{\text{Convection}} - \underbrace{\frac{1}{1-\varepsilon} \sum_{k=1}^{n_k} \Delta H_k R_k}_{\text{Reaction heat}}$$

$$\frac{\rho_g}{M_g} k_j \left(\frac{S}{\varepsilon} \right) (c_{g,j} - c_{s,j}) = R_j$$

Mass-transfer rate = reaction rate

Heat/mass transfer coefficients

Heat transfer coefficient

$$h = \frac{Nu \cdot k_g}{d_s}$$

$$Re = \frac{\rho_{gas} \cdot v_f \cdot d_s}{\eta_{gas}}$$

$$Nu = A \cdot Re^{0.43} \cdot Pr^{1/3}$$

$$Pr = \frac{\eta_g C_{p,g}}{k_g}$$

Mass transfer coefficient

$$k_j = \frac{Sh \cdot D_j}{d_s}$$

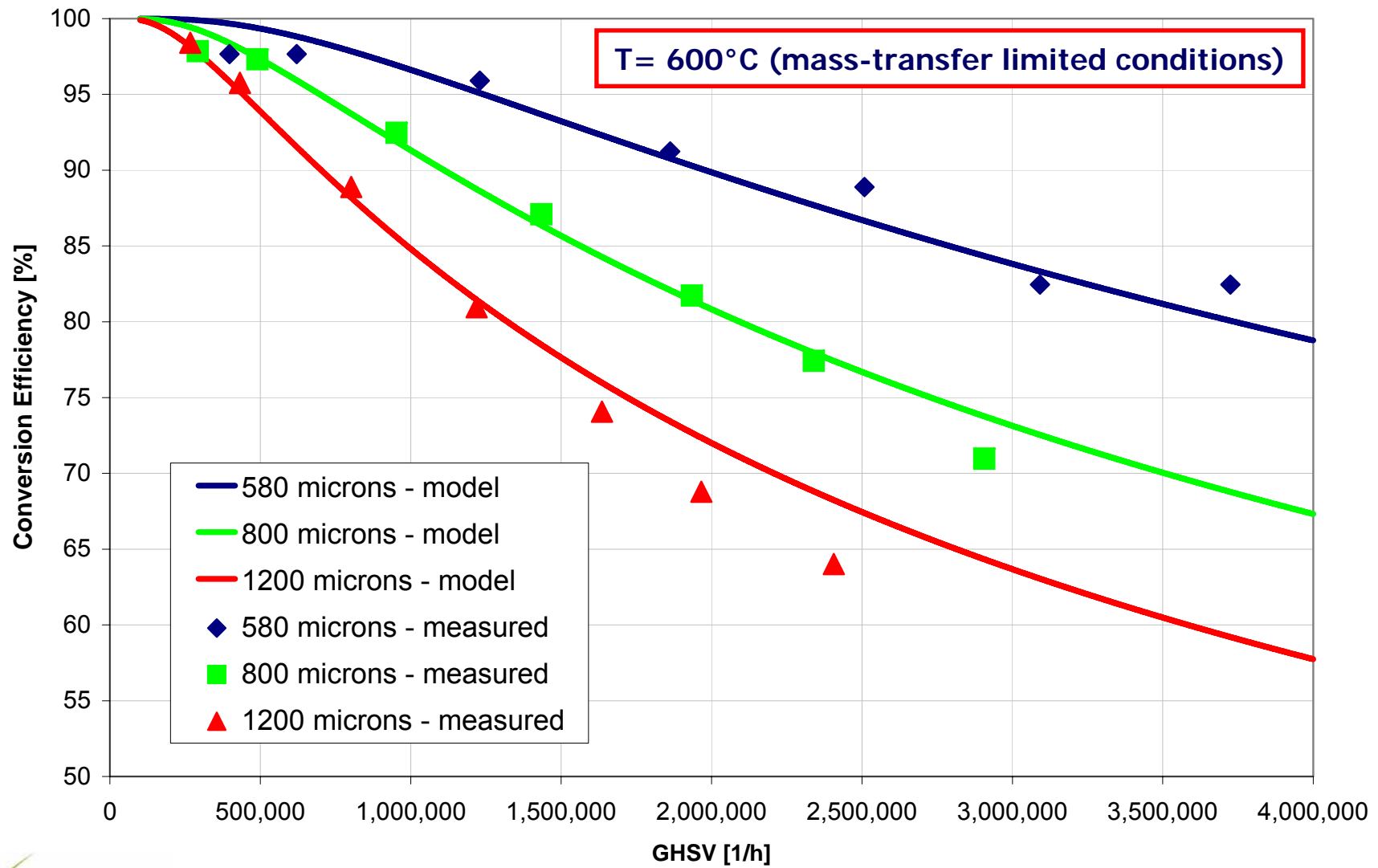
$$Sh_i = A \cdot Re^{0.43} \cdot Sc_i^{1/3}$$

$$Sc_i = \frac{\eta_g}{\rho_g \cdot D_i}$$

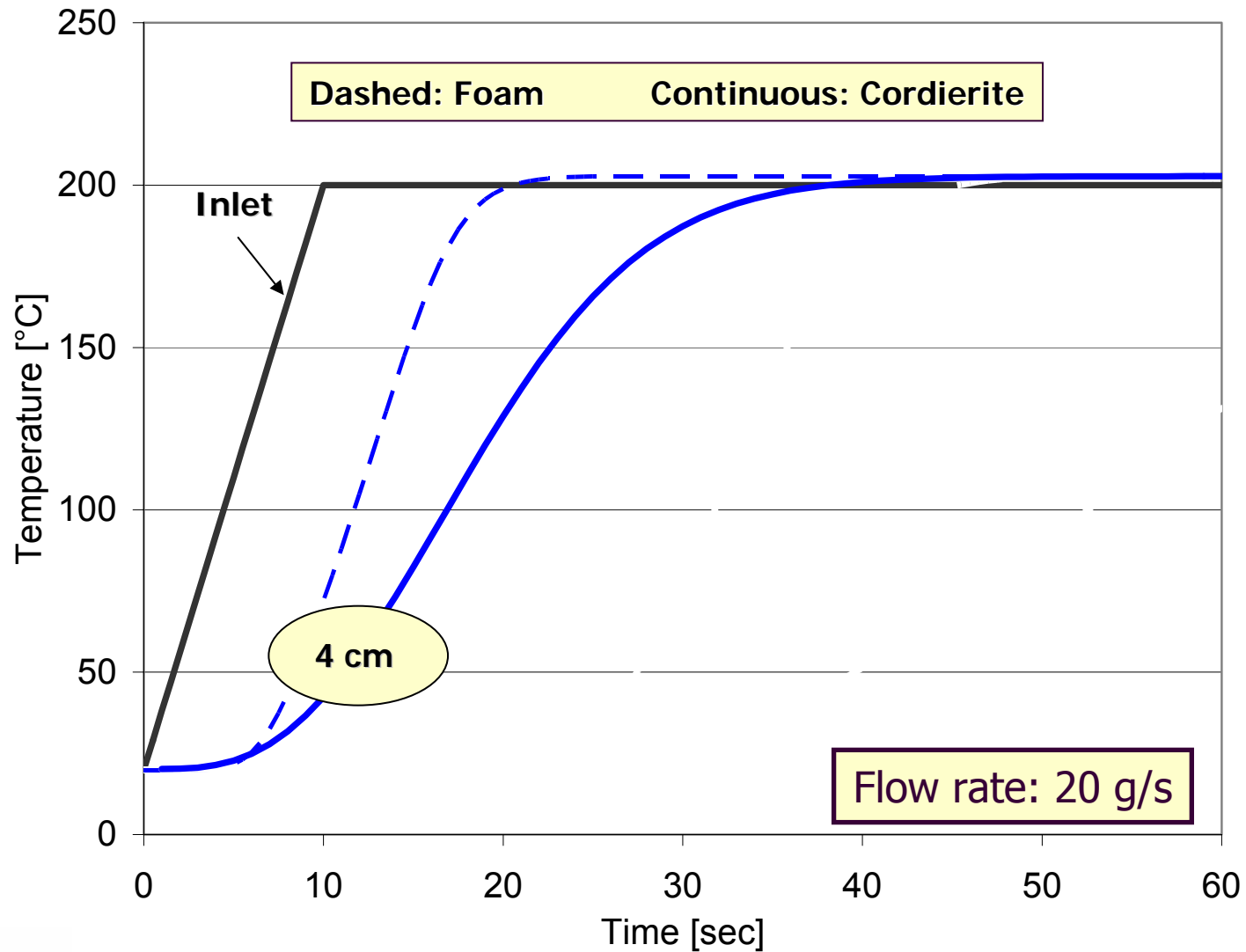
Parameter to be calibrated from experiments

D_j	Species diffusivity
ρ_{gas}	Gas density
v_f	Face velocity
d_s	Mean strut diameter
η_{gas}	Dynamic gas viscosity

Foam model calibration

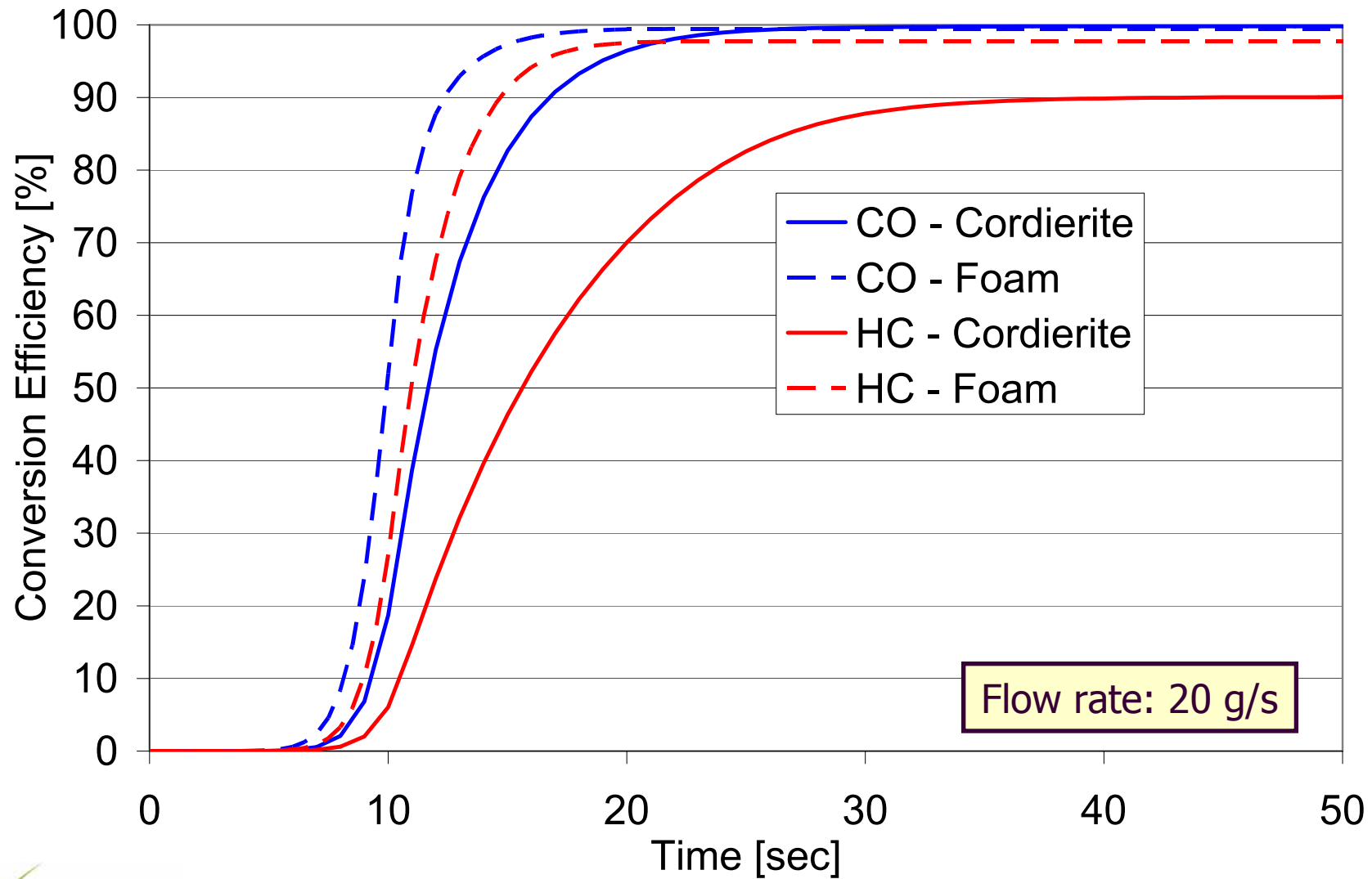


Temperature response modeling study Foam 1200 microns vs Cordierite 400 cpsi

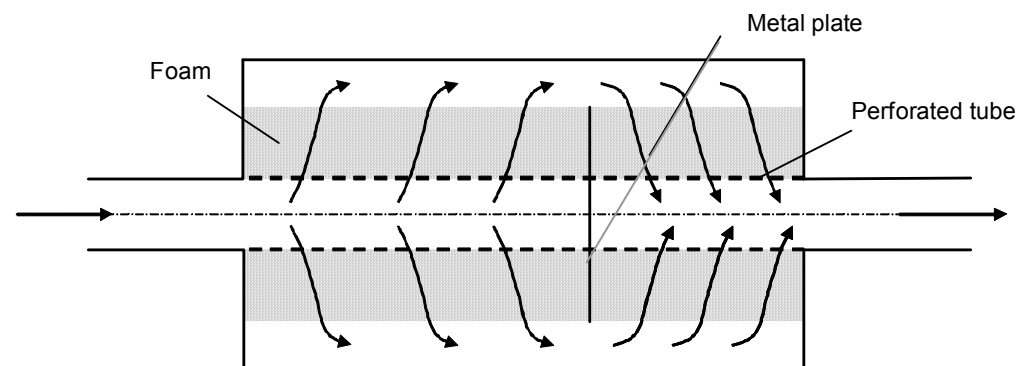
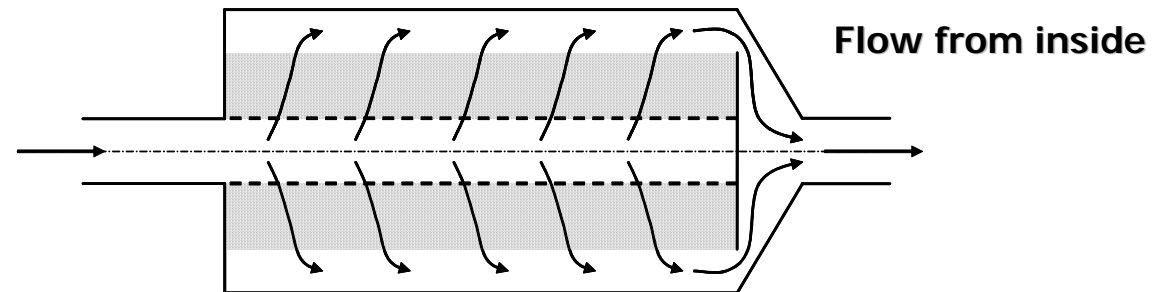
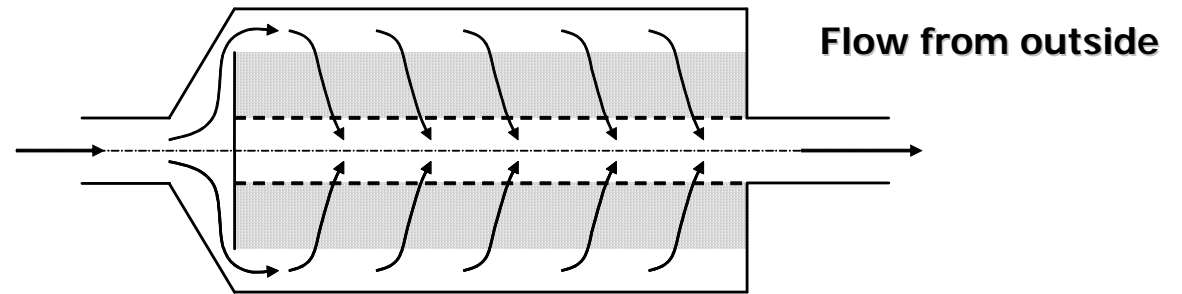


CO, HC conversion efficiency vs time

Length: 4 cm

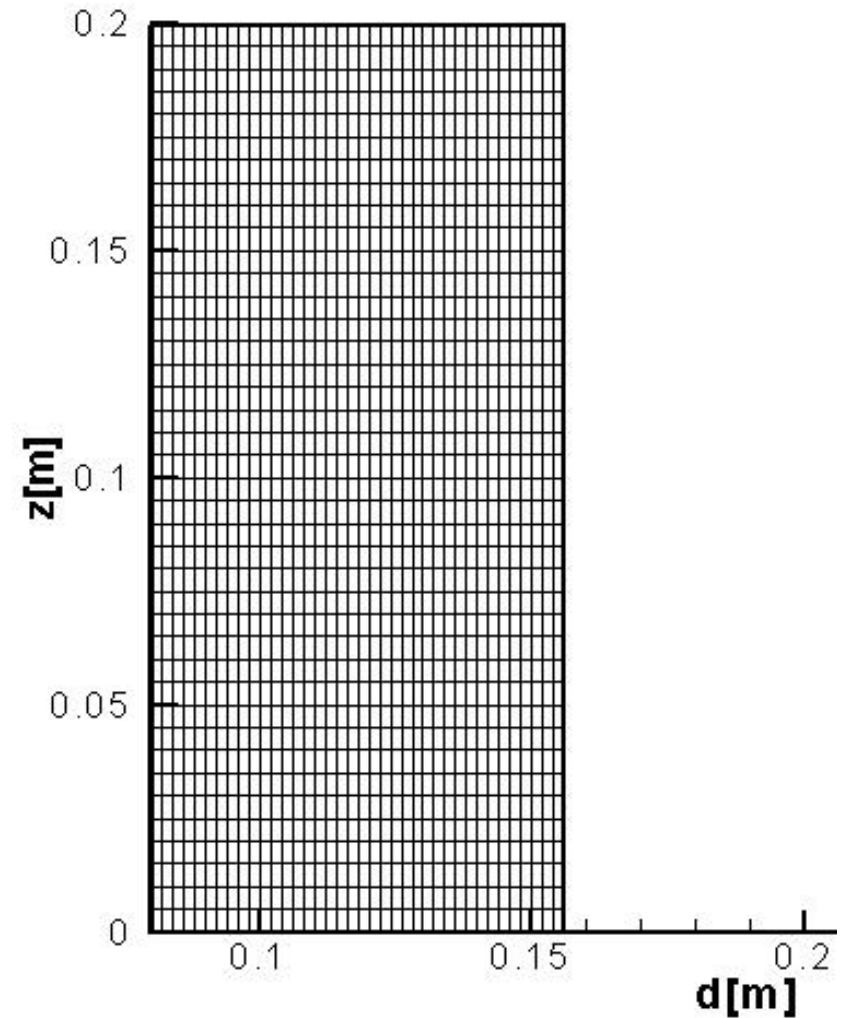


2-d modeling "Radial flow", "Cross flow" designs



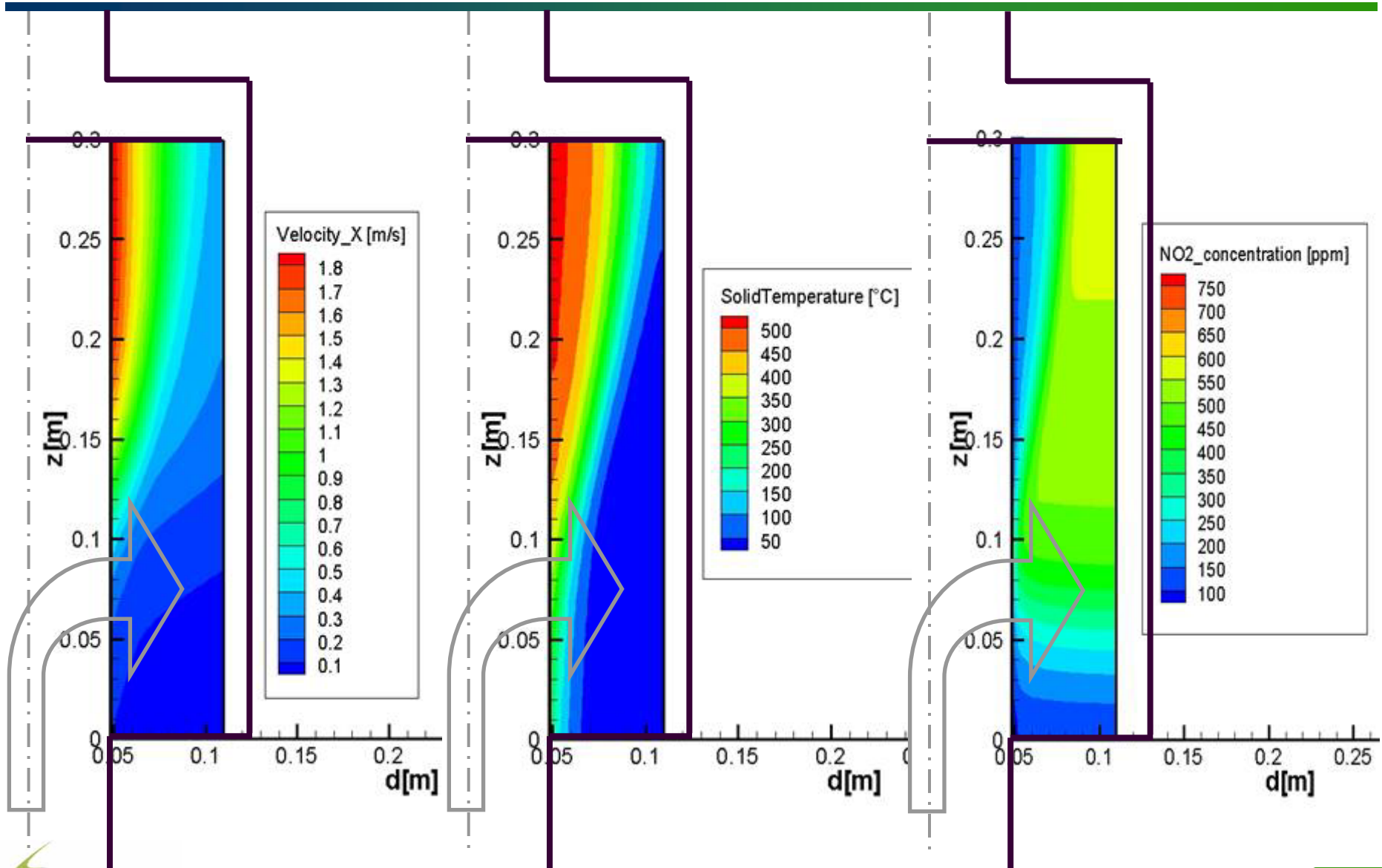
2-d modeling for “radial-flow” or “cross-flow” designs

- Solution of
 - ◆ Mass balance
 - ◆ Momentum balance
 - ◆ Energy balance
 - ◆ Species balance
- The filtration equations are also applied in each node
- The equations are solved in the gas channels and the foam phase



Transient 2-d simulation of foam catalyst warm-up

Time = 5 s

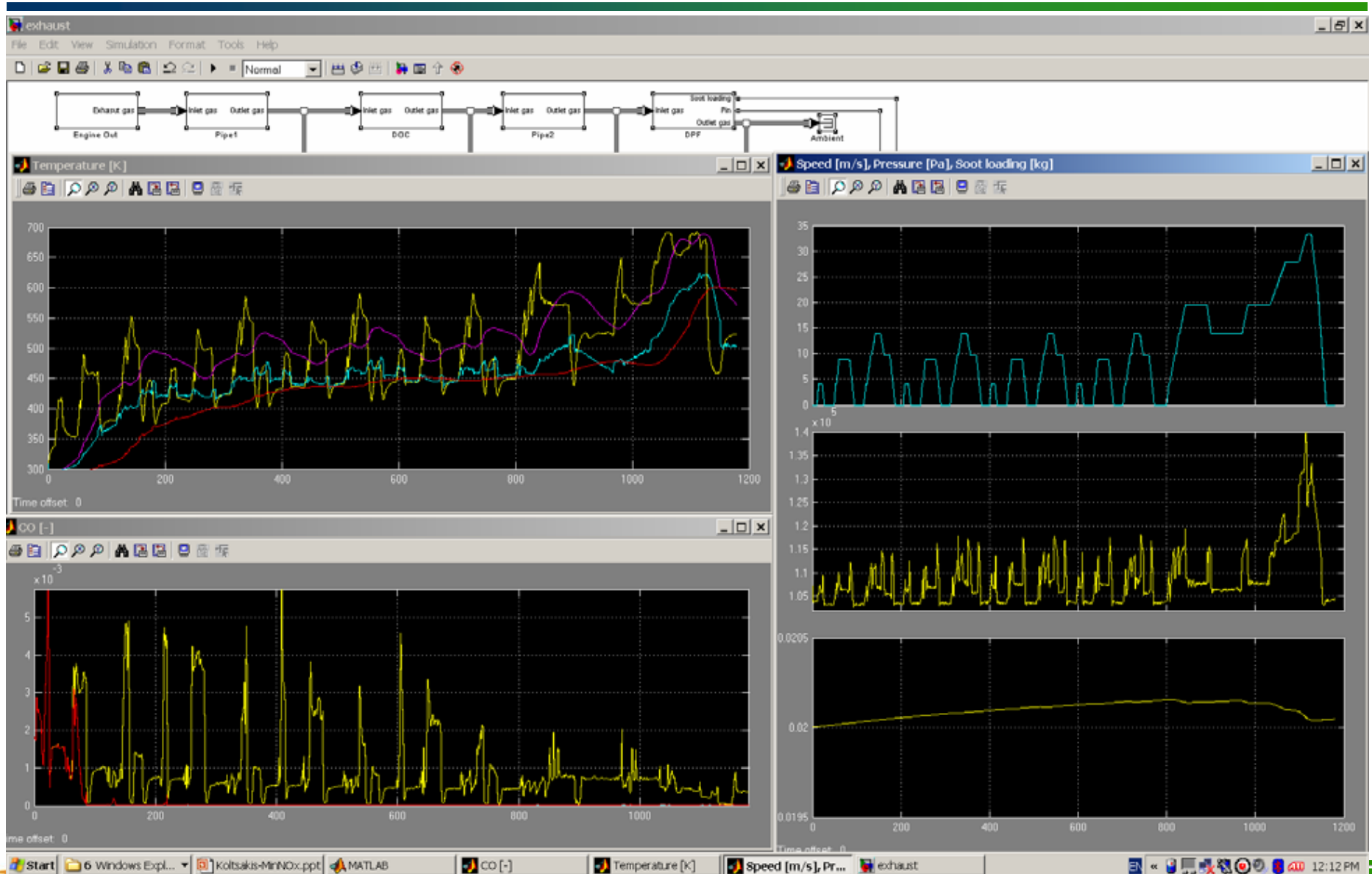




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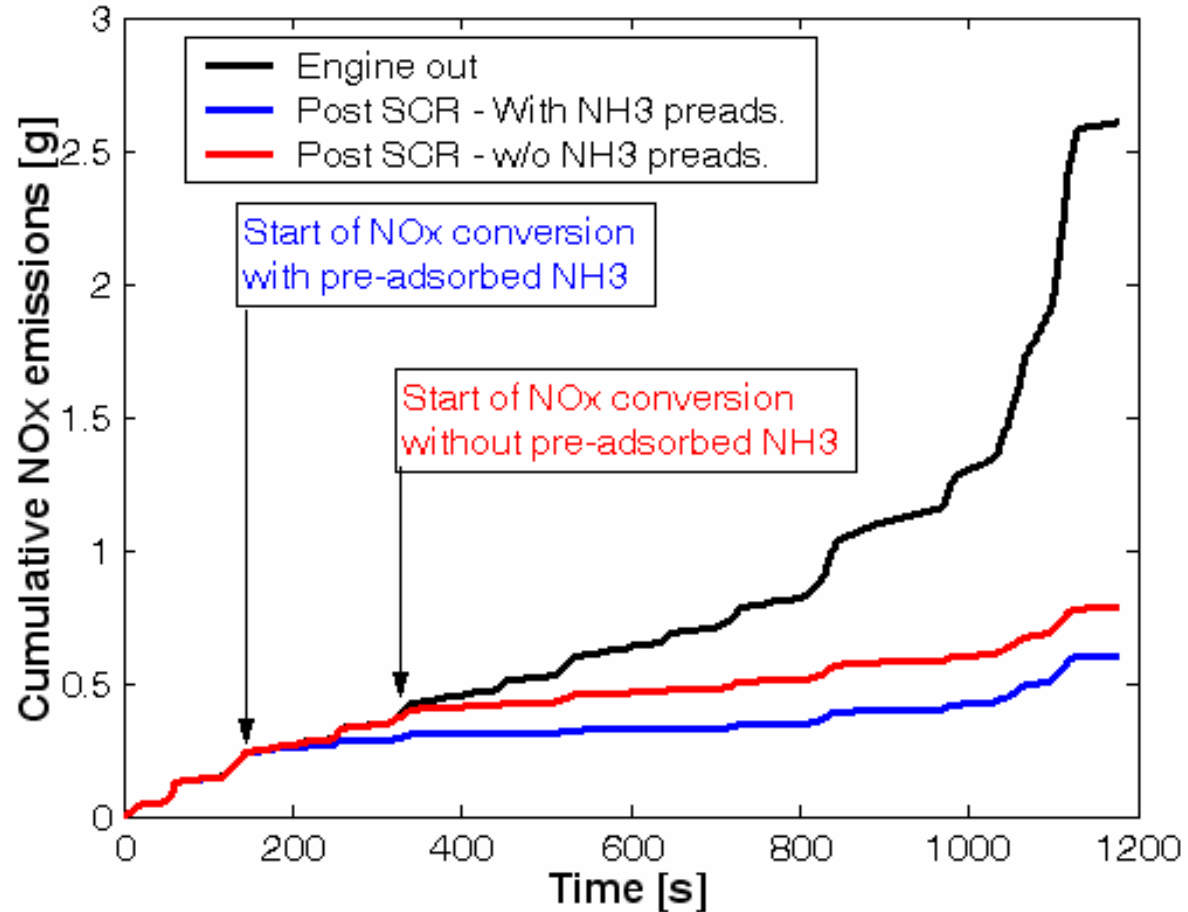
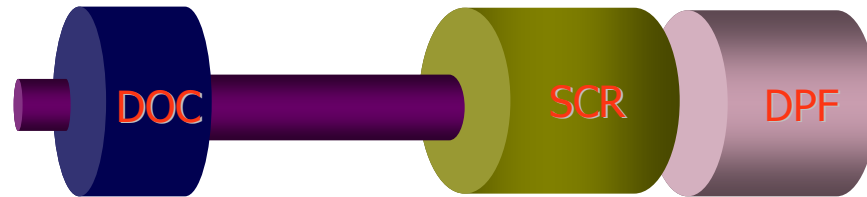
Integrated exhaust line simulation

System simulation in MATLAB/SIMULINK environment



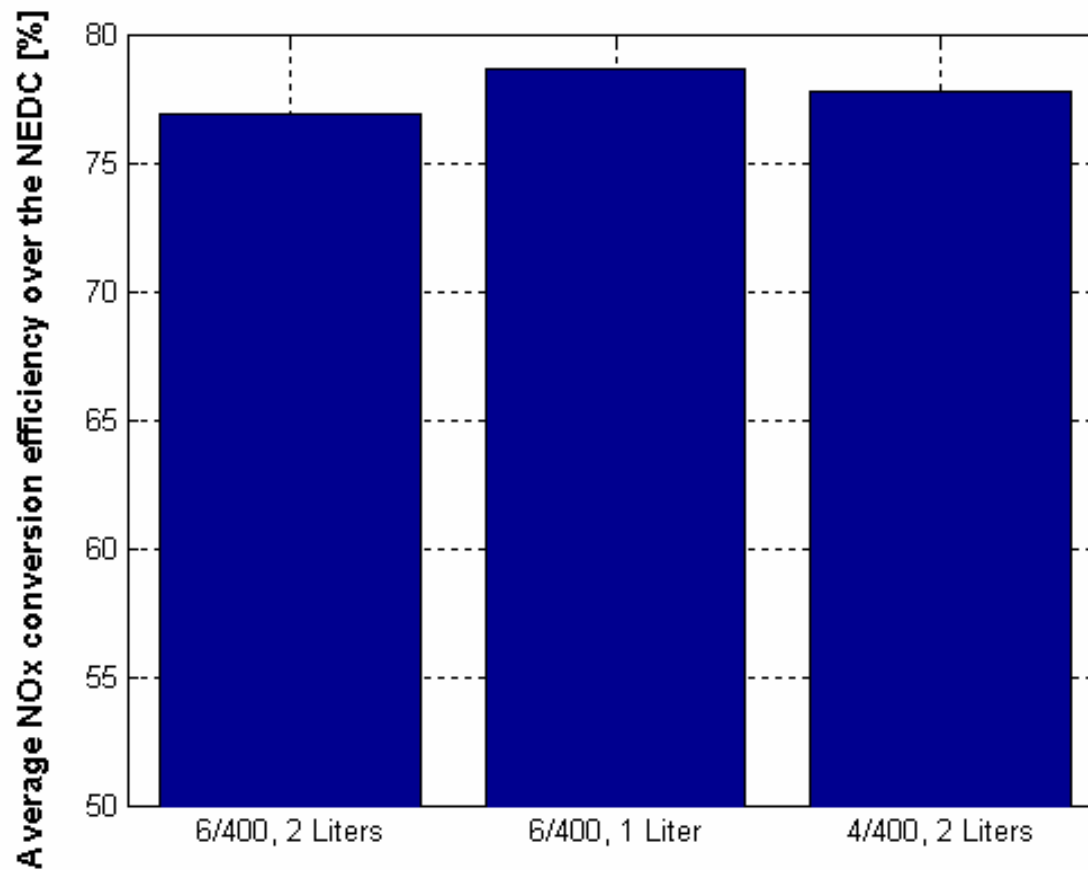
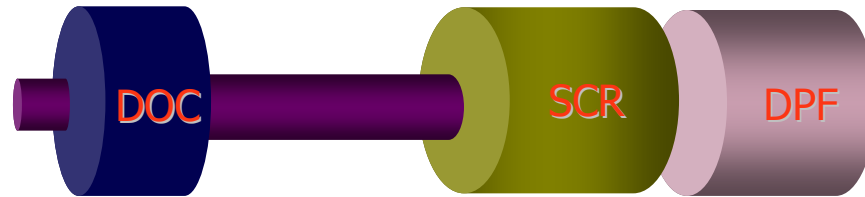
Reactors in series

Effect of NH_3 pre-adsorption



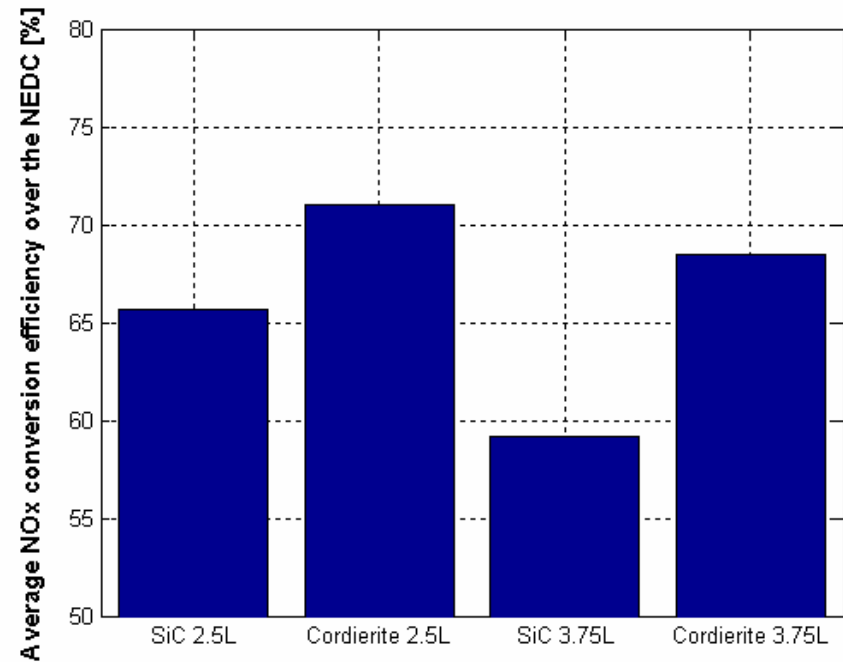
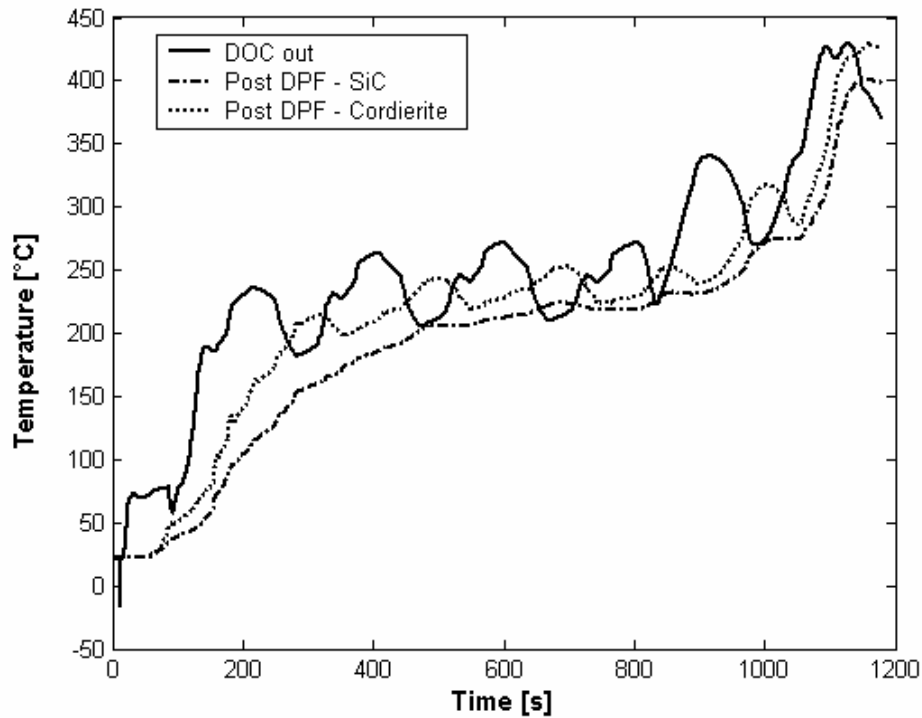
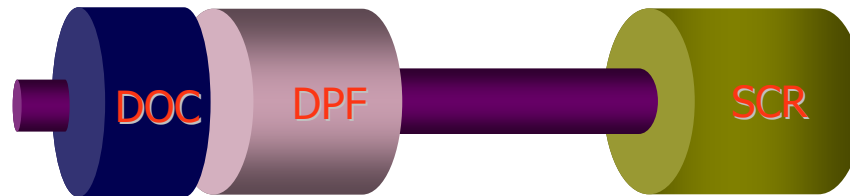
Reactors in series

Effect of DOC geometry

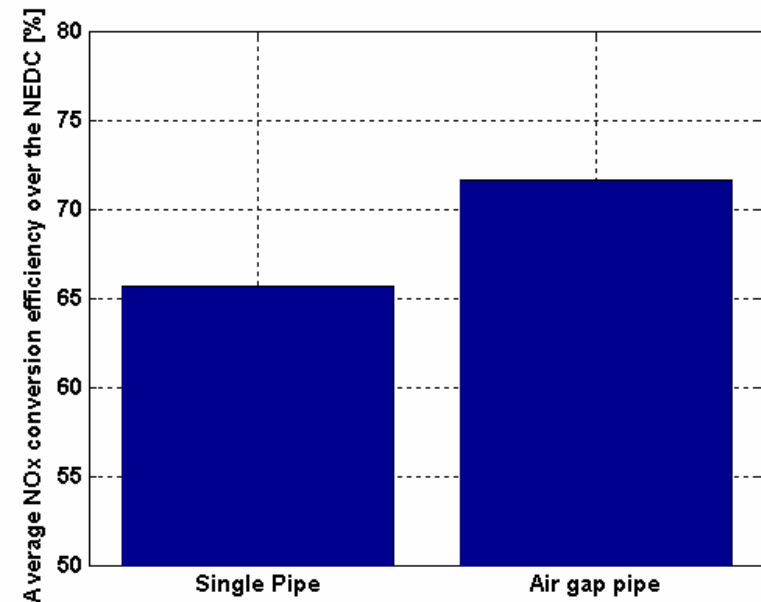
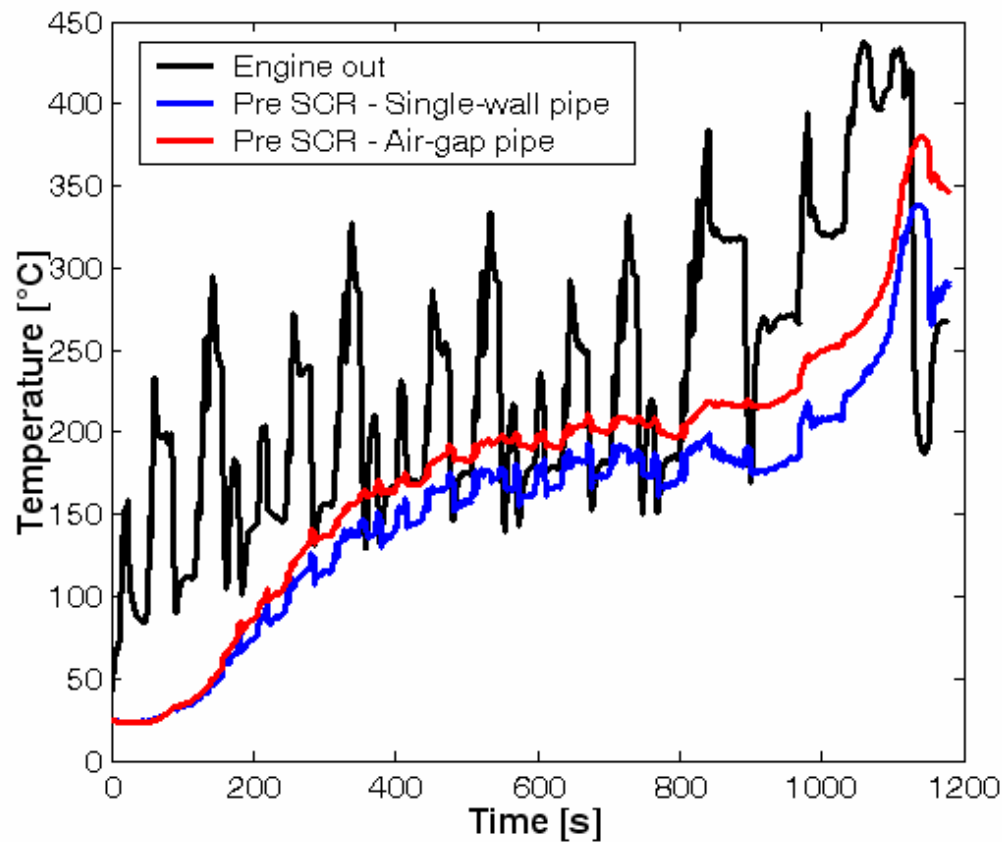
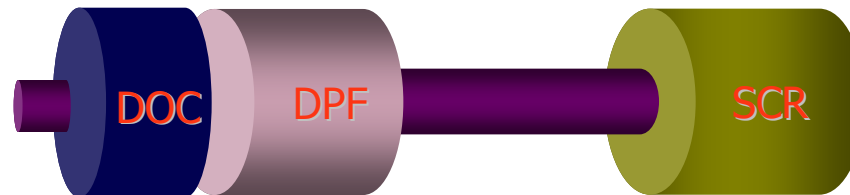


Reactors in series

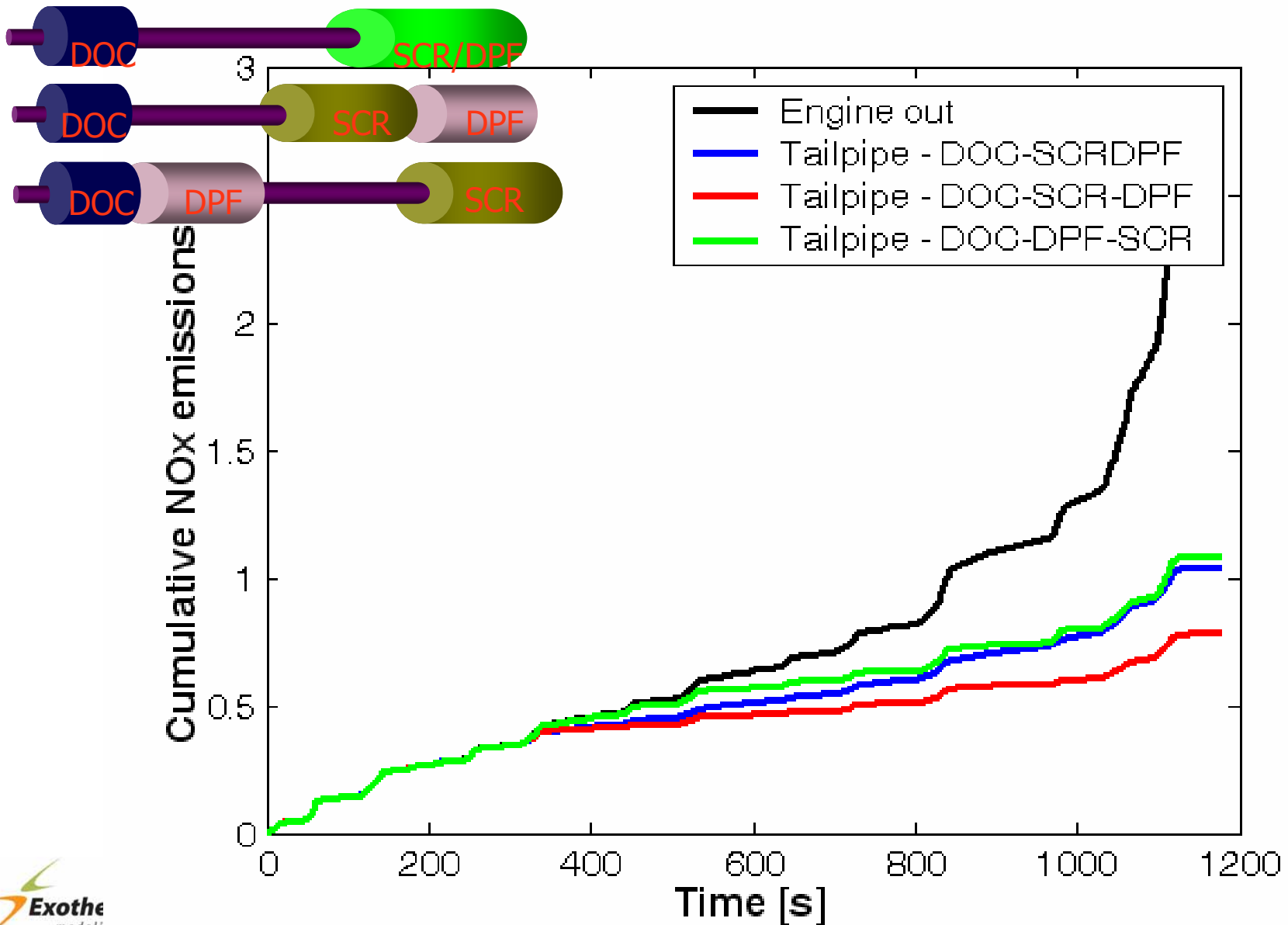
Effect of DPF size, material



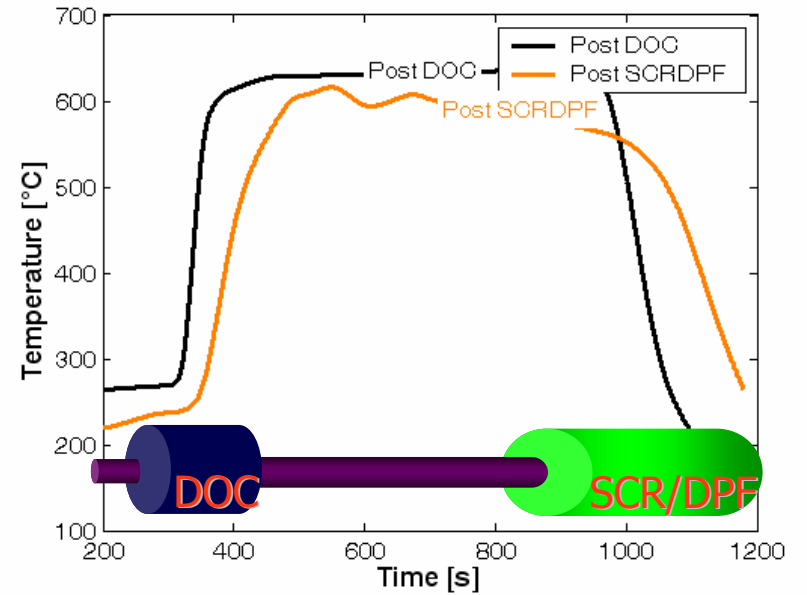
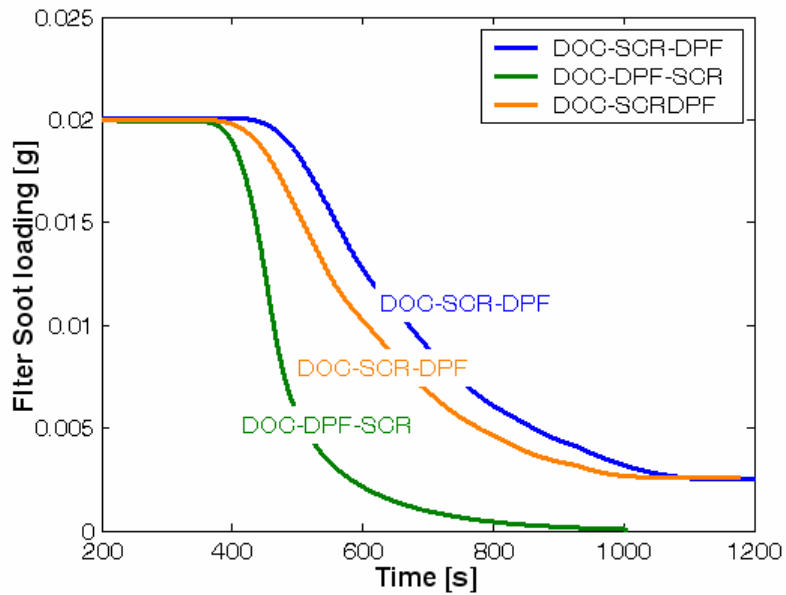
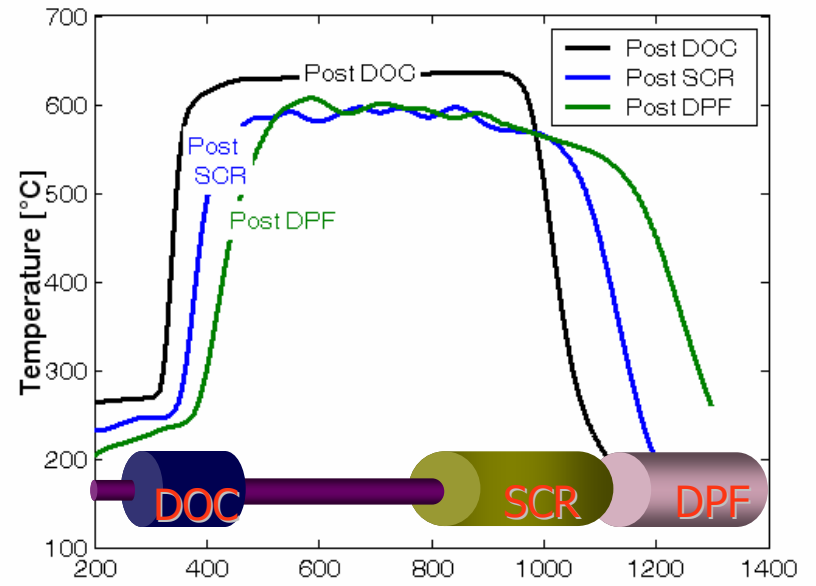
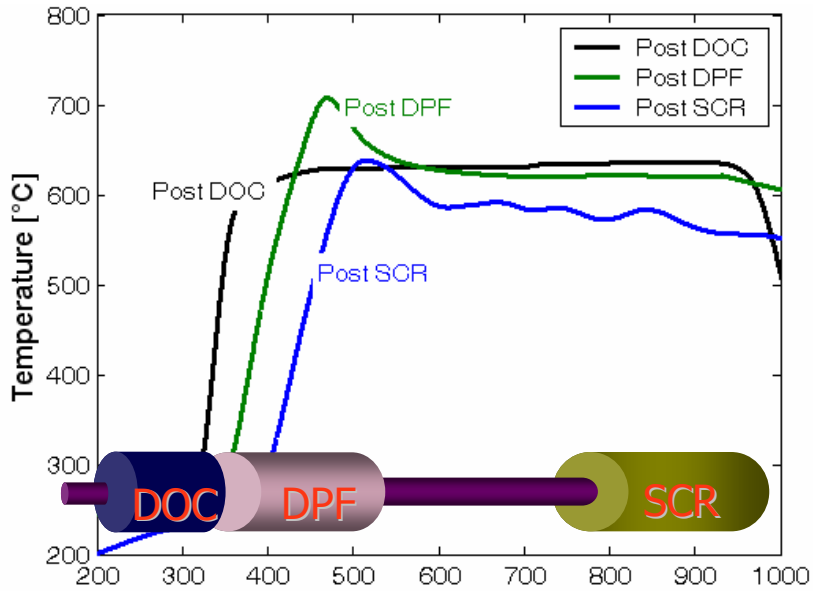
Effect of pipe insulation



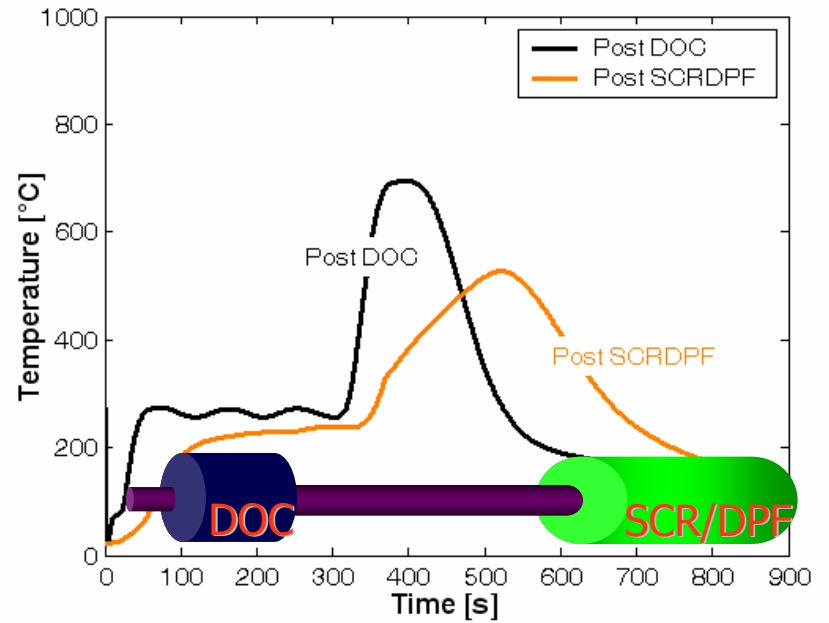
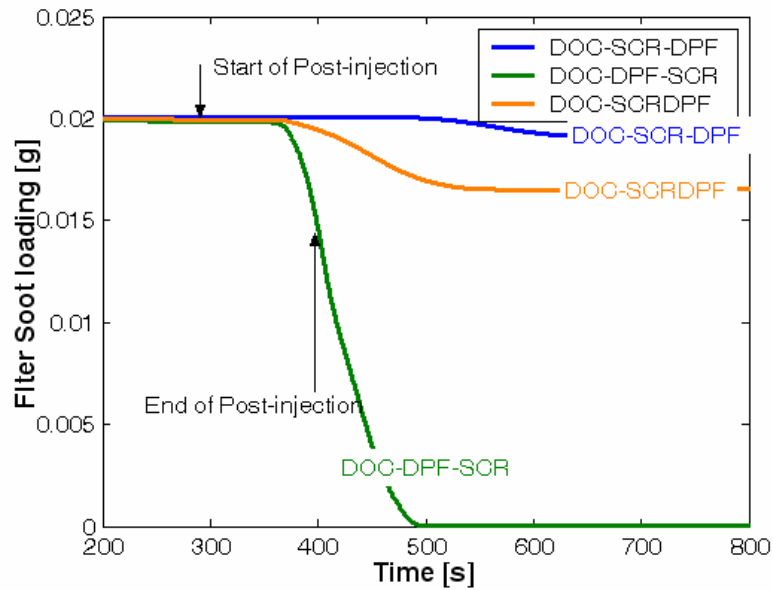
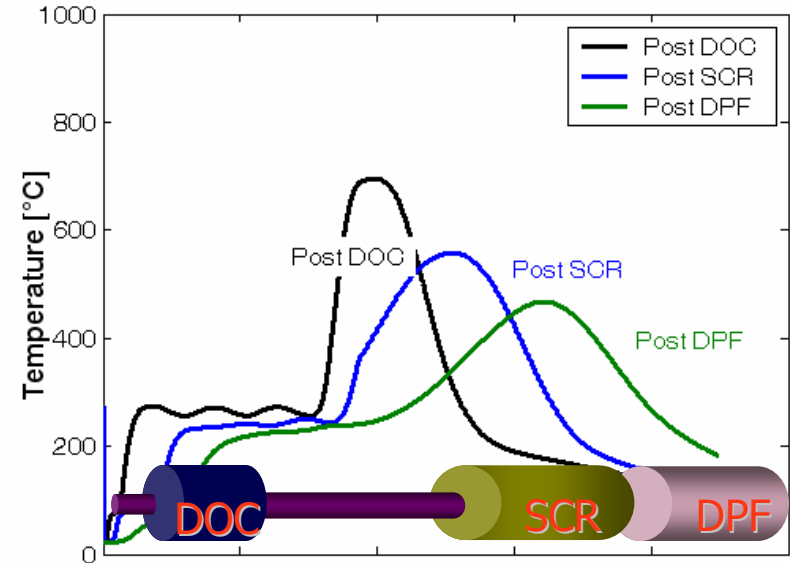
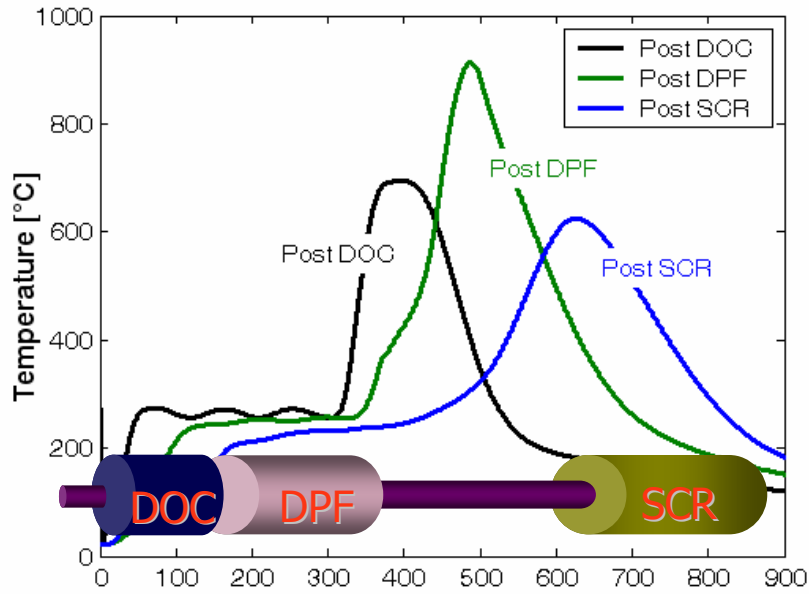
Comparison of various positioning strategies, including "wall-flow" SCR



Controlled regeneration

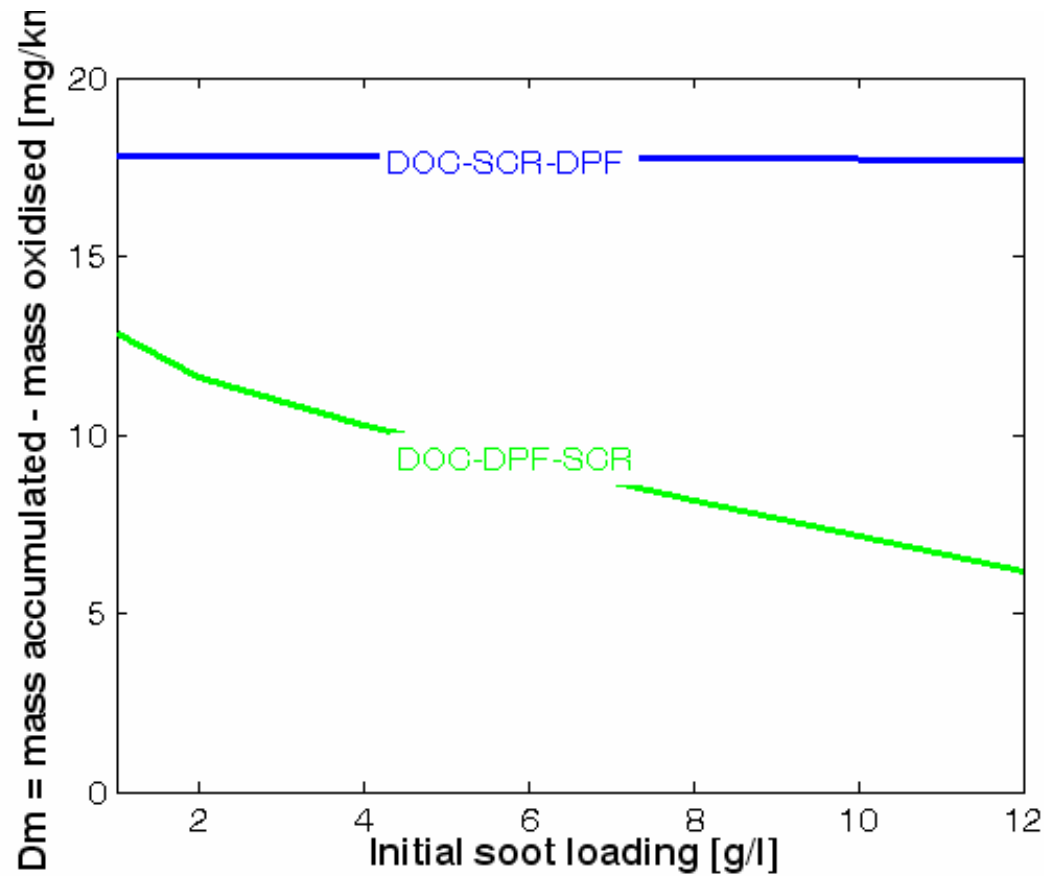


Uncontrolled regeneration



Effect of passive regeneration

Soot accumulation rate in successive European Driving Cycles



Summary

Flow-through reactors

- DOC modeling
 - ◆ HC adsorption
 - ◆ Radial effects
- LNT modeling
 - ◆ T dependence of effective NO_x storage capacity
 - ◆ Effect of OSC during regeneration
 - ◆ Sulfation/desulfation
- SCR modeling
 - ◆ NO/NO₂ ratio
 - ◆ NH₃ adsorption/desorption

Summary

4-way reactors

- CDPF modeling
 - ◆ Transport-reaction modeling
 - ◆ Catalyst zoning (axially/intra-wall)
 - ◆ 3-d regeneration modeling
- Wall-flow de-NO_x modeling (NSC, SCR)
 - ◆ Axial, intra-wall variations
- Foam de-NO_x modeling
 - ◆ Filtration/Flow/Heat transfer interactions
- System simulation
 - ◆ Emission cycle predictions
 - ◆ Passive/active regeneration predictions