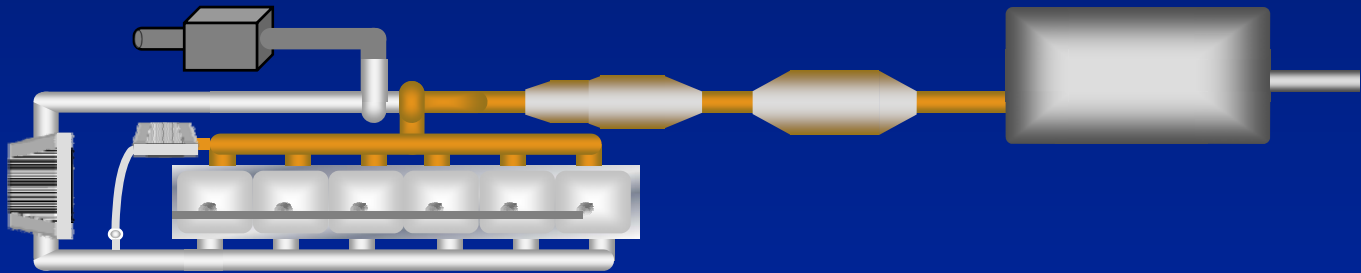




Development and Application of a Fast *Quasi-Steady* Solver for Integrated Modeling of Exhaust Aftertreatment Systems

*Syed Wahiduzzaman, Weiyong Tang, Seth Wenzel,
Gamma Technologies, Inc.*



11th Cleers Workshop

May 13-14 2008, Dearborn, MI, USA



Modeling Solutions Overview



Solution
Overview

Calibration

Q-S
Solver

SCR

DOC

Aged DOC

SIL/HIL /NN

2D/3D Model

Conclusions

- Flow model to coupled reactor model
GUI based chemistry library
(SAE 2007-01-4127, 9-10th Cleers Workshop)
- Computational y efficient solver
Quasi-Steady (QS) solver
(SAE 2008-01-0866)
- Kinetic parameter calibration
DoE (Design of Experiment) or direct optimizer
(SAE 2007-01-4127)

Modeling Solutions Overview (Cont.)



Solution
Overview



- **Advanced applications**
System modeling, effects of aging
- **Fast models for SIL and HIL applications**
From detailed model to NN model
(SIA, 28-29th May, 2008, INSA de Rouen, France)
- **Multi-dimensional and quasi-dimensional solution**
QS based 2D/3D modeling

Calibration

Q-S
Solver

SCR

DOC

Aged DOC

SIL/HIL /NN

2D/3D Model

Conclusions

Flow Model to Reactor Model



Reactants	Products
CO + 0.5O2	CO2
C3H6 + 4.5O2	3CO2 + 3H2O

OCrxn-01

Reactants	Products	Pre-exponent Multiplier	Temperature Exponent	Activation Temperature	Concentration Expressi...	Coverage Expression f...
BaCO3 + 2NO2 + .5O2	Ba(NO3)2 + CO2	1500	0	600	{NO2}*{O2}^0.5	A(1)
BaCO3 + 2NO + 1.5O2	Ba(NO3)2 + CO2	15000	0	500	{NO}^0.5*{O2}^1.5	A(1)
Ba(NO3)2 + 3CO	BaCO3 + 2NO + 2CO2	2.0E14	0	400	{CO}^3.0	1-A(1)
Ba(NO3)2 + H2 + CO2	BaCO3 + 2NO2 + H2O	0	0	400	{CO2}*{H2}	1-A(1)
NO+0.5O2	NO2	9.0E9	-1	8419.25	{NO}	1
NO2	NO+0.5O2	5.0E10	-1	8419.25	{NO2}	1
CO + NO	CO2 + 0.5N2	9.0E17	0	400	1.5E16*{CO}^3.0*{N...	1

LNTrxns-01

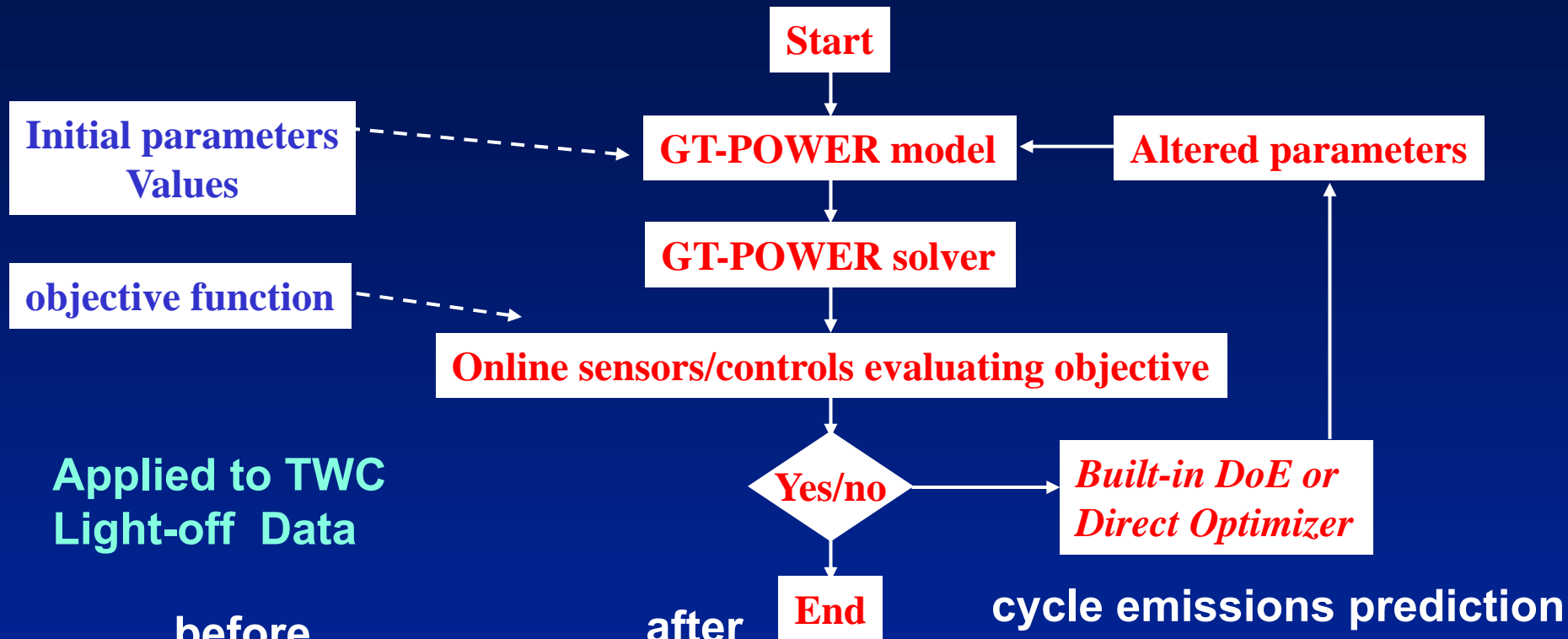
Pre-exponent Multiplier	Temperature Exponent	Activation Temperature	Concentration Expressi...	Coverage Expression f...
8000000	-1	5500		
1.429129E10	-1	8419.25		
7.70533E8	-1	8419.25		
5.39E16	-1	16000		

Concentration Expressions	
{CO}*{O2}/G(1)^2.0/G(2)/G(3)	
{C3H6}*{O2}/G(1)^2.0/G(2)/G(3)	
{H2}*{O2}/G(1)^2.0/G(2)/G(3)	
{NO}*{O2}	
{NO2}	

Langmuir-Hinshelwood Expressions	
1.0 + 65.6*exp(961.0/T)*{CO} + 1.08e3*exp(361.0/T)*{C3H6}	
1.0 + 3.98*exp(11611/T)*{CO}^2.0*{C3H6}^2.0	
1.0 + 4.79e5*exp(-3733./T)*{NO}^0.7	
1.0 + 19.86*exp(654.5/T)*{CO}	
1.0 + 65.6*exp(961.0/T)*{CO} + 1.08e3*exp(361.0/T)*{HC}	

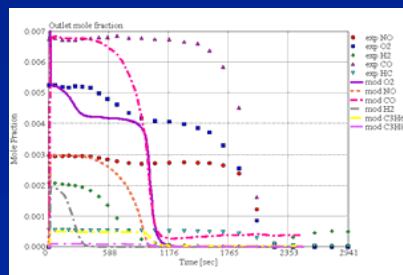
Simulation Workflow

Experiment => calibration => Prediction

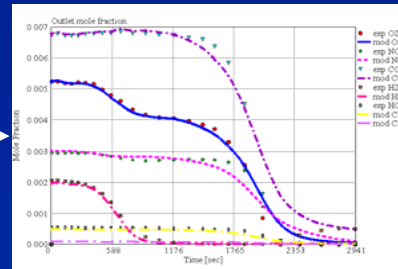


Applied to TWC
Light-off Data

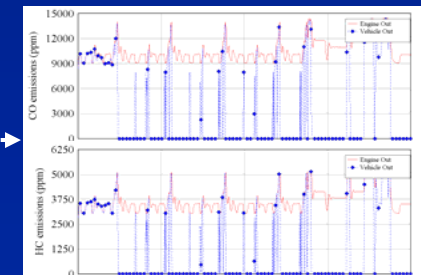
before



after



cycle emissions prediction



All in a one integrated environment

Computational Efficiency of Q-S Solver

(SAE 2008-01-0866)



- ❑ TWC kinetic model
- ❑ Simulation duration: 2942 seconds
- ❑ 20 sub-volume, dt = 0.1 seconds
- ❑ QS can be 10-100 times faster than real time

Solution
Overview

Calibration

Q-S
Solver

SCR

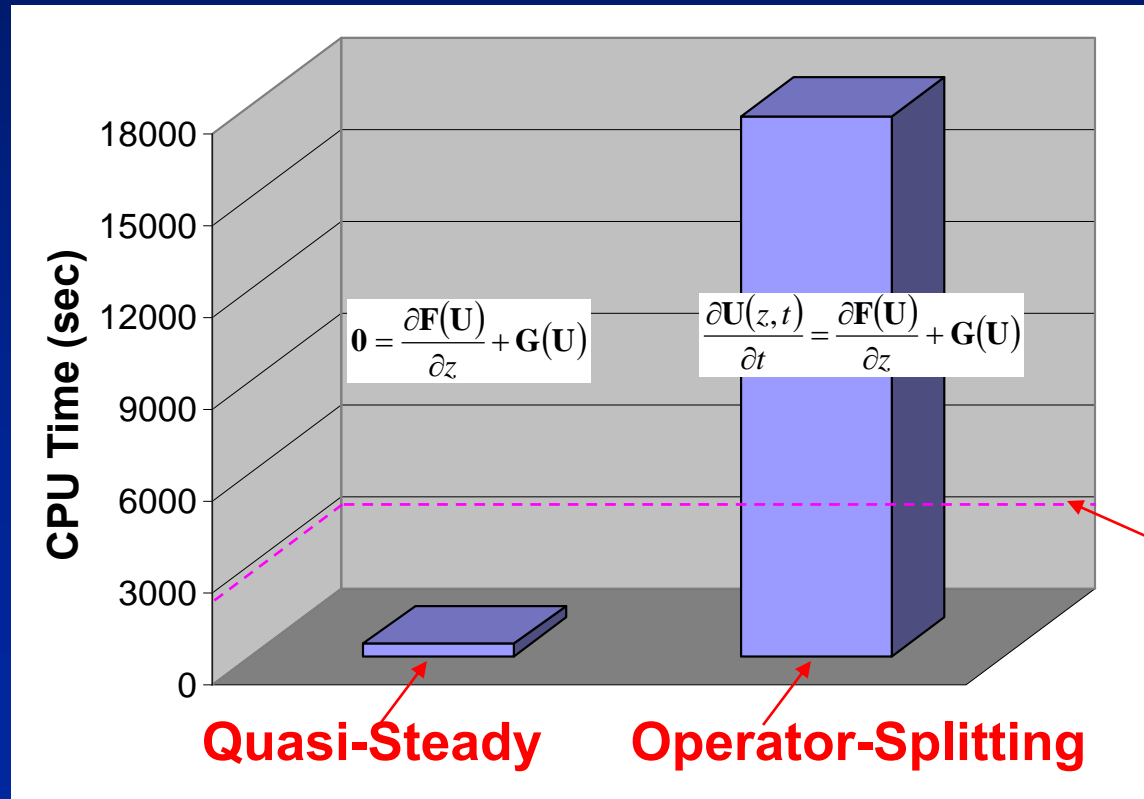
DOC

Aged DOC

SIL/HIL /NN

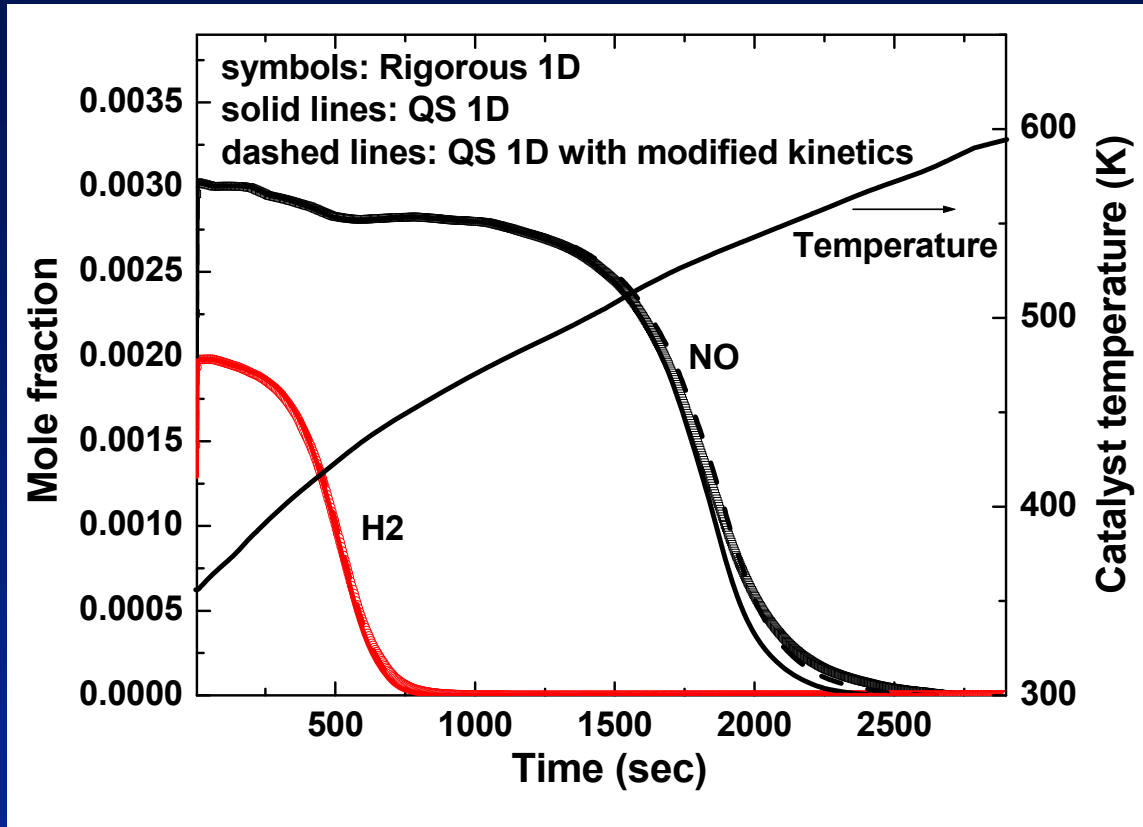
2D/3D Model

Conclusions



RT threshold

Accuracy of QS Approach



Solution Overview

Calibration

Q-S Solver

SCR

DOC

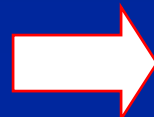
Aged DOC

SIL/HIL /NN

2D/3D Model

Conclusions

$$\frac{\partial \mathbf{C}_g}{\partial t} + u \frac{\partial \mathbf{C}_g}{\partial z} = \dot{\mathbf{R}}(\mathbf{C}_s, \theta, T_s)$$



$$u \frac{\partial \mathbf{C}_g}{\partial z} = \dot{\mathbf{R}}(\mathbf{C}_s, \theta, T_s) - \frac{\mathbf{C}_g - \mathbf{C}_g^0}{\Delta t} = \dot{\mathbf{R}}'(\mathbf{C}_s, \theta, T_s)$$

Component Level Modeling

Zeolite Based SCR



- Experimental data was provided by PSA Peugeot Citroën
- Five set of calibration data aimed at determination of parameters involving

- Test 1: Storage capacity, absorption/desorption



- Test 2: Ammonia oxidation



- Test 3: “Standard” SCR reaction



- Test 4: “Slow” SCR reaction



- Test 5: “Fast” SCR reaction



Solution
Overview

Calibration

Q-S
Solver

SCR

DOC

Aged DOC

SIL/HIL /NN

2D/3D Model

Conclusions





SGB protocol for testing SCR catalyst

Solution Overview

Calibration

Q-S Solver

SCR

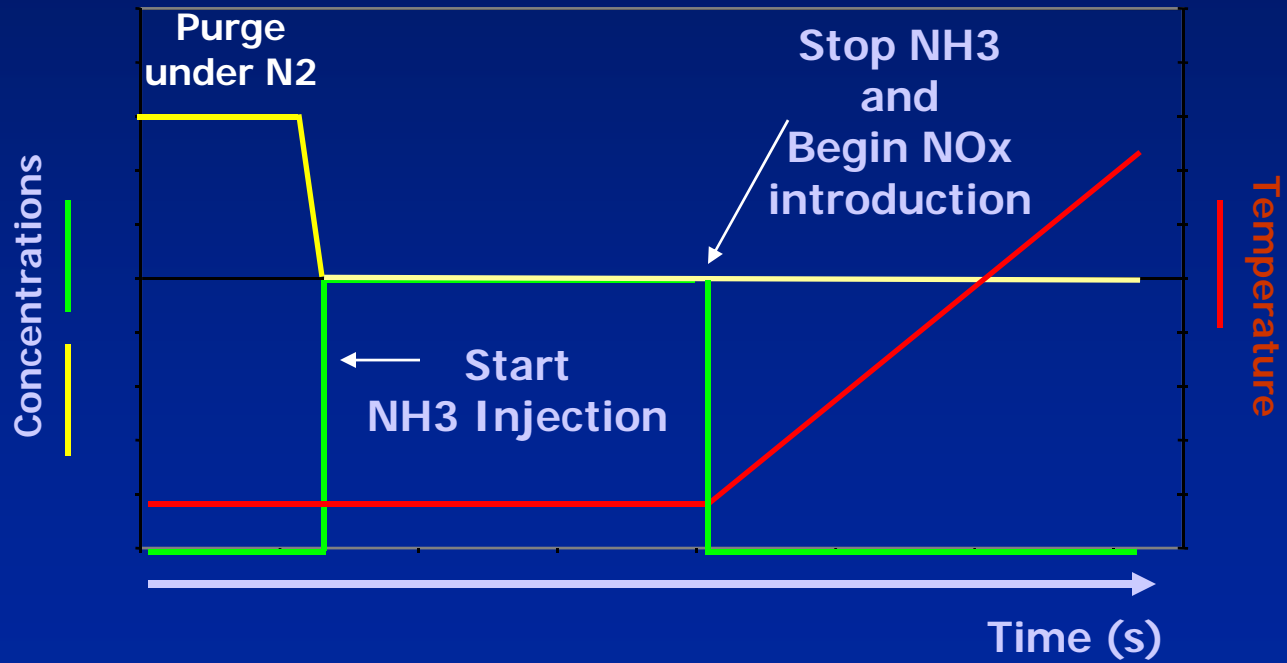
DOC

Aged DOC

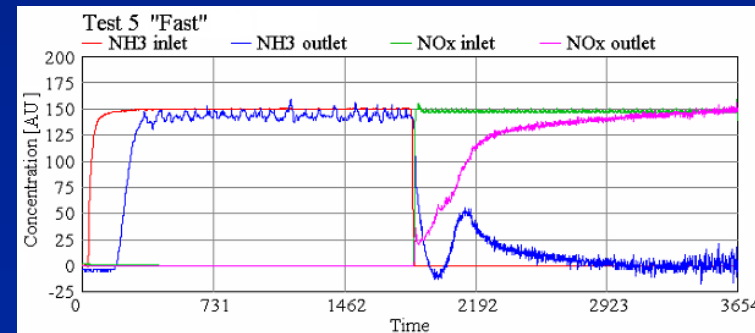
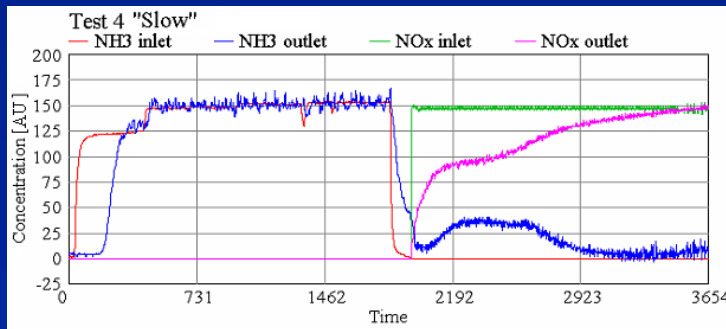
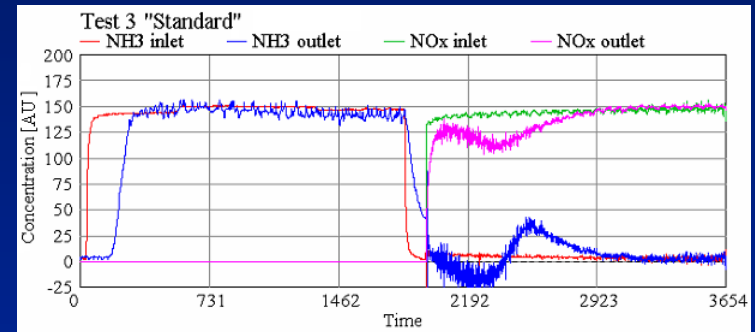
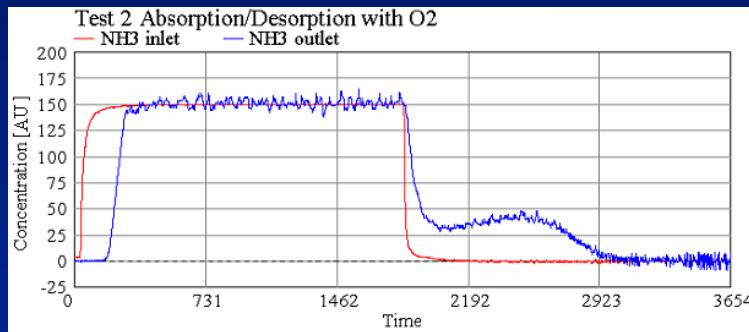
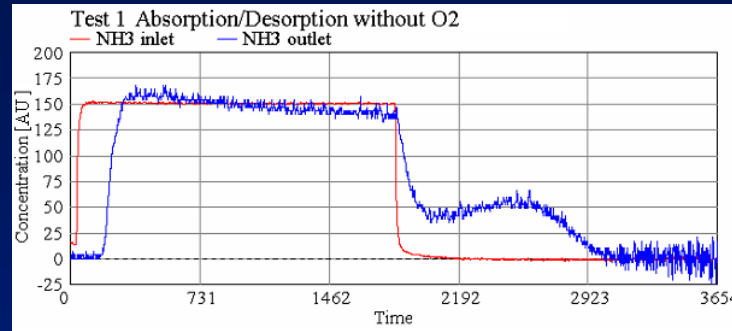
SIL/HIL /NN

2D/3D Model

Conclusions



Processed NH3 and Pollutant Sensors Data



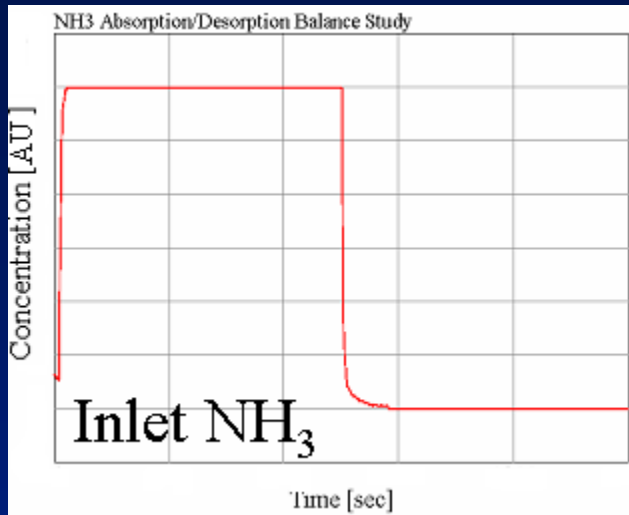
- Solution Overview
- Calibration
- Q-S Solver
- SCR
- DOC
- Aged DOC
- SIL/HIL /NN
- 2D/3D Model
- Conclusions



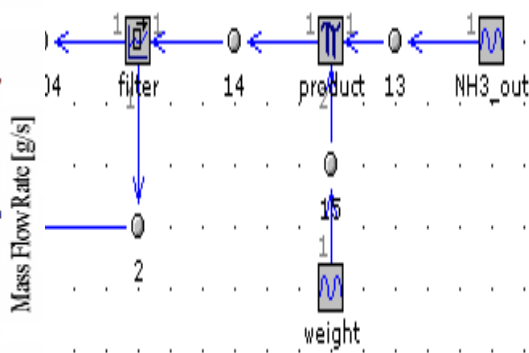
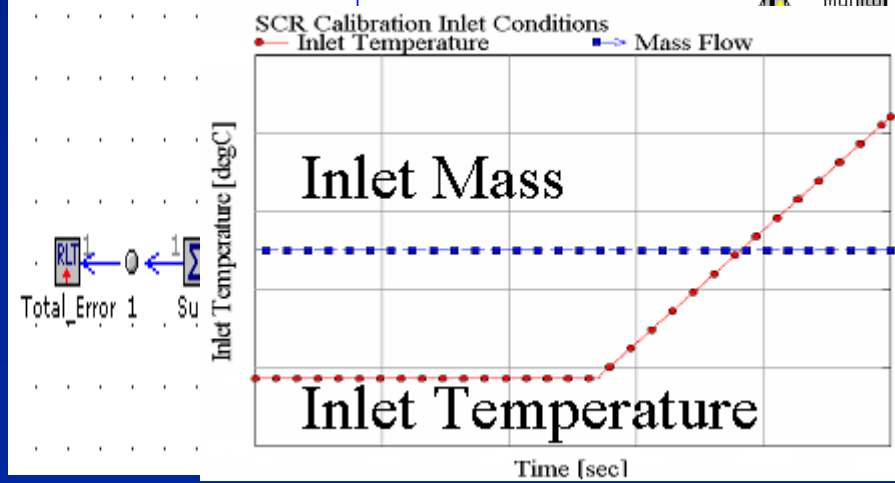
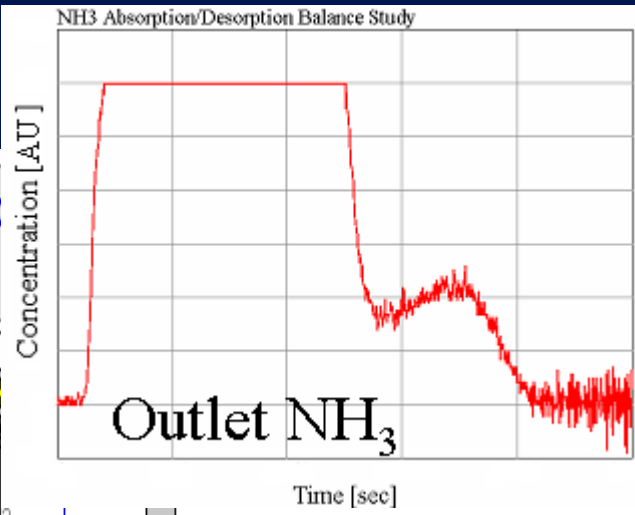
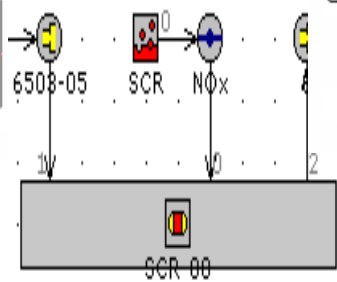
Calculation of Storage Capacity



- Solution Overview
- Calibration
- Q-S Solver
- SCR
- DOC
- Aged DOC
- SIL/HIL /NN
- 2D/3D Model
- Conclusions



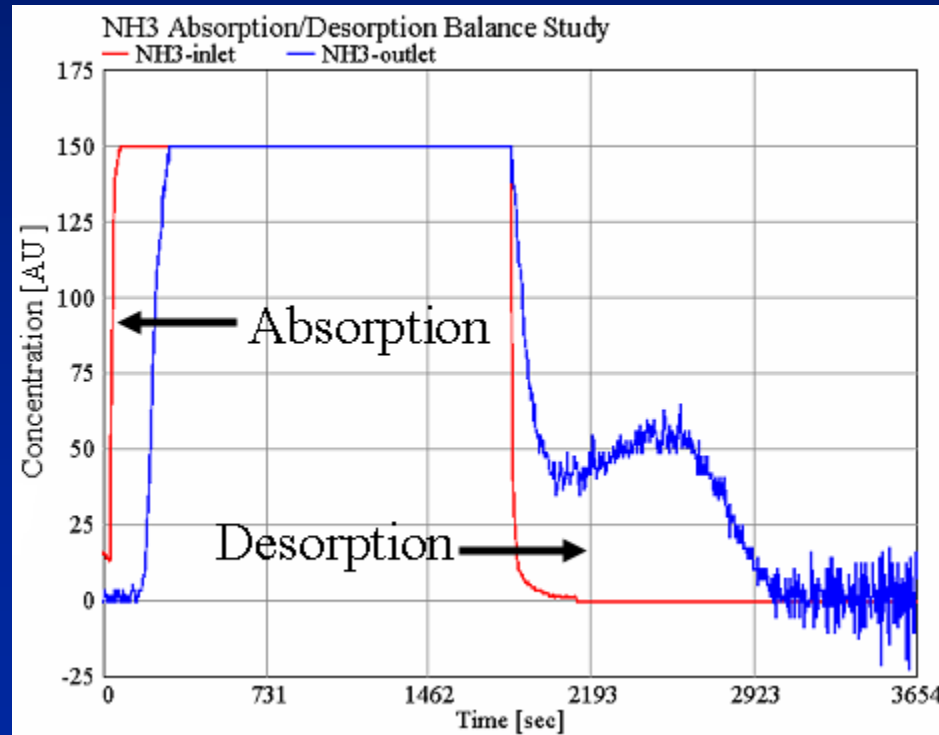
Test4 : adsorption
NH3 without O2



Storage Capacity (cont.)



- Experimental results suggest more NH_3 desorbed than could be accounted for by storage
- Two possibilities exist:
 1. experimental error in one or both NH_3 sensors
 2. NH_3 is pre-stored



Storage Capacity (cont.)



- The onset of saturation and shape of saturation curve indicated by the exit NH_3 sensor seemed to be consistent
- Optimization was performed to determine:
 - storage capacity
 - pre-stored NH_3 (if any)
- Optimization goal:
 - conserve NH_3 mass
 - conserve onset/shape of NH_3 saturation curve
- Built-in direct optimizer (Brent) was used

Solution
Overview

Calibration

Q-S
Solver

SCR

DOC

Aged DOC

SIL/HIL /NN

2D/3D Model

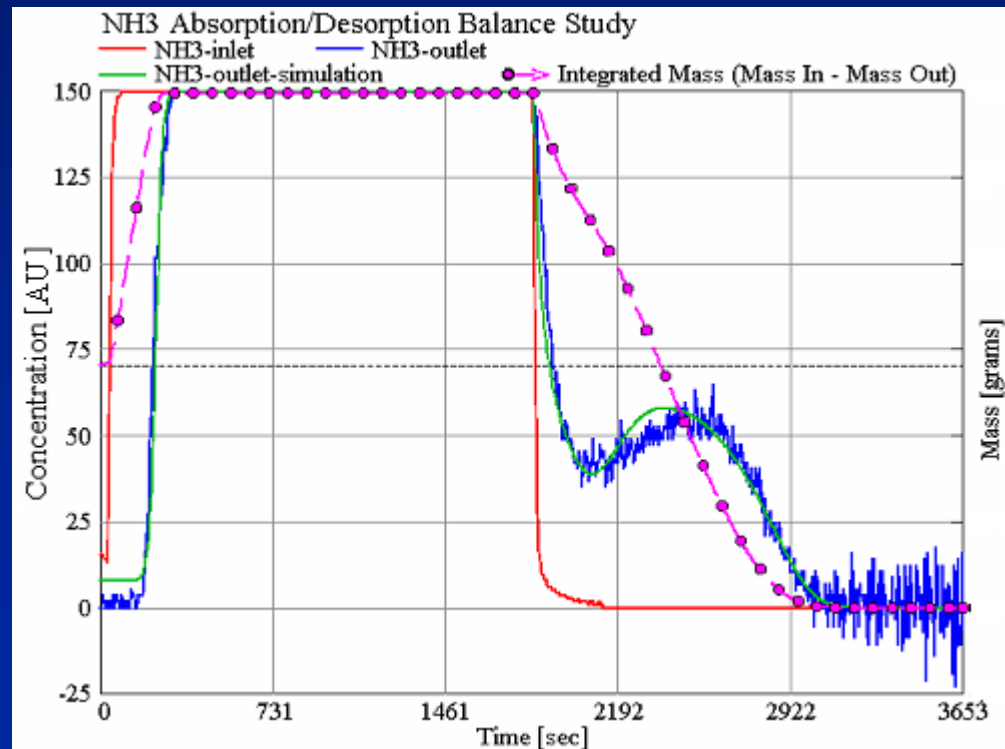
Conclusions



Storage Capacity (cont.)



- A pre-storage corresponding to 45% coverage and a storage capacity of $4.9E-3\text{gmole/m}^2$ were determined
- These generally agree with all experiments



Solution
Overview

Calibration

Q-S
Solver

SCR

DOC

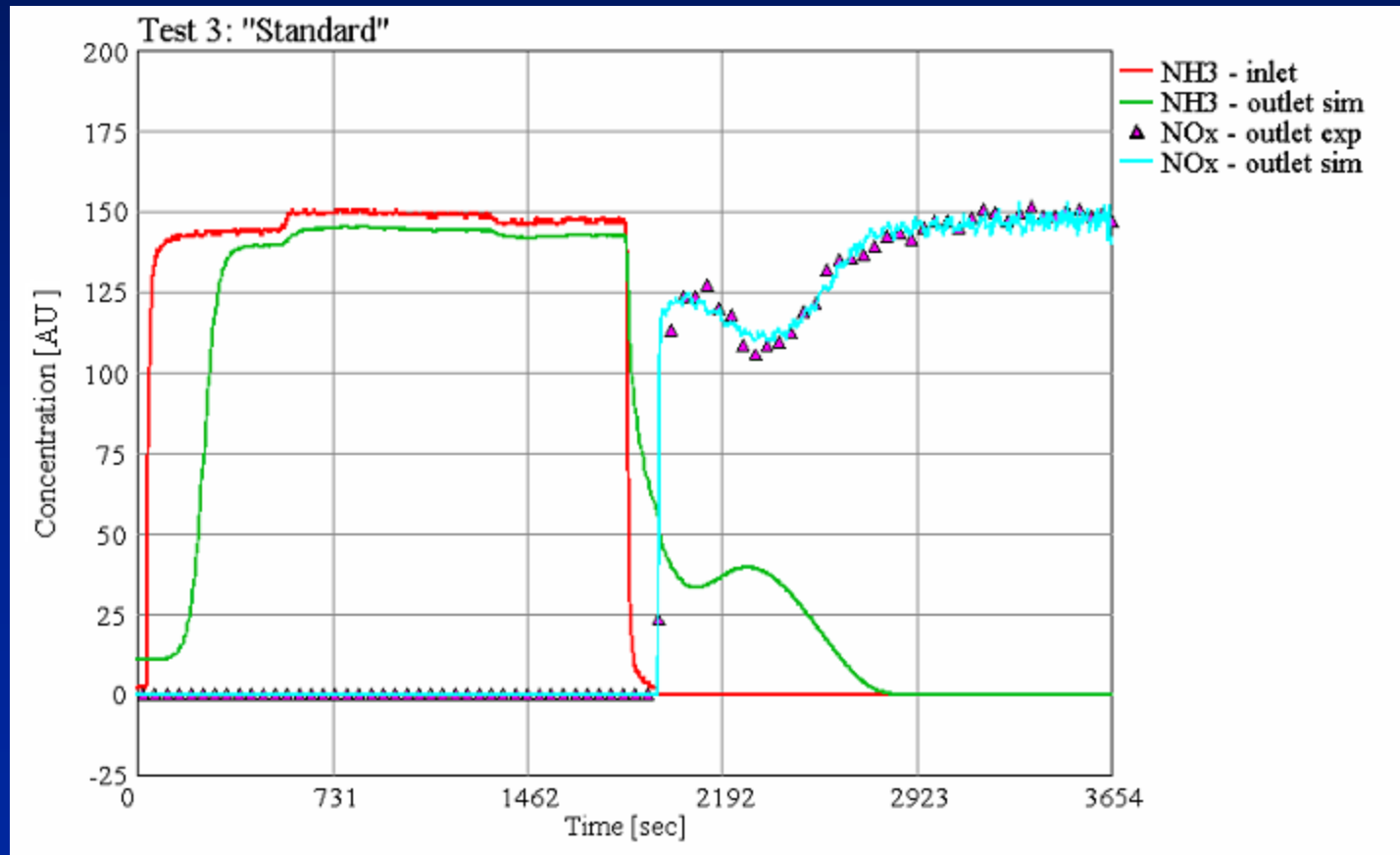
Aged DOC

SIL/HIL /NN

2D/3D Model

Conclusions

Standard Reaction



Solution
Overview

Calibration

Q-S
Solver

SCR

DOC

Aged DOC

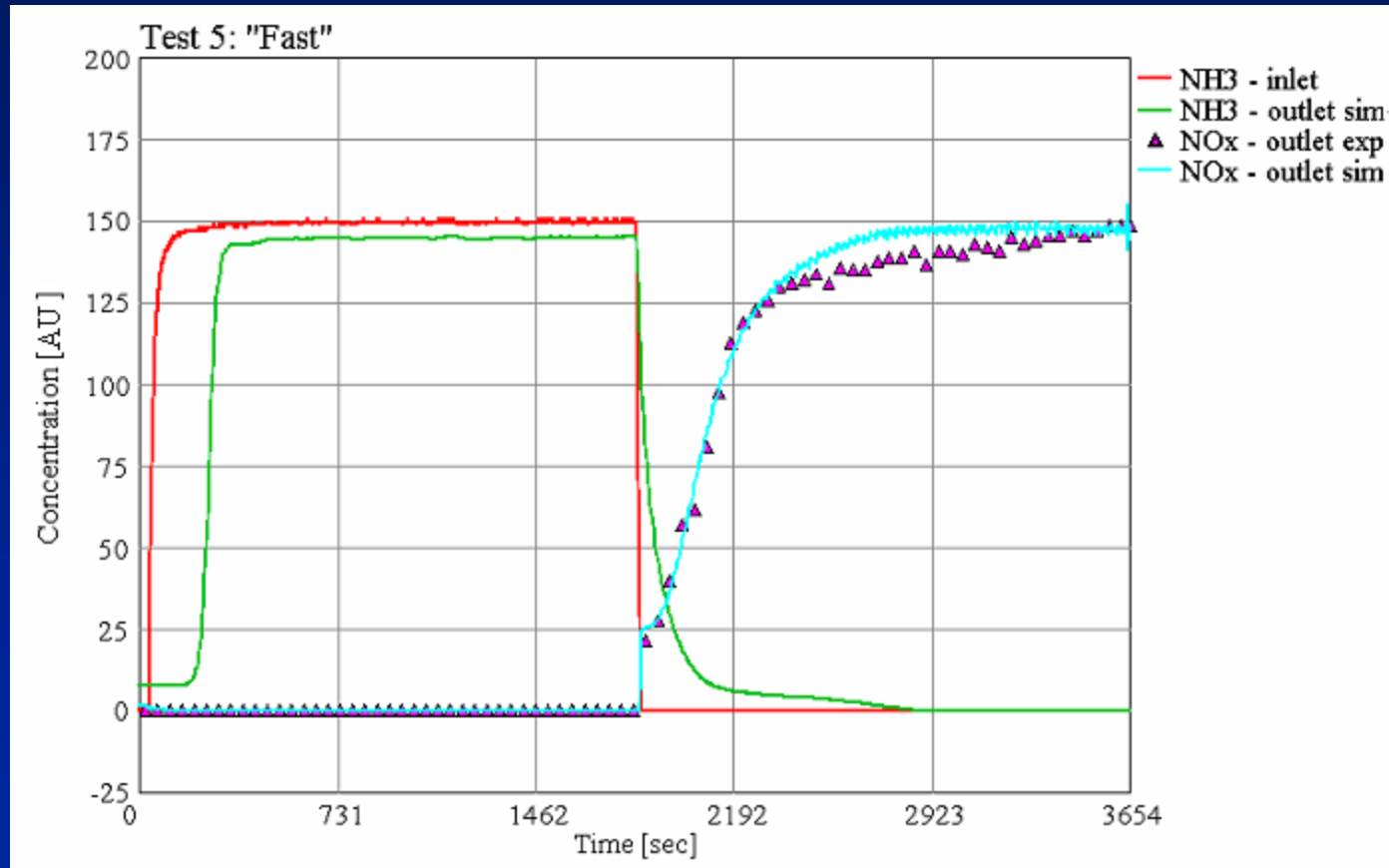
SIL/HIL /NN

2D/3D Model

Conclusions



Fast Reaction



- Solution Overview
- Calibration
- Q-S Solver
- SCR
- DOC
- Aged DOC
- SIL/HIL /NN
- 2D/3D Model
- Conclusions





SCR NO_x Selectivity Study

- NO_x conversion should be highest at NO₂/NO_x ratio of 0.5 (or NO:NO₂ = 1:1)
- Study was performed using
 - Vary NO₂/NO_x ratio from 0-1
 - Vary temperature from 400-700K
 - 10 ppm NH₃ slip
 - 150 ppm NO_x, NH₃ (variable), 10% H₂O, 10% O₂, balance N₂
 - Constant volume flow rate = 0.55 liter/s

Solution
Overview

Calibration

Q-S
Solver

SCR

DOC

Aged DOC

SIL/HIL /NN

2D/3D Model

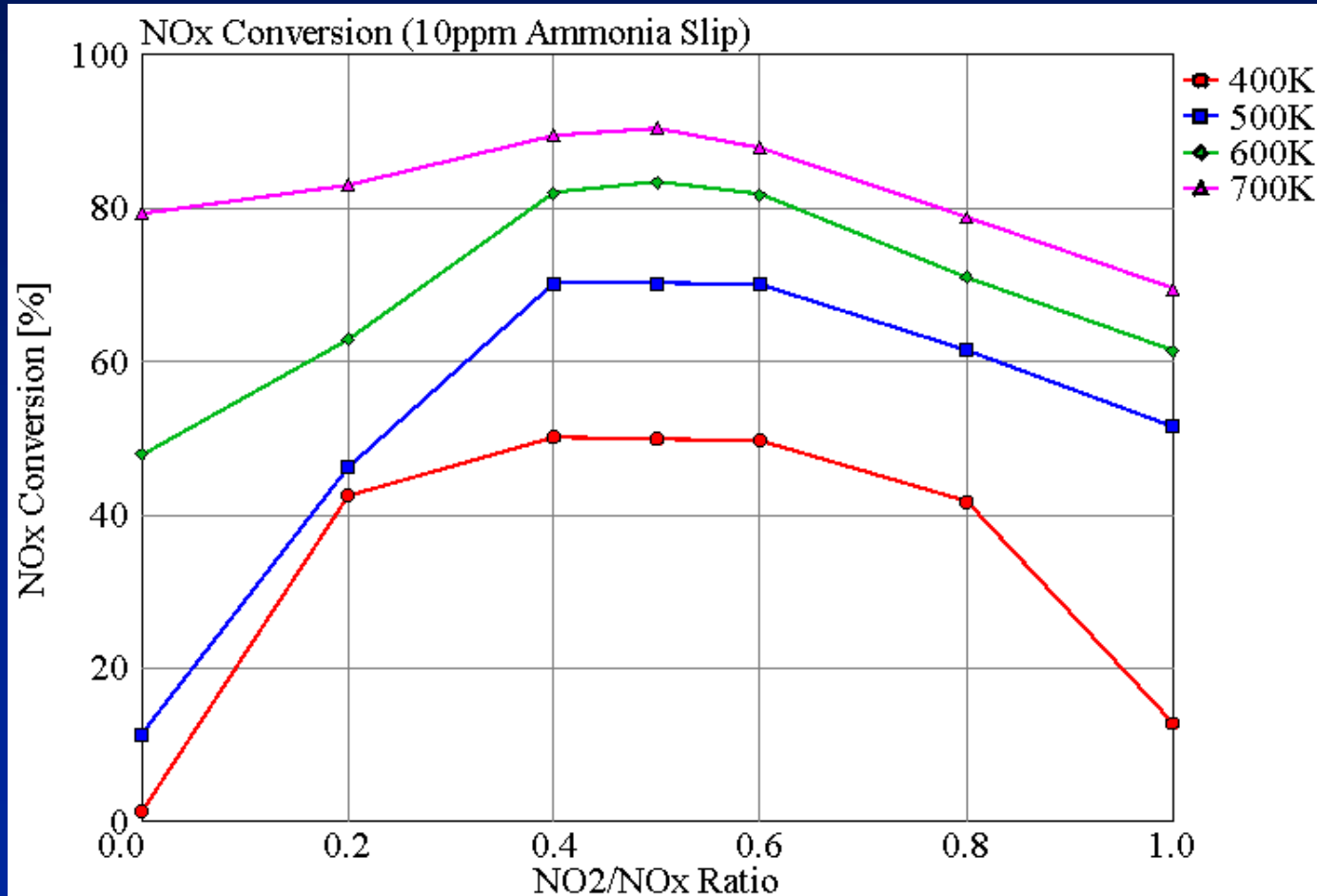
Conclusions





SCR NO_x Selectivity Study

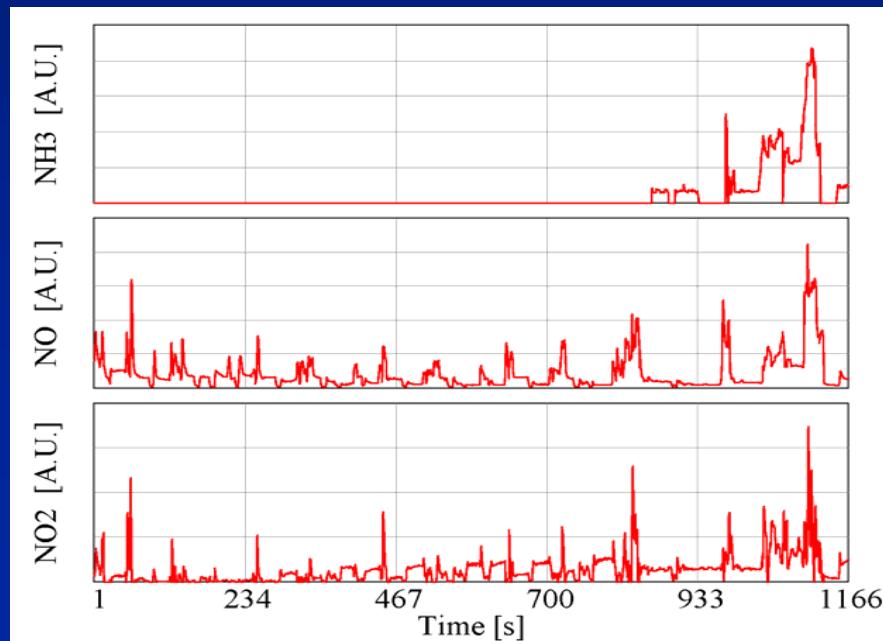
- Solution Overview
- Calibration
- Q-S Solver
- SCR
- DOC
- Aged DOC
- SIL/HIL /NN
- 2D/3D Model
- Conclusions



Transient Emission Predictions



- Calibrated SCR model used for Transient NDEC cycle
- Model ran under two conditions:
 - Absorption site 100% “open” (no NH_3 prestorage)
 - Absorption site 0.0% “open”



Solution
Overview

Calibration

Q-S
Solver

SCR

DOC

Aged DOC

SIL/HIL /NN

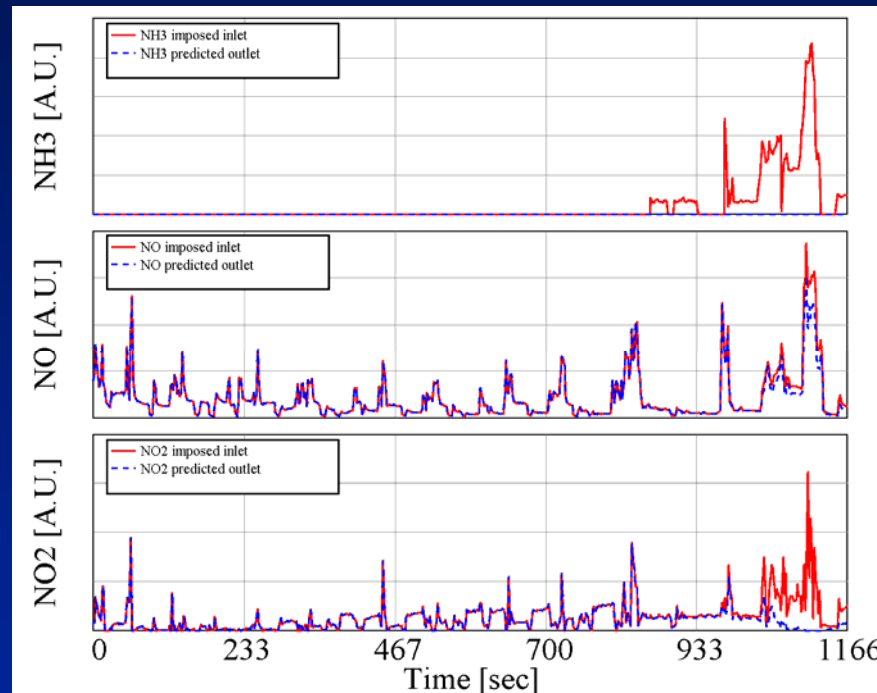
2D/3D Model

Conclusions

Emission Predictions (cont.)



- All sites “open” (no NH₃ prestored)



- Cumulative Mass Changes:

NO = -28% NO_x = -37%

NO₂ = -49% NH₃ = -100%

Solution
Overview

Calibration

Q-S
Solver

SCR

DOC

Aged DOC

SIL/HIL /NN

2D/3D Model

Conclusions

Computational Efficiency: SCR



- Simulations were performed on a Pentium 4 3.4GHz processor with 1 GB of RAM

Solution
Overview

Calibration

Q-S
Solver

SCR

DOC

Aged DOC

SIL/HIL /NN

2D/3D Model

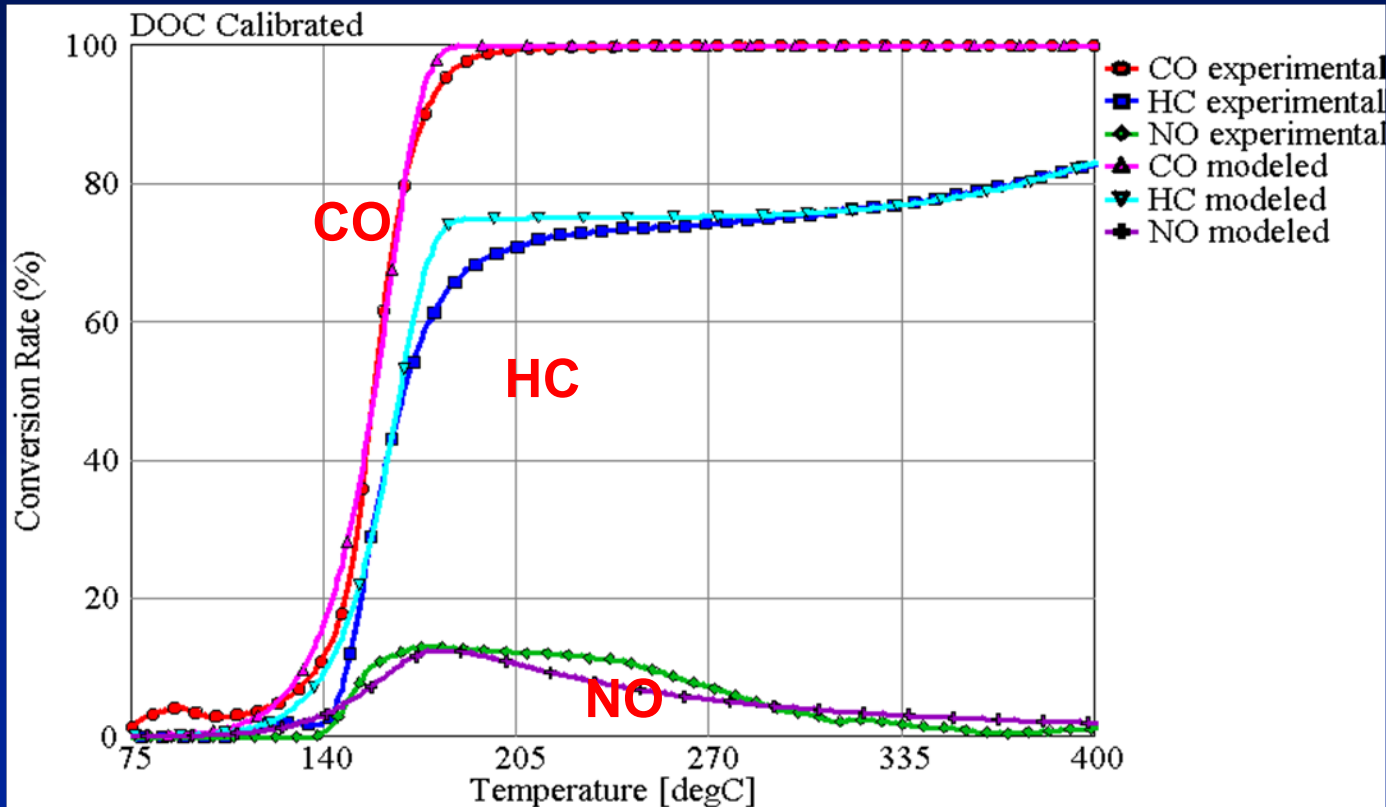
Conclusions

	Time Step Size (s)	Simulation Time (s)	Computational Time (s)
Abs/Des without O2	0.50	3654	31
Abs/Des with O2	0.50	3654	43
Standard Reaction	0.50	3654	45
Slow Reaction	0.50	3654	49
Fast Reaction	0.50	3654	57
Transient without NH ₃ prestored	0.25	1166	85
Transient with NH ₃ prestored	0.25	1166	87

Component Level Modeling: DOC



□ Step 1: Kinetic model calibration



Experiment was done at PSA Peugeot Citroen

Solution
Overview

Calibration

Q-S
Solver

SCR

DOC

Aged DOC

SIL/HIL /NN

2D/3D Model

Conclusions

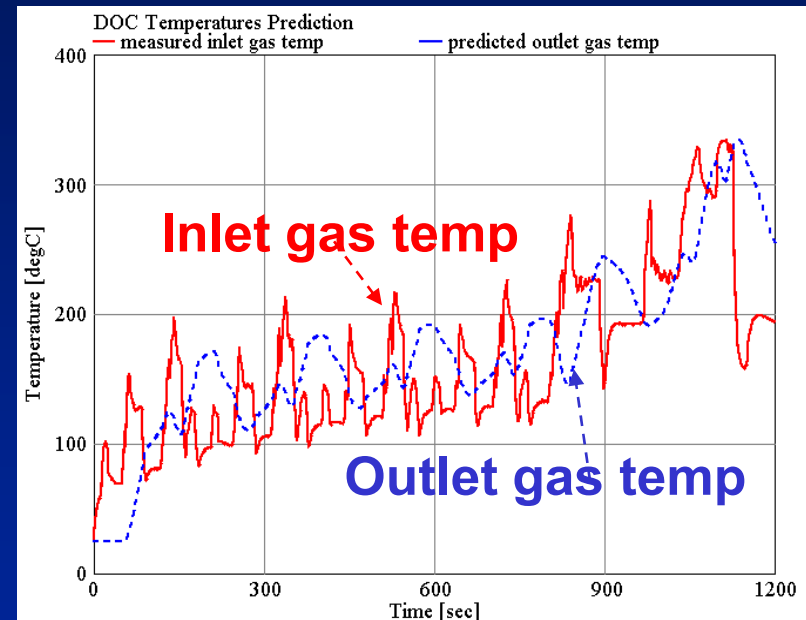
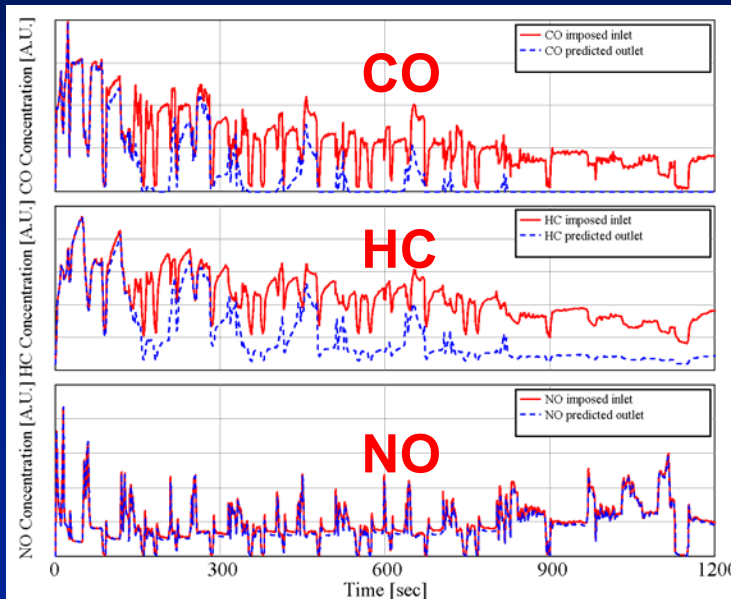


NEDC Test Cycle Emissions: DOC



□ Step 2: Emission predictions

• Transient NEDC cycle



• Cumulative mass conversions predicted to be:

CO = 61%

HC = 49%

NO = 6%

Solution
Overview

Calibration

Q-S
Solver

SCR

DOC

Aged DOC

SIL/HIL /NN

2D/3D Model

Conclusions

Computational Efficiency: DOC



- Simulations were performed on a Pentium 4 3.4GHz processor with 1 GB of RAM

Solution
Overview

Calibration

Q-S
Solver

SCR

DOC



Aged DOC

SIL/HIL /NN

2D/3D Model

Conclusions

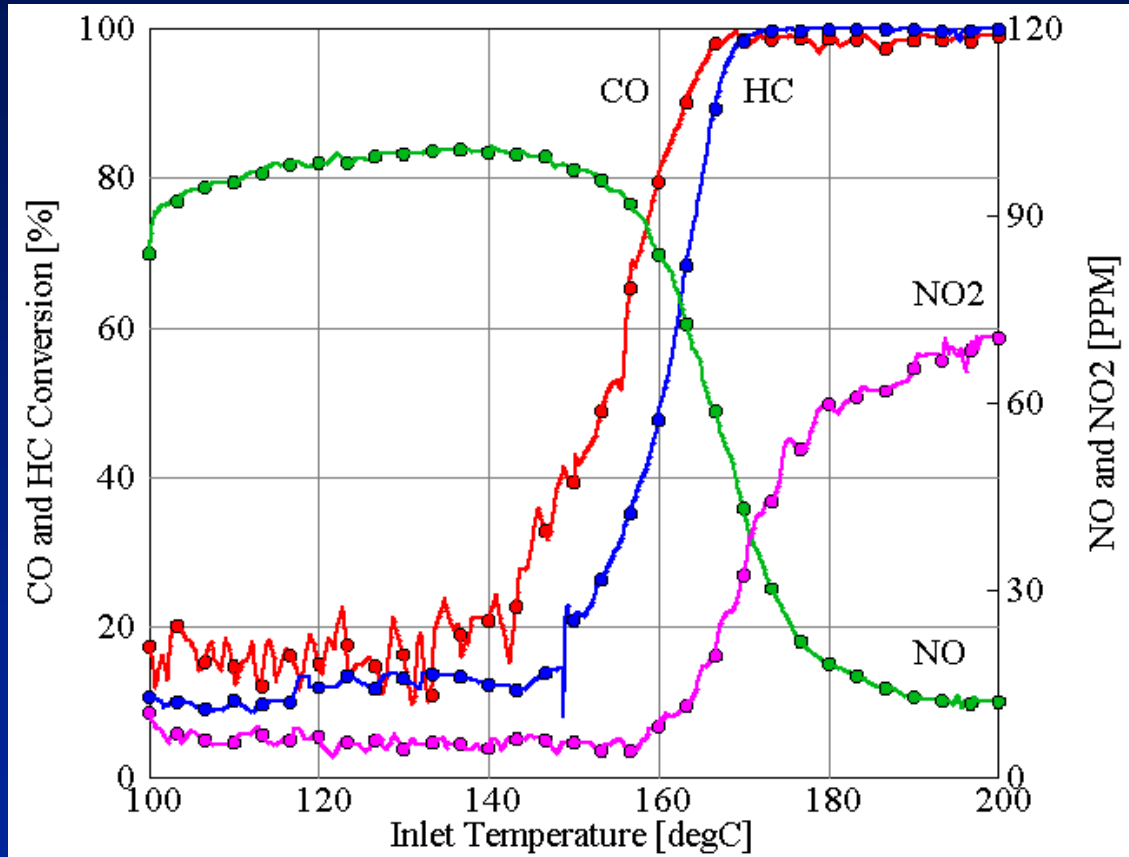
	Time Step Size (s)	Simulation Time (s)	Computational Time (s)
Step 1: Calibration	0.25	327	11
Step 2: Prediction	0.25	1200	71

Aged DOC Modeling



Gas	Exp 1
CO(ppm)	1000
C ₂ H ₄ (ppm)	300
H ₂ (ppm)	333
NO ₂ (ppm)	100
NO(ppm)	0
H ₂ O(Vol.-%)	4.5
CO ₂ (Vol.-%)	5
O ₂ (Vol.-%)	10
*Balance consists of N ₂	

- Solution Overview
- Calibration
- Q-S Solver
- SCR
- DOC
- Aged DOC
- SIL/HIL /NN
- 2D/3D Model
- Conclusions



Measurements from Santhoji and coworkers:

"Aged DOC is a Net Consumer of NO₂: Analysis of Vehicle, Engine-dynamometer and Reactor Data", SAE NO. 2007-01-3984

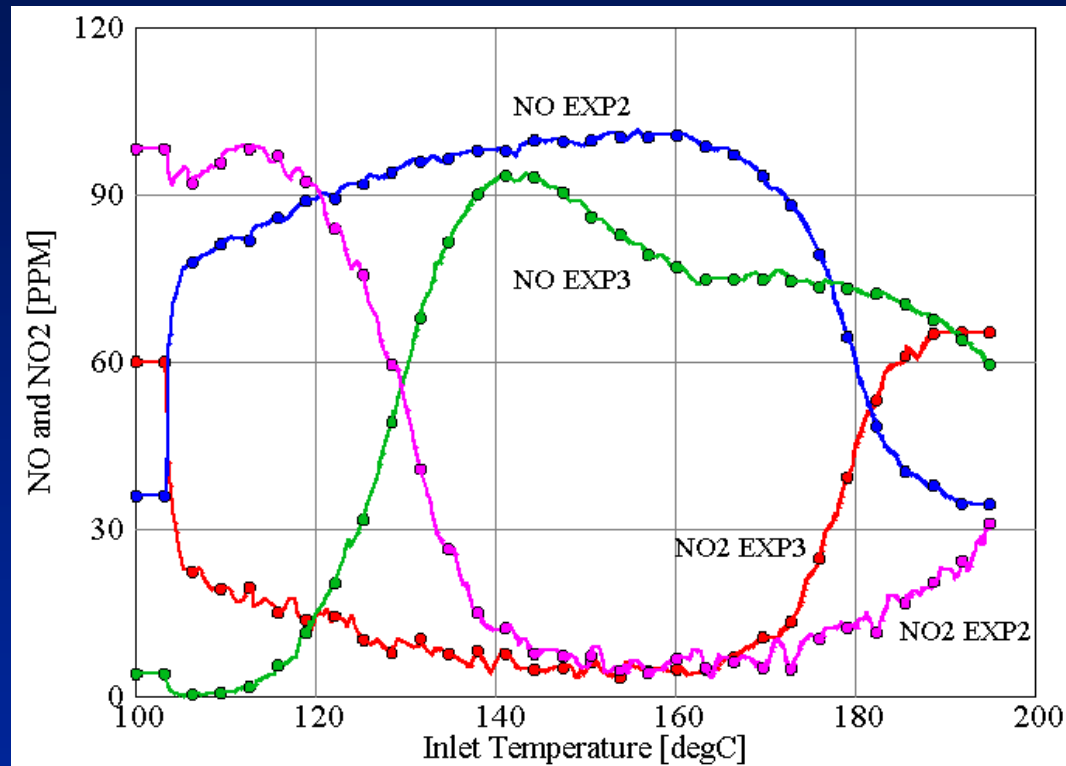
Aged DOC Modeling



- Solution Overview
- Calibration
- Q-S Solver
- SCR
- DOC
- Aged DOC
- SIL/HIL /NN
- 2D/3D Model
- Conclusions

Gas	Exp2	Exp3
CO(ppm)	1000	0
C ₂ H ₄ (ppm)	0	300
H ₂ (ppm)	0	0
NO ₂ (ppm)	100	100
NO (ppm)	0	0
H ₂ O (Vol.-%)	4.5	4.5
CO ₂ (Vol.-%)	5	5
O ₂ (Vol.-%)	10	10

*Balance consists of N2



Measurements from Santhoji and coworkers:

"Aged DOC is a Net Consumer of NO₂: Analysis of Vehicle, Engine-dynamometer and Reactor Data", SAE NO. 2007-01-3984

Aged DOC Modeling



- Introduce additional reactions:



Solution
Overview

Calibration

Q-S
Solver

SCR

DOC

Aged DOC

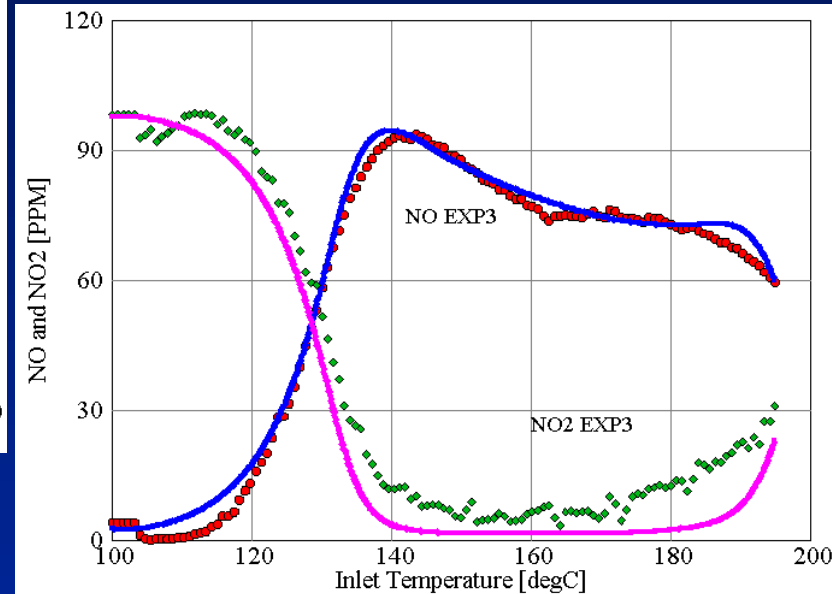
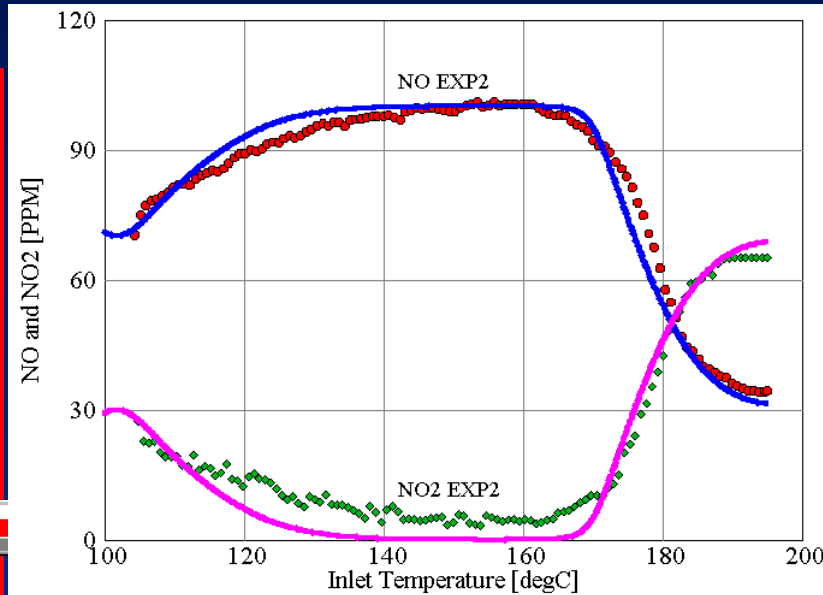


SIL/HIL /NN

2D/3D Model

Conclusions

Aged DOC Modeling



Exp.
Sim. _____



Measurements from Santhoji and coworkers:

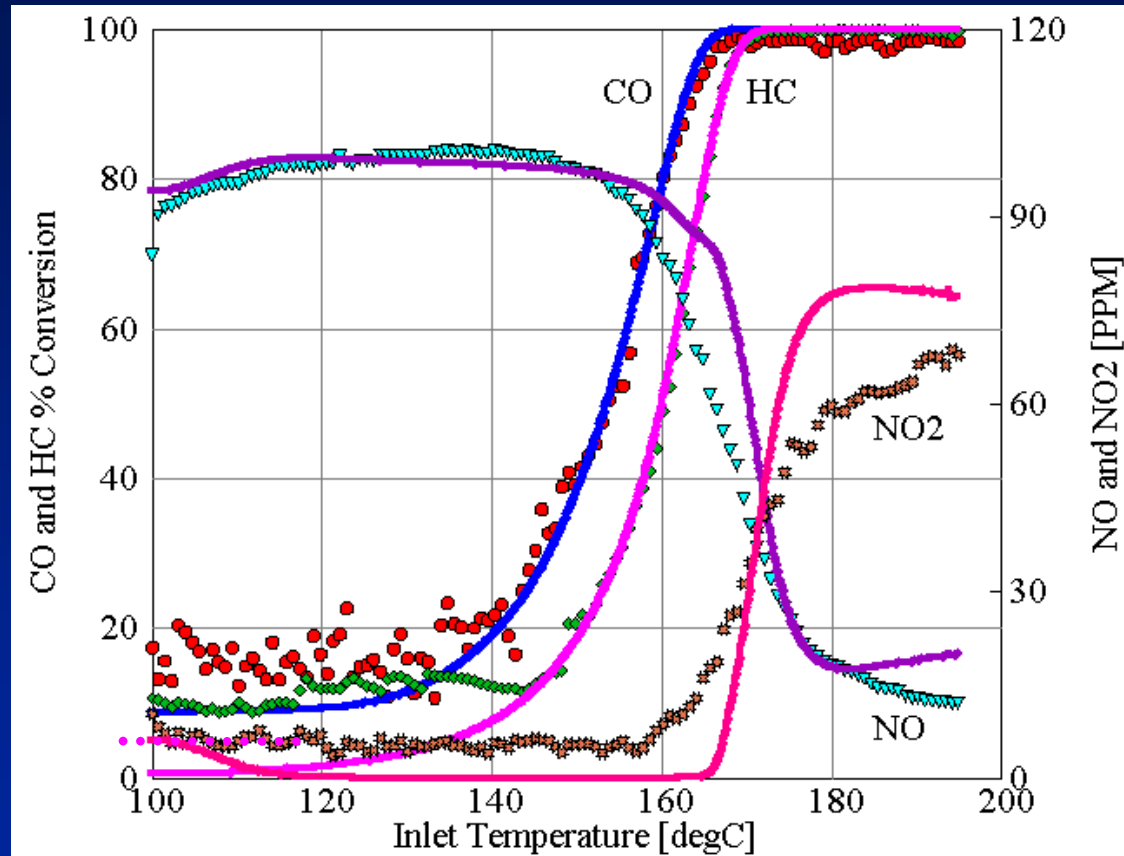
"Aged DOC is a Net Consumer of NO₂: Analysis of Vehicle, Engine-dynamometer and Reactor Data", SAE NO. 2007-01-3984

- Solution Overview
- Calibration
- Q-S Solver
- SCR
- DOC
- Aged DOC**
- SIL/HIL /NN
- 2D/3D Model
- Conclusions

Aged DOC Modeling



Exp. Sim. —



Measurements from Santhoji and coworkers:

"Aged DOC is a Net Consumer of NO₂: Analysis of Vehicle, Engine-dynamometer and Reactor Data", SAE NO. 2007-01-3984

Solution Overview

Calibration

Q-S Solver

SCR

DOC

Aged DOC

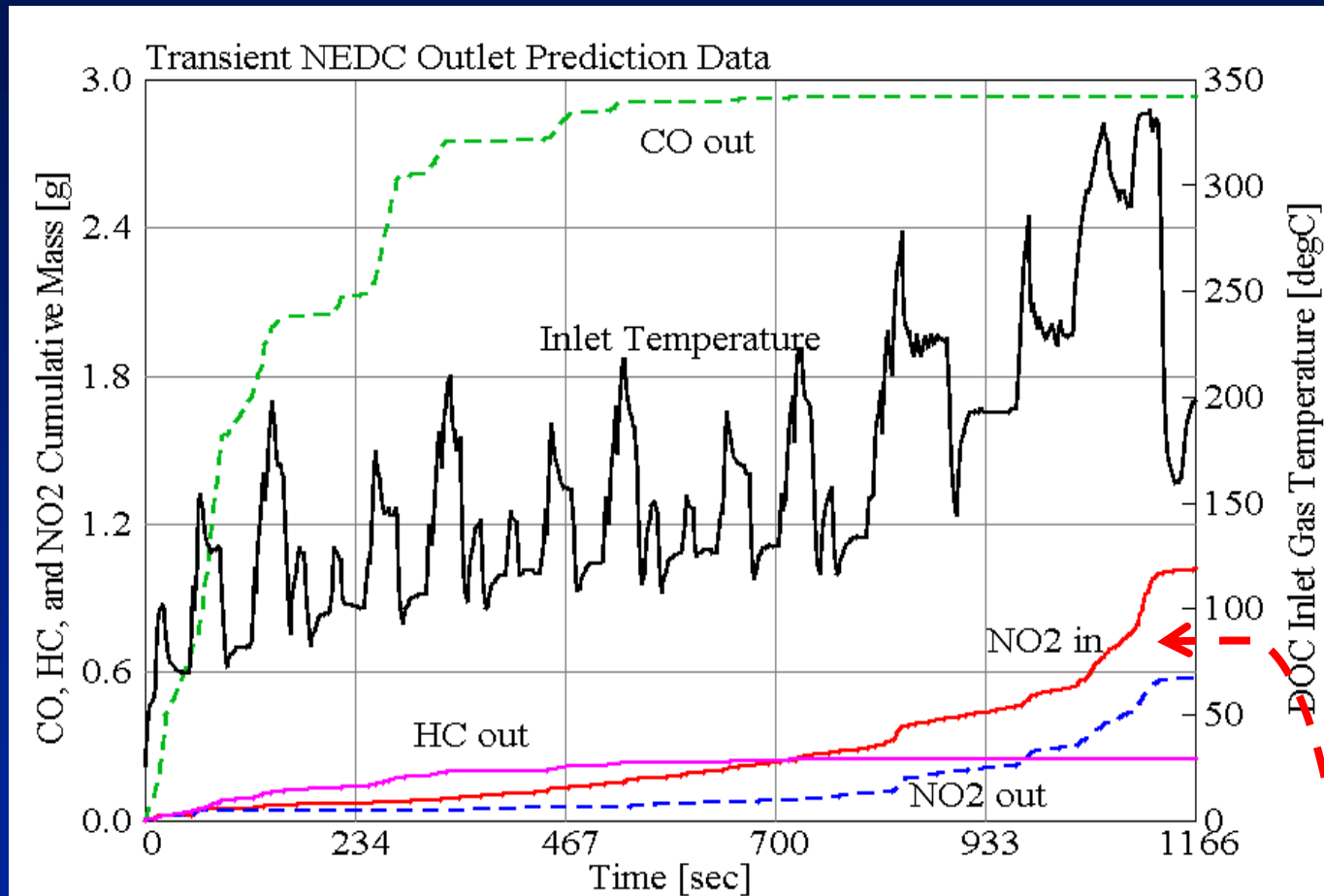


SIL/HIL /NN

2D/3D Model

Conclusions

Aged DOC Modeling



Model predicts cumulative NO₂ reduction = 44%

Experimental inlet conditions provided by PSA Peugeot Citroen

Solution Overview

Calibration

Q-S Solver

SCR

DOC

Aged DOC

SIL/HIL /NN

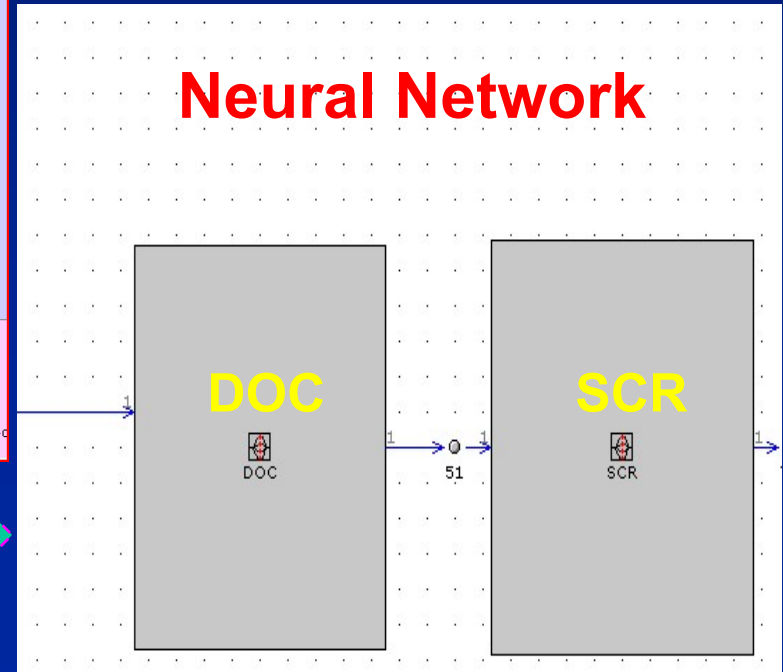
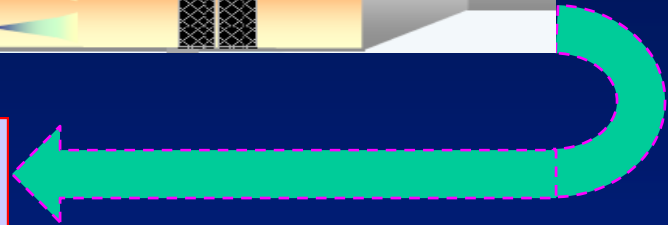
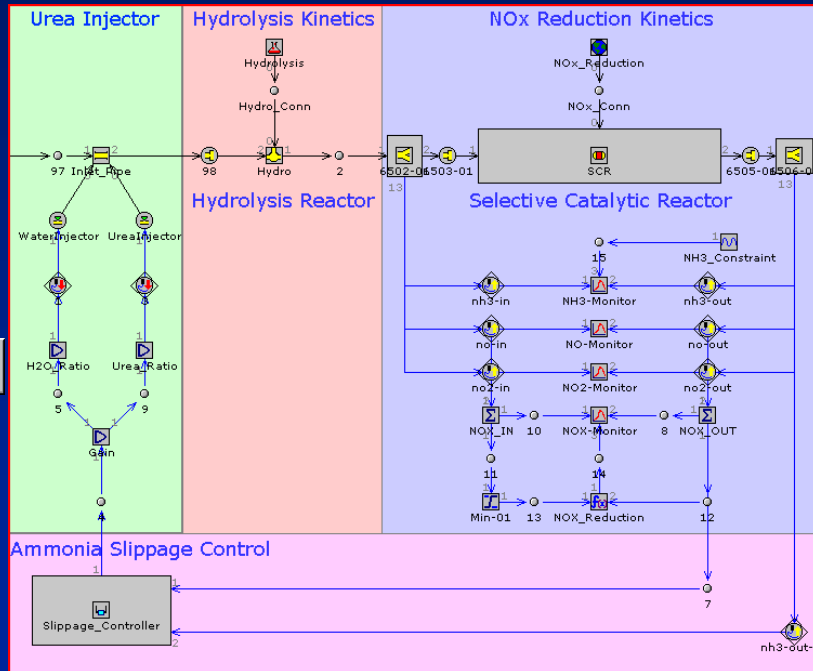
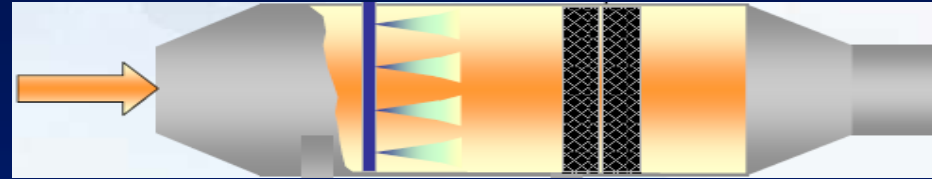
2D/3D Model

Conclusions





SIL/HIL Model Generation



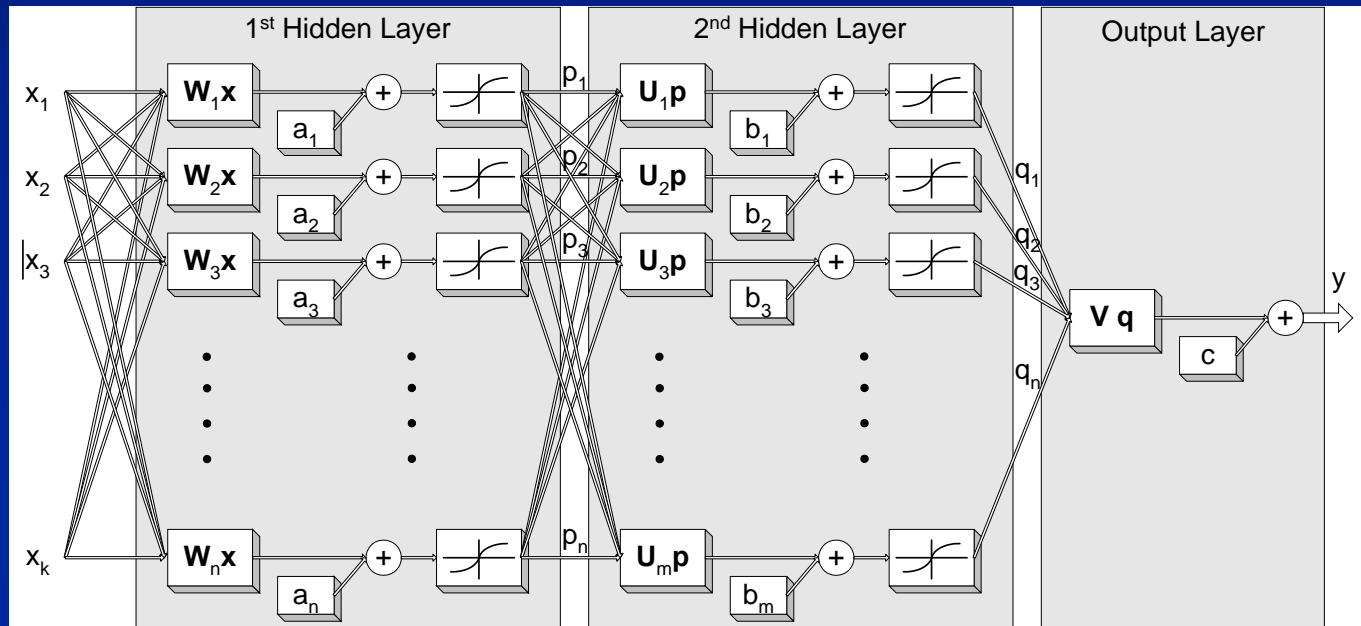
- Solution Overview
- Calibration
- Q-S Solver
- SCR
- DOC
- Aged DOC
- SIL/HIL /NN
- 2D/3D Model
- Conclusions





Neural Network Training

- **Three-Layer Feedforward Neural Network**
 - ✓ 2 hidden layers with tan-sigmoid activation functions
 - ✓ 1 output layer with linear activation function
- **Levenberg-Marquardt algorithm for training**
- **Excellent Neural Network generalization capability**
 - ✓ Fixed balanced penalties
 - ✓ Adjustable penalties (“Bayesian Regularization”)



Solution
Overview

Calibration

Q-S
Solver

SCR

DOC

Aged DOC

SIL/HIL /NN

2D/3D Model

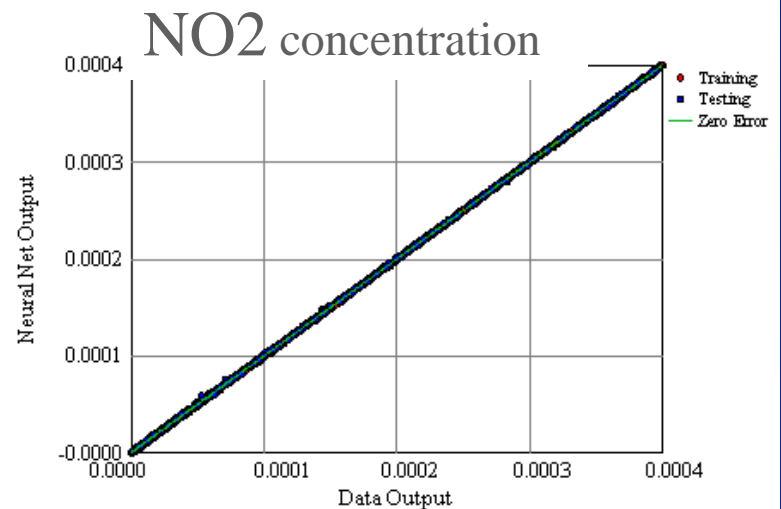
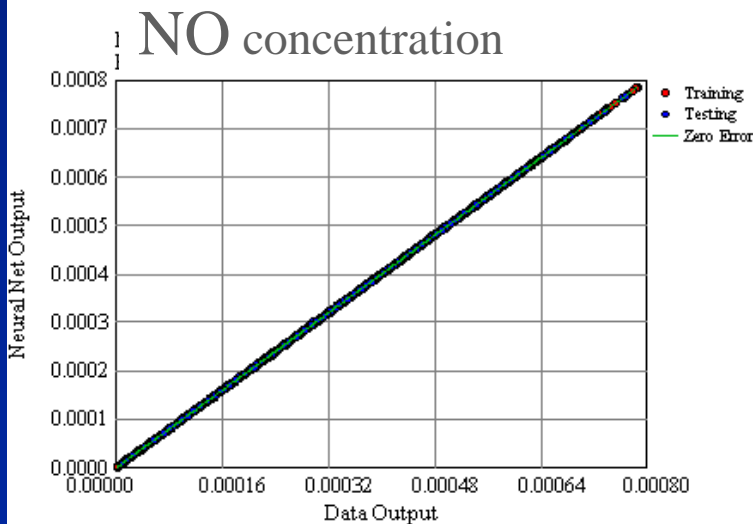
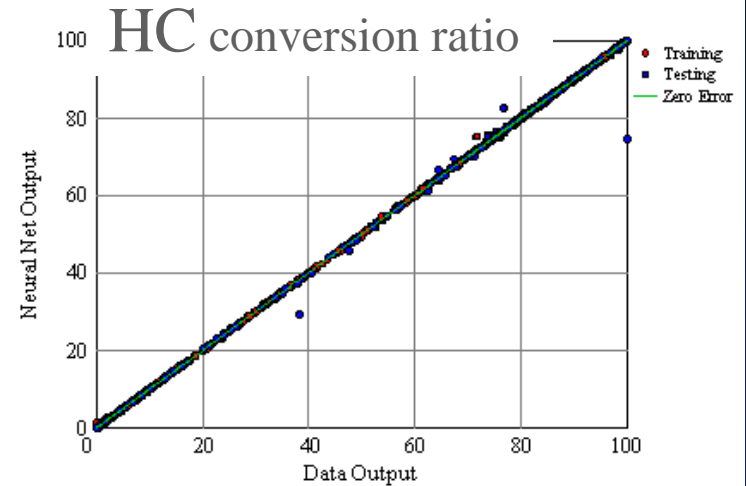
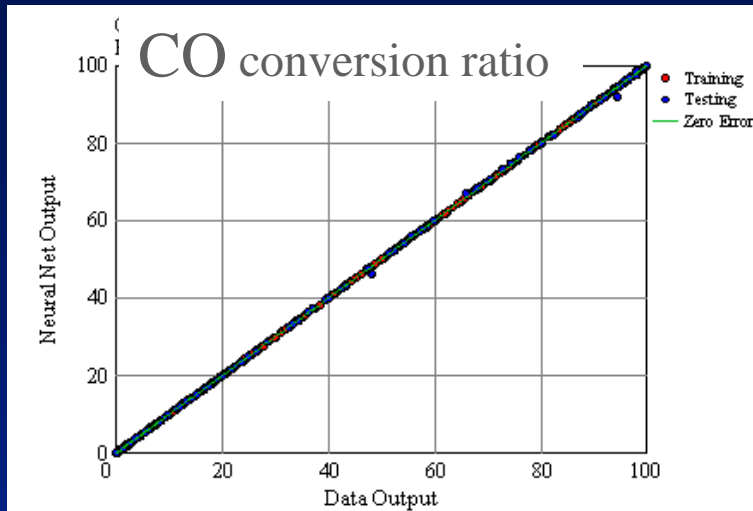
Conclusions



Conversion Efficiency



- DOC



Solution Overview

Calibration

Q-S Solver

SCR

DOC

Aged DOC

SIL/HIL /NN

2D/3D Model

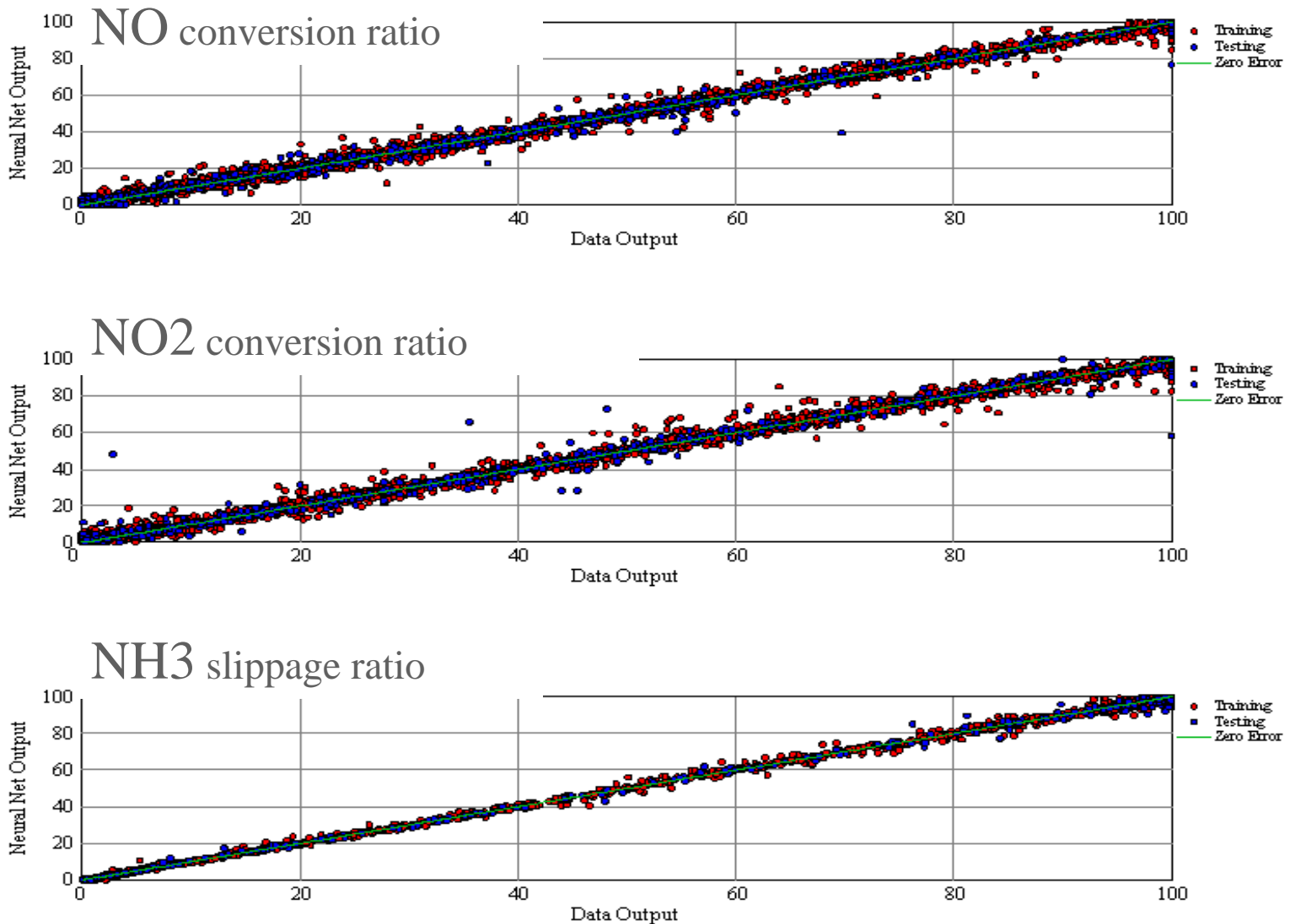
Conclusions



Conversion Efficiency



- SCR

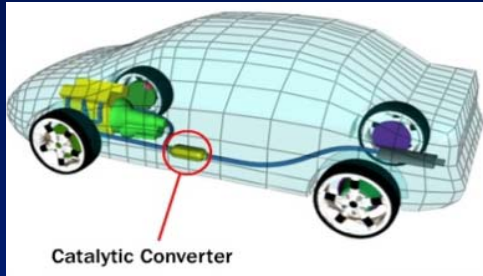


- Solution Overview
- Calibration
- Q-S Solver
- SCR
- DOC
- Aged DOC
- SIL/HIL /NN
- 2D/3D Model
- Conclusions





SIL/HIL Enabled Engine/NN-AT Model



Solution Overview

Calibration

Q-S Solver

SCR

DOC

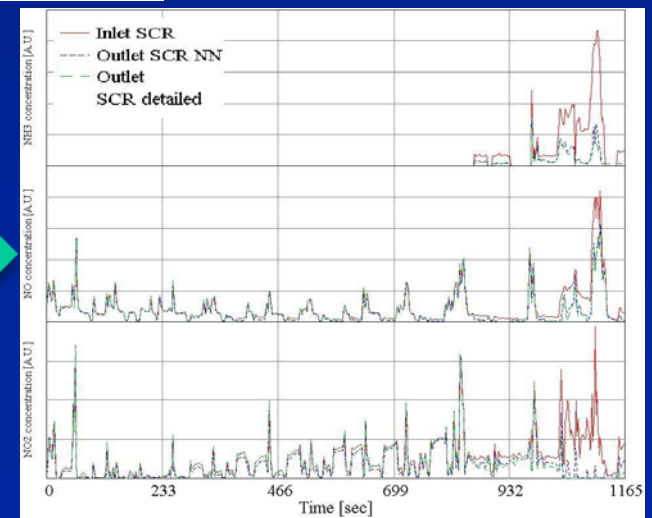
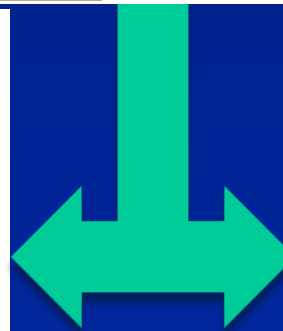
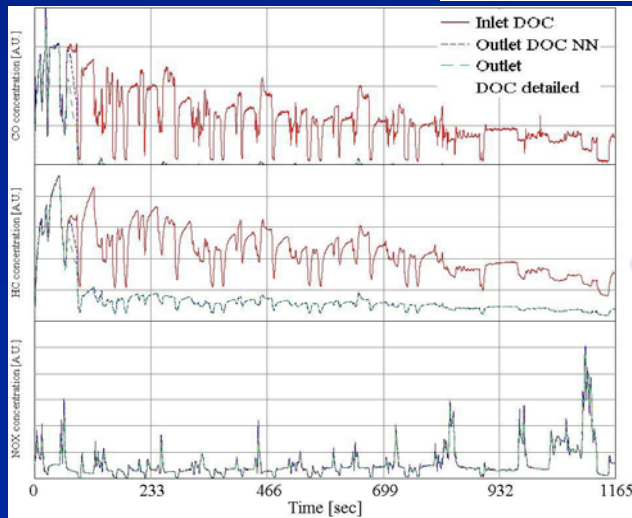
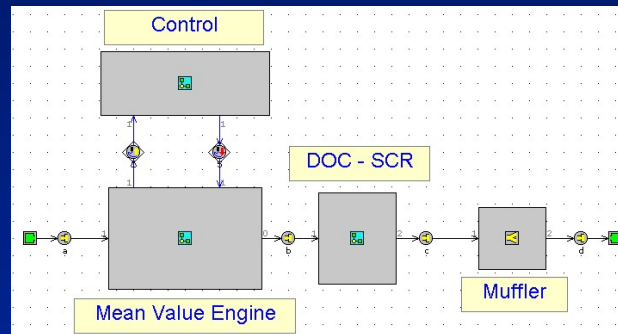
Aged DOC

SIL/HIL /NN



2D/3D Model

Conclusions



Computational Speed Comparison (1180s NDEC)



Model Type	Solver	CPU
Standalone Kinetic AT	QS	90s
Standalone Neural Network AT	Explicit	2s
Detailed Engine + Kinetic AT	Explicit	60h
MV Engine + Kinetic AT	Explicit	39h
MV Engine (Explicit) + Kinetic AT (QS)	Mixed	635s
MV Engine + Neural Network AT	Explicit	625s
MV Engine + Neural Network AT	GT-Suite RT	331s

Solution
Overview

Calibration

Q-S
Solver

SCR

DOC

Aged DOC

SIL/HIL /NN



2D/3D Model

Conclusions

Pseudo-Multi-D Methodologies



Are real time 3-D simulations possible?



3D - vs- 1D



– Based on thermal object

- Explicit discretization
- Discretized CatalystBrick and thermal objects

– Based on Mathematical formulation (3-D conduction solution)

- Implicit discretization
- Diesel particulate filters

Solution
Overview

Calibration

Q-S
Solver

SCR

DOC

Aged DOC

SIL/HIL /NN

2D/3D Model

Conclusions



Aftertreatment Simulation

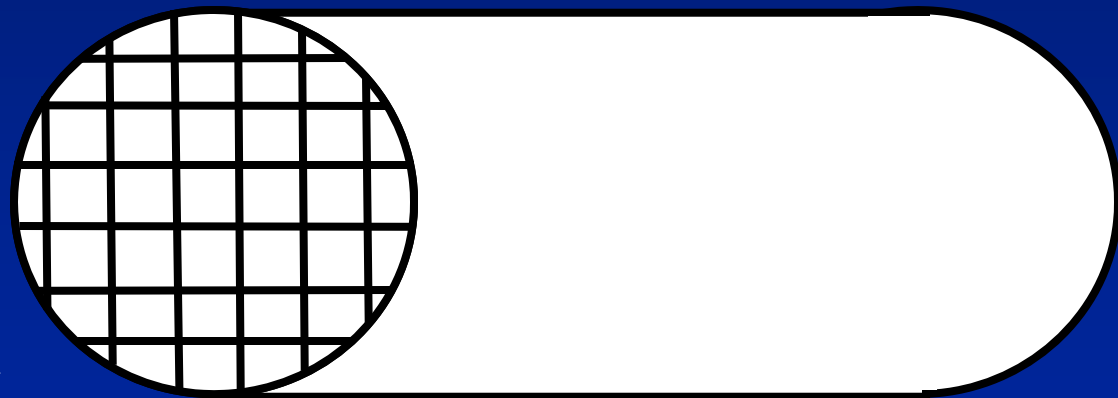


- **Modeling Techniques**

- **3D: model discretized in X, Y, and Z direction**
 - captures heat loss to environment
 - allows for non-uniform inlet flow
 - most computationally demanding



Inlet Flow



Solution
Overview

Calibration

Q-S
Solver

SCR

DOC

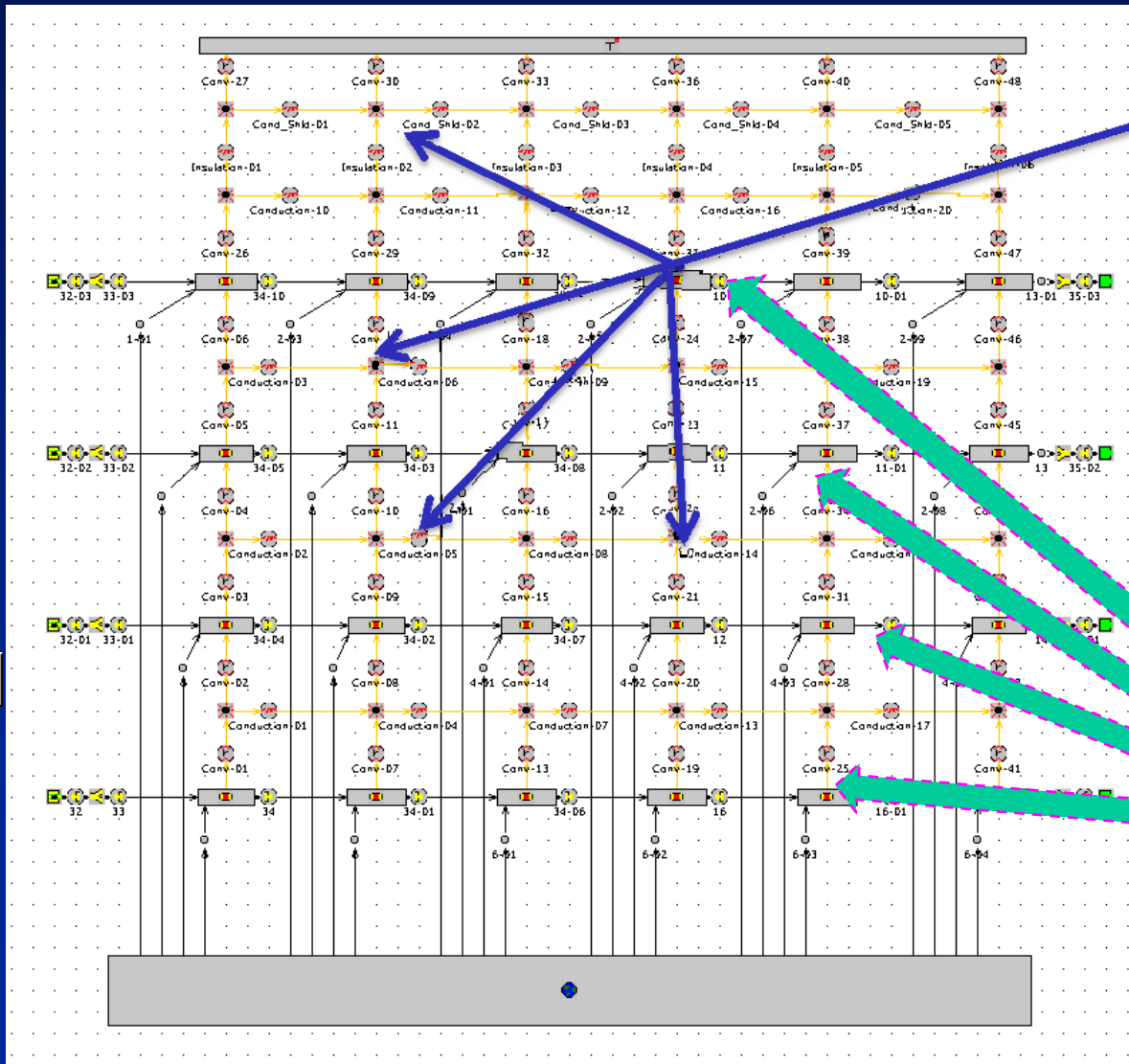
Aged DOC

SIL/HIL /NN

2D/3D Model

Conclusions

Aftertreatment Simulation



Thermal links

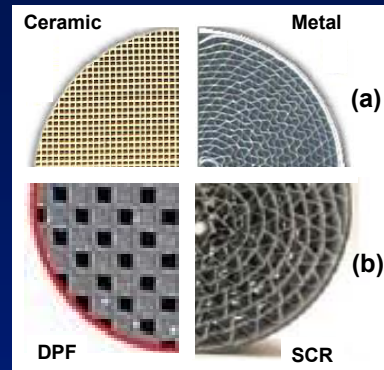
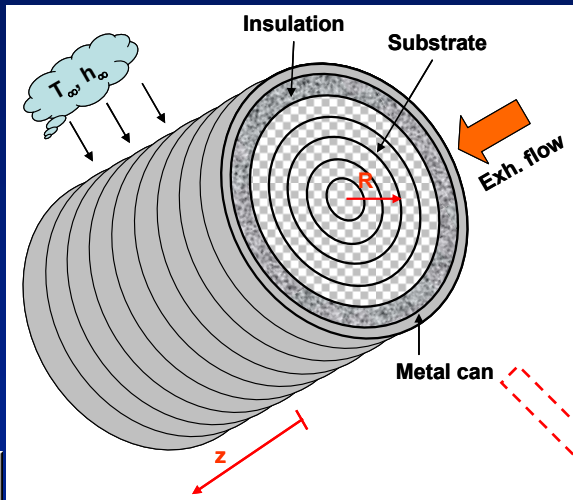
- Solution Overview
- Calibration
- Q-S Solver
- SCR
- DOC
- Aged DOC
- SIL/HIL /NN
- 2D/3D Model
- Conclusions



Representative Channel Approach

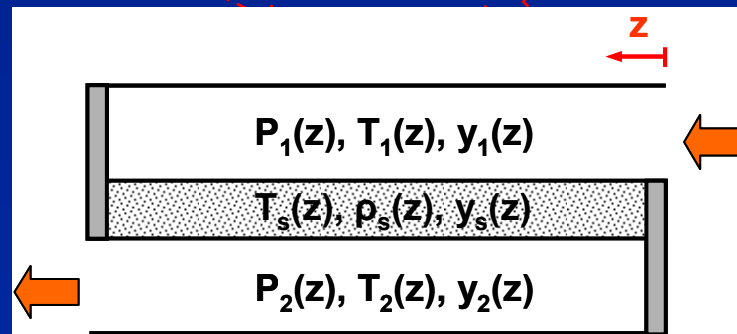
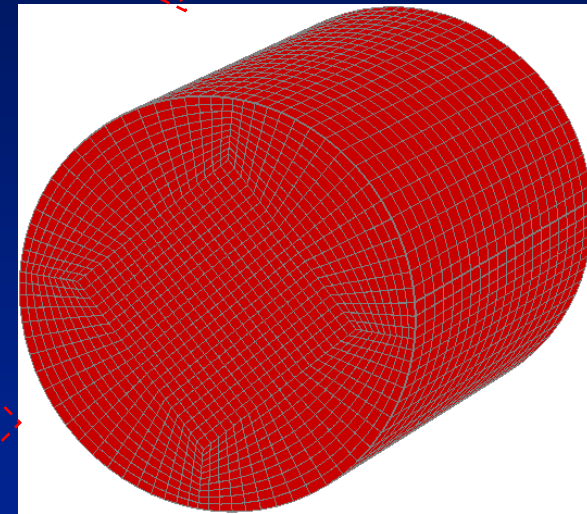


- Solution Overview
- Calibration
- Q-S Solver
- SCR
- DOC
- Aged DOC
- SIL/HIL /NN
- 2D/3D Model
- Conclusions

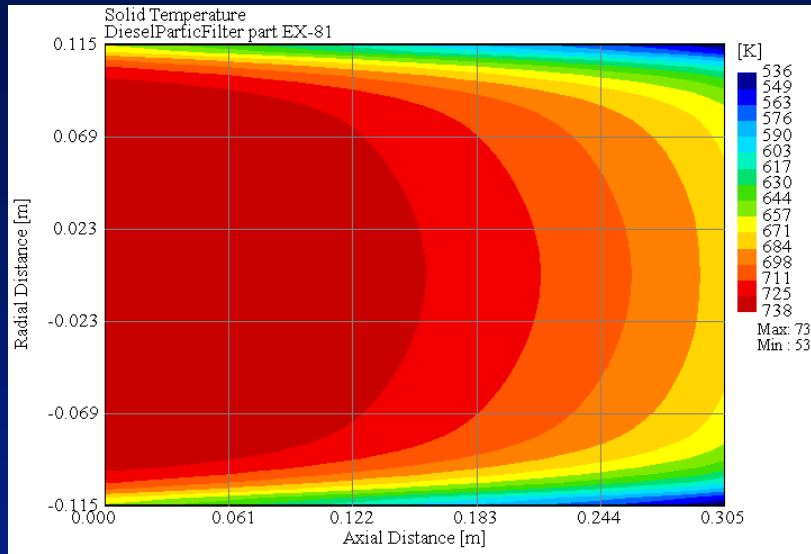


2D

3D

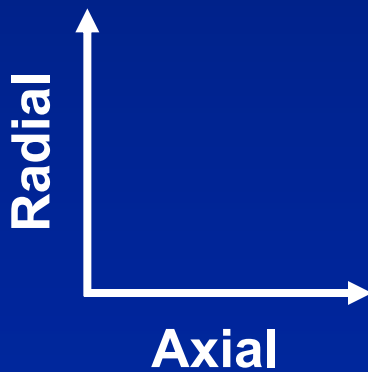
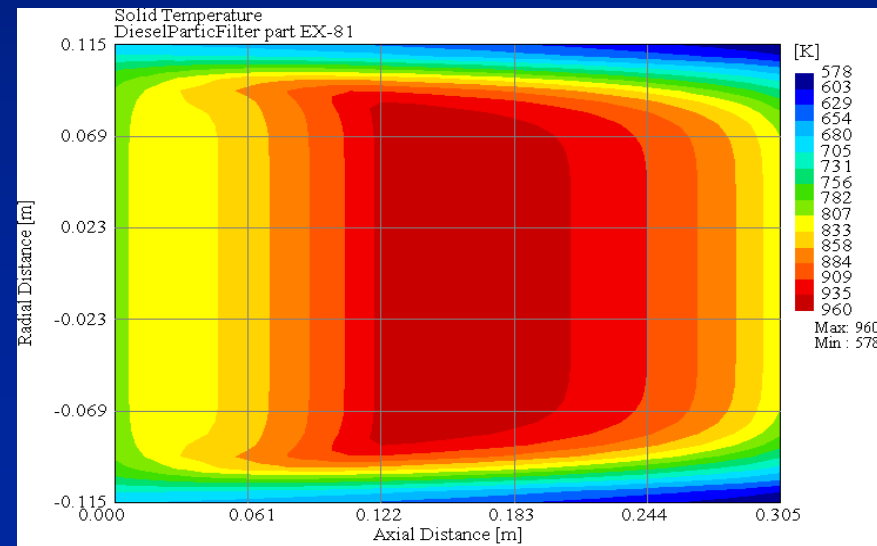


Typical Transient 2D Results



Warm-up

Regeneration



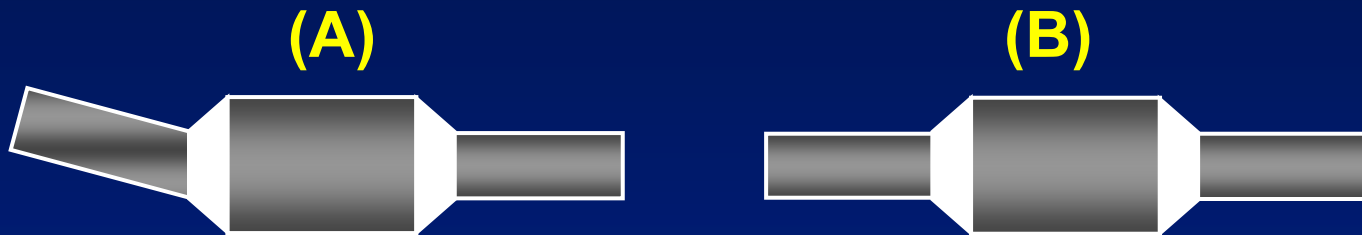
- Solution Overview
- Calibration
- Q-S Solver
- SCR
- DOC
- Aged DOC
- SIL/HIL /NN
- 2D/3D Model
- Conclusions



Non-uniform Flow Distributions



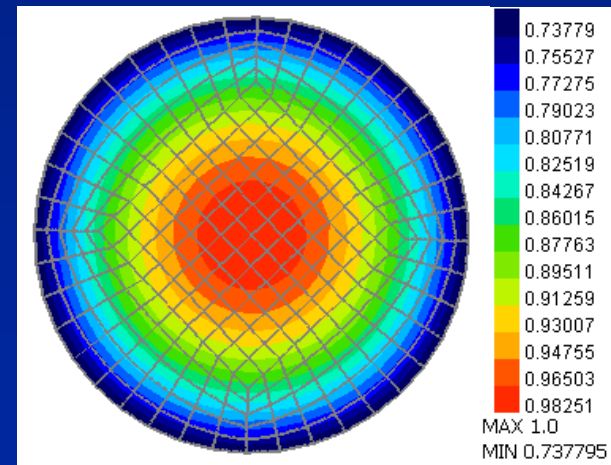
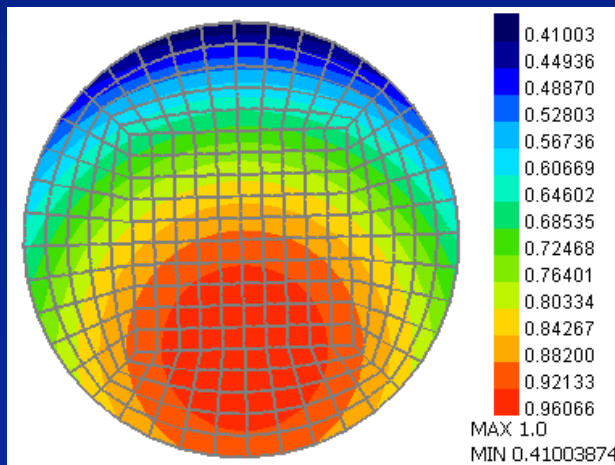
Physical layout out



Pseudo front inlet mass flow rate intensity

(A)

(B)



Solution Overview

Calibration

Q-S Solver

SCR

DOC

Aged DOC

SIL/HIL /NN

2D/3D Model

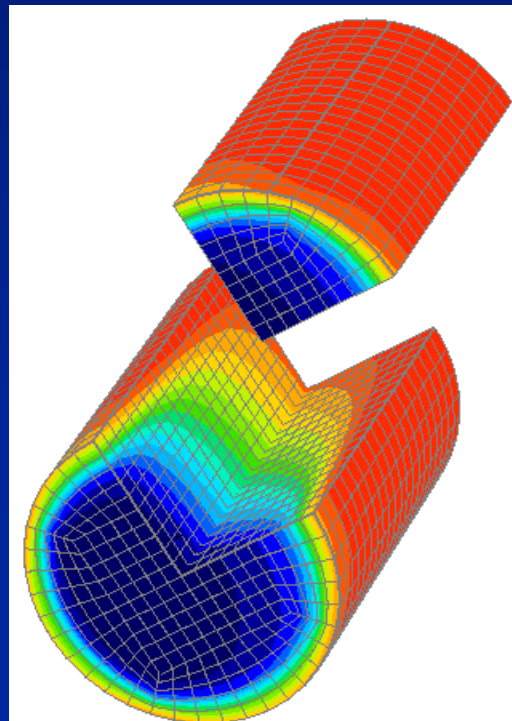
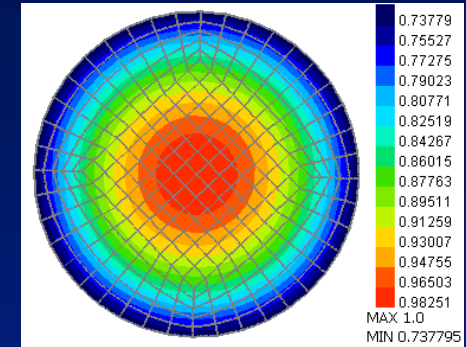
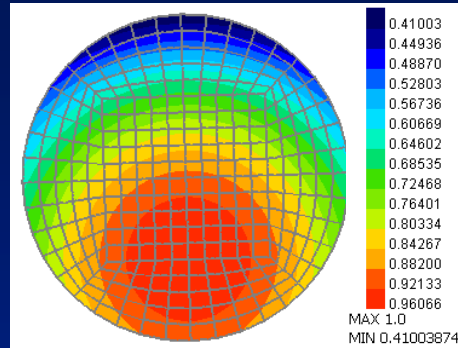
Conclusions



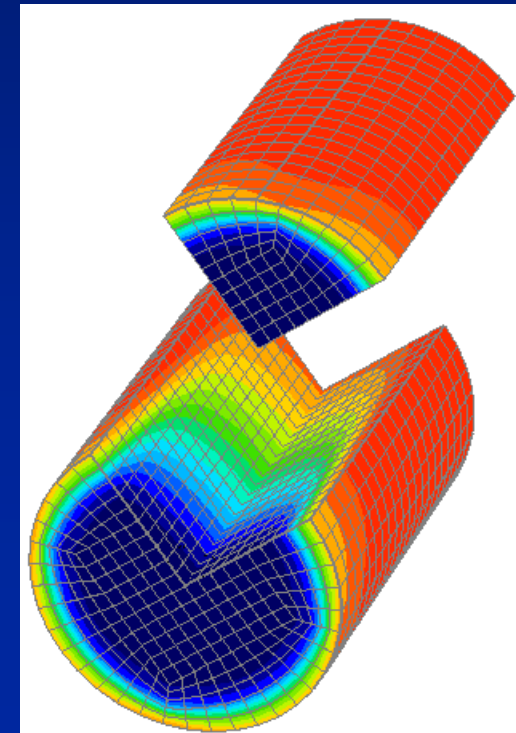
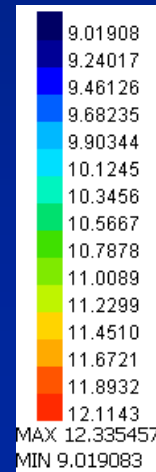


Typical Transient 3D Results

Non-uniform front inlet mass flow rate intensity



Loading Density at 110 sec. (g/L)



Solution
Overview

Calibration

Q-S
Solver

SCR

DOC

Aged DOC

SIL/HIL /NN

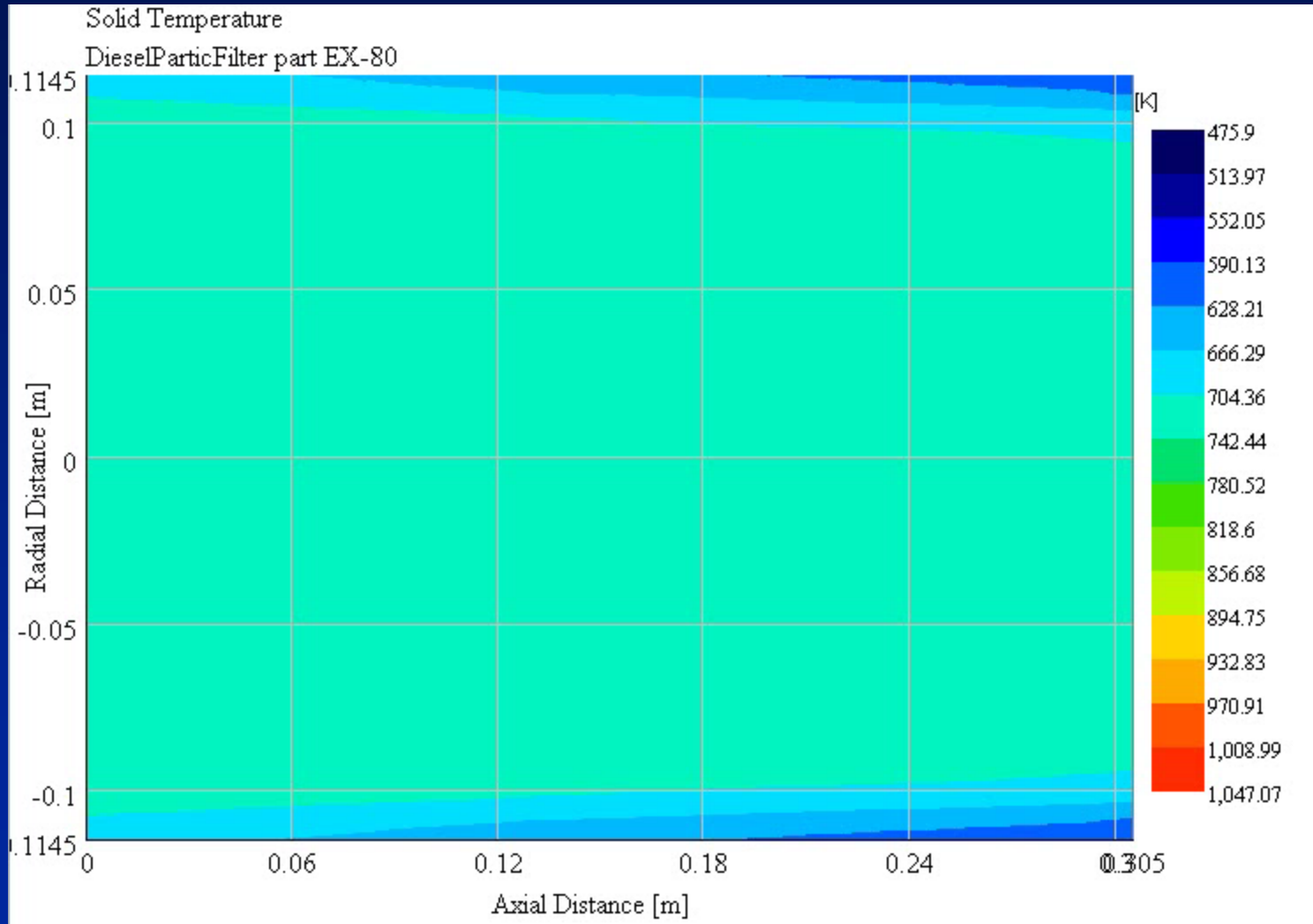
2D/3D Model

Conclusions



Typical Transient 2D Results

DPF Regeneration Animation



Solution
Overview

Calibration

Q-S
Solver

SCR

DOC

Aged DOC

SIL/HIL /NN

2D/3D Model

Conclusions





Conclusion

- A *Quasi-steady (QS)* based solver have been implemented that conserves accuracy of the computationally demanding fully explicit solver
- Calibration of global kinetics was shown to be computationally efficient using DOE direct optimizers
- Feasibility of SIL/HIL compatible model generation was demonstrated using detailed kinetic model
- Various levels of modeling were demonstrated:
Detailed engine/vehicle + detailed kinetics to mean-value engine/vehicle + NN/AT model
- 1-D methodology was extended to simulate multi-dimensional effects using QS based quasi 2D/3D development

Solution
Overview

Calibration

Q-S
Solver

SCR

DOC

Aged DOC

SIL/HIL /NN

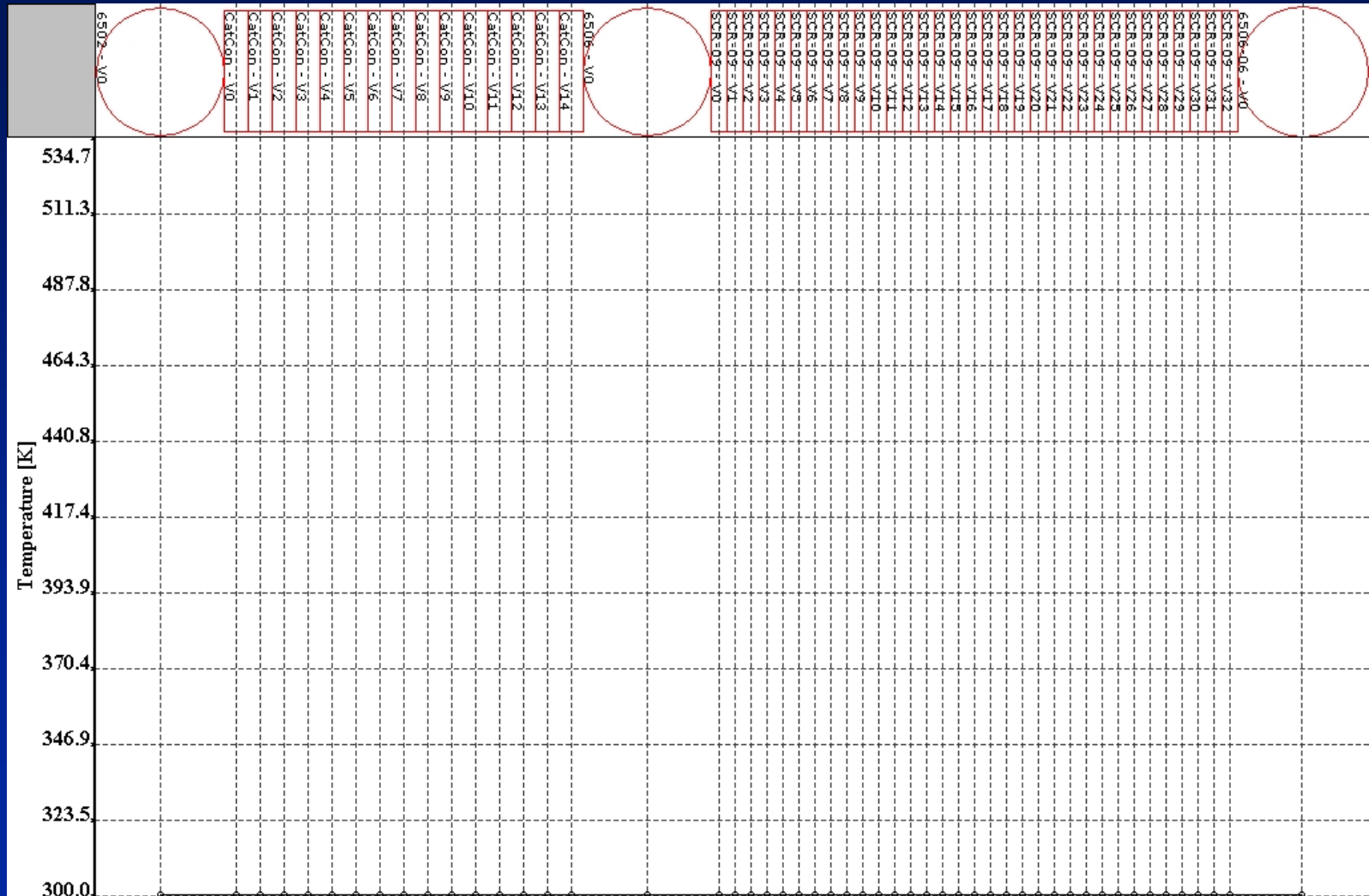
2D/3D Model

Conclusions





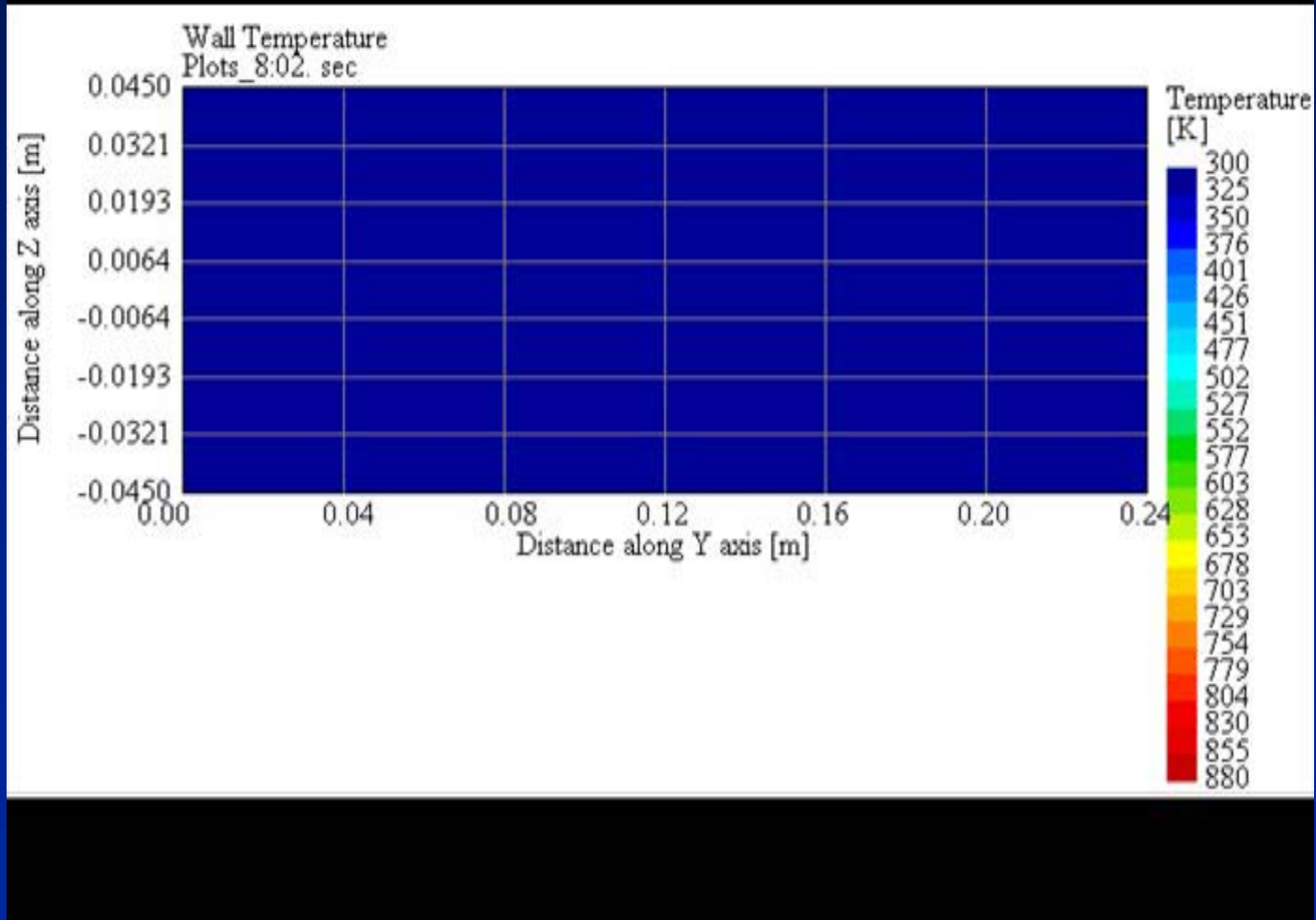
1-D Catalyst Simulation



- Solution Overview
- Calibration
- Q-S Solver
- SCR
- DOC
- Aged DOC
- SIL/HIL /NN
- 2D/3D Model
- Conclusions



2-D Catalyst Simulation



Solution
Overview

Calibration

Q-S
Solver

SCR

DOC

Aged DOC

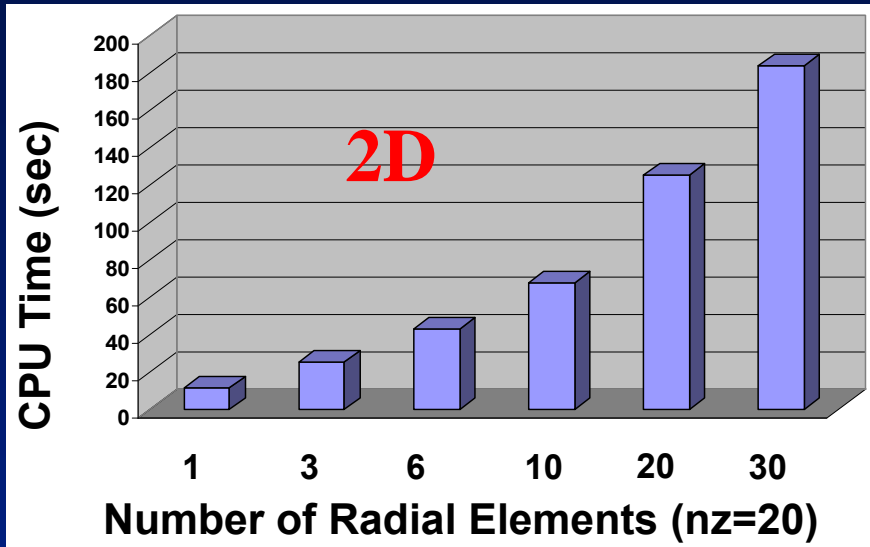
SIL/HIL /NN

2D/3D Model

Conclusions

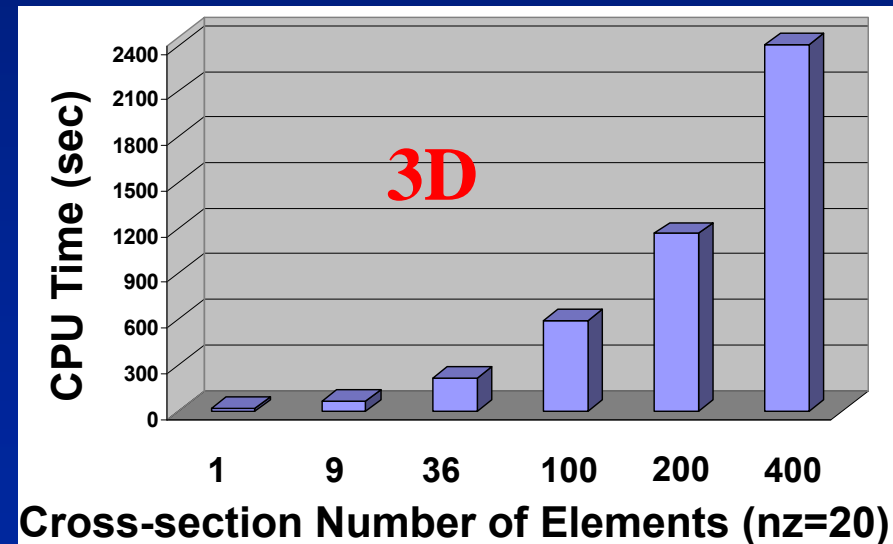


Computational Speed Consideration



With regeneration rxn
Axial nodes = 21
300 second duration
 $dt = 0.1$ sec.
AMD 1.8 GHz, 1.28 GB RAM

**Real time is POSSIBLE
for 2D/3D AT simulation**



- Solution Overview
- Calibration
- Q-S Solver
- SCR
- DOC
- Aged DOC
- SIL/HIL /NN
- 2D/3D Model
- Conclusions

